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Inconsistent Ontology Handling by Translating Description Logics into Defeasible Logic Programming *

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Abstract

The Semantic Web is a future vision of the web where stored information has exact meaning, thus enabling computers to understand and reason on the basis of such information. Assigning semantics to web resources is addressed by means of ontology definitions which are meant to be written in an ontology description language such as OWL-DL that is based on so-called Description Logics (DL). Although ontology definitions expressed in DL can be processed with existing DL reasoners, such DL reasoners are incapable of dealing with inconsistent ontology definitions.

Previous research has determined that a subset of DL can be effectively translated into an equivalent subset of logic programming. We propose a method for dealing with inconsistent ontology definitions in the Semantic Web. Our proposal involves mapping DL ontologies into DeLP programs. That is, given an OWL-DL ontology $O_{owl}$, an equivalent DL ontology $O_{DL}$ can be obtained. Provided $O_{DL}$ satisfies certain restrictions, it can be translated into a DeLP program $O_{DeLP}$. Therefore, given a query $Q$ w.r.t. $O_{owl}$, a dialectical process will be performed to determine if $Q$ is warranted w.r.t. $O_{DeLP}$.

Keywords: Semantic web, defeasible argumentation, Description Logics, Defeasible Logic Programming, inconsistent ontology handling.

1 Introduction

The Semantic Web [3] is a future vision of the web where stored information has exact meaning, thus enabling computers to understand and reason on the basis of such information. Assigning semantics to web resources is addressed by means of ontology definitions. The term ontology stands for a specification of a conceptualization, that is to say a description of the concepts and relationships that can exist for an agent or a community of agents.

As proposed by the World Wide Web Consortium...
(W3C)\(^1\), ontology definitions are meant to be written in an ontology description language such as OWL [16], whose subset known as OWL-DL is based on so-called Description Logics (DL) [1]. Although ontology definitions expressed in DL can be processed with existing DL reasoners (e.g., RACER [14]), such DL reasoners are incapable of dealing with inconsistent ontology definitions. In particular, when a DL reasoner is presented with an inconsistent ontology definition, it will be unable to extract any useful consequences from it.

However, previous research [13] has determined that a subset of DL can be effectively translated into an equivalent subset of Horn logic. In particular, DeLP is an argumentative framework based on logic programming that is capable of dealing with possibly inconsistent knowledge bases codified as a set of Horn-like clauses [8]. When presented with a query \( Q \) w.r.t. a KB \( \mathcal{P} \), DeLP performs a dialectical process in which all arguments in favor and against \( Q \) are considered. In such a process, arguments regarded as ultimately undefeated will be considered warranted.

In this article, we propose a method for dealing with inconsistent ontology definitions in the Semantic Web. Our proposal involves mapping DL ontologies into a DeLP program. That is, given an OWL-DL ontology \( \mathcal{O}_{\text{Owl}} \), an equivalent DL ontology \( \mathcal{O}_{\text{DL}} \) can be obtained. Provided \( \mathcal{O}_{\text{DL}} \) satisfies certain restrictions, it can be translated into a DeLP program \( \mathcal{O}_{\text{DeLP}} \). Then given a query \( Q \), a dialectical process will be performed to determine if \( Q \) is warranted w.r.t. \( \mathcal{O}_{\text{DeLP}} \).

**Outline:** Section 2 introduces the fundamentals of Description Logics. Section 3 briefly explains the Defeasible Logic Programming formalism. Section 4 introduces how the mapping from DL to DeLP is performed. Section 5 explains how inconsistent ontology definitions are handled within DeLP. Section 6 briefly analyzes features of and extensions to the presented approach. Section 7 discusses related work. Finally Section 8 concludes.

## 2 Description Logics

**Description Logics** (DL) are a well-known family of knowledge representation formalisms [1]. They are based on the notions of concepts (unary predicates, classes) and roles (binary relations), and are mainly characterized by constructors that allow complex concepts and roles to be built from atomic ones. The expressive power of a DL system is determined by the constructs available for building concept descriptions, and by the way these descriptions can be used in the terminological (Tbox) and assertional (Abox) components of the system.

We now describe the basic language for building DL expressions. Let \( C \) and \( D \) stand for concepts and \( R \) for a role name. Concept descriptions are built from concept names using the constructors conjunction (\( C \cap D \)), disjunction (\( C \cup D \)), negation (\( \neg C \)), existential restriction (\( \exists R.C \)), and value restriction (\( \forall R.C \)). To define the semantics of concept descriptions, concepts are interpreted as subsets of a domain of interest, and roles as binary relations over this domain. An interpretation \( I \) consists of a non-empty set \( \Delta^I \) (the domain of \( I \)) and a function \( ^I \) (the interpretation function of \( I \)) which maps every concept name \( A \) to a subset \( A^I \) of \( \Delta^I \), and every role name \( R \) to a subset \( R^I \) of \( \Delta^I \times \Delta^I \). The interpretation function is extended to arbitrary concept descriptions as follows: \( \neg C^I = \Delta^I \setminus C^I \); \( C \cap D^I = C^I \cap D^I \); \( C \cup D^I = C^I \cup D^I \); \( \exists R.C^I = \{ x s.t. (x, y) \in R^I \text{ and } y \in C^I \} \), and \( \forall R.C^I = \{ x | \forall y, (x, y) \in R^I \text{ implies } y \in C^I \} \). Besides, the expressions \( \top \) and \( \bot \) are short-hands for \( C \sqcup \neg C \) and \( C \sqcap \neg C \), resp. Further extensions to the basic DL are possible including inverse and transitive roles noted as \( P^- \) and \( P^+ \), resp.

A DL knowledge base (KB) \( KB = (T, A) \) consists of two finite and mutually disjoint sets: the Tbox \( T \) which introduces the terminology and the Abox \( A \) which contains facts about particular objects in the application domain. Tbox statements have the form \( C \sqsubseteq D \) (inclusions) and \( C \equiv D \) (equalities), where \( C \) and \( D \) are (possibly complex) concept descriptions.

The semantics of Tbox statements is as follows. An interpretation \( I \) satisfies \( C \sqsubseteq D \) iff \( C^I \subseteq D^I \), \( I \) satisfies \( C \equiv D \) iff \( C^I = D^I \). Objects in the Abox are referred to by a finite number of individual names and these names may be used in two types of assertional statements: concept assertions of the type \( C(a) \) and role assertions of

\(^1\)www.w3c.org
Consider the ontology $KB = (T, A)$ in Figure 1 about flying animals. Sentence (1) in the Tbox $T$ says that every bird is an animal, sentence (2) says that every bird flies. Sentences (3) and (4) say that eagles and penguins are birds. Sentences (5), (6) and (7) say that penguins do not fly unless they are genetically-altered, where a genetically-altered penguin is a penguin that has been operated by a genetic surgeon. Sentence (8) establishes that eagles with a broken wing are no longer able to fly. Sentence (9) defines relation $\text{isOperatedBy}$ as the inverse of relation operates. Finally, sentence (10) defines a genetic surgeon as a geneticist who is also a surgeon.

Sentence (11) in the Abox $A$ expresses that Opus is a penguin. Sentences (12) and (13) establish that Avenger is an eagle who has a broken wing. Sentences (14) and (15) say that Frankenstein is both a geneticist and a surgeon, resp. Finally, sentence (16) establishes that Frankenstein has operated Opus.

Figure 1. Description Logics knowledge base $KB = (T, A)$ about flying animals

3 Declarative Logic Programming

Declarative Logic Programming (DeLP) [8] provides a language for knowledge representation and reasoning that uses declarative argumentation [6, 17, 18] to decide between contradictory conclusions through a dialectical analysis. Codifying knowledge by means of a DeLP program provides a good trade-off between expressivity and implementability. Recent research has shown that DeLP provides a suitable framework for building real-world applications (e.g., clustering algorithms [9] and intelligent web forms [10, 12]) that deal with incomplete and potentially contradictory information.

In a declarative logic program $P = (\Pi, \Delta)$, a set $\Delta$ of declarative rules $P \leftarrow Q_1, \ldots, Q_n$, and a set $\Pi$ of strict rules $P \leftarrow Q_1, \ldots, Q_n$ can be distinguished. Deriving literals in DeLP results in the construction of arguments. An argument $A$ is a (possibly empty) set of ground defeasible rules that together with the set $\Pi$ provide a logical proof for a given literal $Q$, satisfying the additional requirements of non-contradiction and minimality. Formally:

**Definition 1 (Argument)** Given a DeLP program $P$, an argument $A$ for a query $Q$, denoted $(A, Q)$, is a subset of ground instances of defeasible rules in $P$, such that: (1) there exists a defeasible derivation for $Q$ from $\Pi \cup A$; (2) $\Pi \cup A$ is non-contradictory (i.e., $\Pi \cup A$ does not entail two complementary literals $P$ and $\neg P$), and (3) there is no $A' \subseteq A$ such that there exists a defeasible derivation for $Q$ from $\Pi \cup A'$. An argument $(A_1, Q_1)$ is a sub-argument of another argument $(A_2, Q_2)$ if $A_1 \subseteq A_2$. Given a DeLP program $P$, $\text{Args}(P)$ denotes the set of all possible arguments that can be derived from $P$.

The notion of defeasible derivation corresponds to the usual query-driven SLD derivation used in logic programming, performed by backward chaining on both strict and defeasible rules; in this context a negated literal $\neg P$ is treated just as a new predicate name $\text{no}_P$. Minimality imposes a kind of ‘Ockham’s razor principle’ [18] on argument construction. The non-contradiction requirement forbids the use of (ground instances
of) defeasible rules in an argument \( \mathcal{A} \) whenever \( \Pi \cup \mathcal{A} \) entails two complementary literals. The notion of contradiction is captured by the notion of counterargument.

**Definition 2 (Counterargument. Defeat)**

An argument \( \langle A_1, Q_1 \rangle \) is a counterargument for an argument \( \langle A_2, Q_2 \rangle \) if there is a subargument \( \langle A, Q \rangle \) of \( \langle A_2, Q_2 \rangle \) such that the set \( \Pi \cup \{ Q_1, Q \} \) is contradictory. An argument \( \langle A_1, Q_1 \rangle \) is a defeater for an argument \( \langle A_2, Q_2 \rangle \) if \( \langle A_1, Q_1 \rangle \) counterargues \( \langle A_2, Q_2 \rangle \), and \( \langle A_1, Q_1 \rangle \) is preferred over \( \langle A_2, Q_2 \rangle \) w.r.t. a preference criterion \( \succeq \) on conflicting arguments. Such criterion is defined as a partial order \( \preceq \subseteq \text{Args}(\mathcal{P}) \times \text{Args}(\mathcal{P}) \). The argument \( \langle A_1, Q_1 \rangle \) will be called a proper defeater for \( \langle A_2, Q_2 \rangle \) if \( \langle A_1, Q_1 \rangle \) is strictly preferred over \( \langle A, Q \rangle \) w.r.t. \( \preceq \); if \( \langle A_1, Q_1 \rangle \) and \( \langle A, Q \rangle \) are unrelated to each other will be called a blocking defeater for \( \langle A_2, Q_2 \rangle \).

Generalized specificity [18] is typically used as a syntax-based criterion among conflicting arguments. However, other alternative partial orders could also be valid. In particular, in this article we are going to use the criterion based on rule comparison introduced in [8]:

**Definition 3 (Rule comparison criterion)**

Let \( \succ \) be a preference relation explicitly defined among defeasible rules. Given two arguments \( \langle A_1, H_1 \rangle \) and \( \langle A_2, H_2 \rangle \), the argument \( \langle A_1, H_1 \rangle \) will be preferred over \( \langle A_2, H_2 \rangle \) if: (1) there exists at least one rule \( r_a \in A_1 \) and one rule \( r_b \in A_2 \) such that \( r_a \succ r_b \), and (2) there is no \( r'_b \in A_2 \) and \( r'_a \in A_1 \) such that \( r'_a \succ r'_b \).

In order to determine whether a given argument \( \mathcal{A} \) is ultimately undefeated (or warranted), a dialectical process is recursively carried out, where defeaters for \( \mathcal{A} \), defeaters for these defeaters, and so on, are taken into account. An argumentation line starting in an argument \( \langle A_0, Q_0 \rangle \) is a sequence \([\langle A_0, Q_0 \rangle, \langle A_1, Q_1 \rangle, \langle A_2, Q_2 \rangle, \ldots, \langle A_n, Q_n \rangle \ldots]\) that can be thought of as an exchange of arguments between two parties, a proponent (evenly-indexed arguments) and an opponent (oddly-indexed arguments). Each \( \langle A_i, Q_i \rangle \) is a defeater for the previous argument \( \langle A_{i-1}, Q_{i-1} \rangle \) in the sequence, \( i > 0 \). In order to avoid fallacious reasoning, dialectics imposes additional constraints on such an argument exchange to be considered rationally acceptable.

Given a DeLP program \( \mathcal{P} \) and an initial argument \( \langle A_0, Q_0 \rangle \), the set of all acceptable argumentation lines starting in \( \langle A_0, Q_0 \rangle \) accounts for a whole dialectical analysis for \( \langle A_0, Q_0 \rangle \) (i.e., all possible dialogues about \( \langle A_0, Q_0 \rangle \) between proponent and opponent), formalized as a dialectical tree.

Nodes in a dialectical tree \( T_{\langle A_0, Q_0 \rangle} \) can be marked as undefeated and defeated nodes (U-nodes and D-nodes, resp.). A dialectical tree will be marked as an AND-OR tree: all leaves in \( T_{\langle A_0, Q_0 \rangle} \) will be marked U-nodes (as they have no defeaters), and every inner node is to be marked as D-node iff it has at least one U-node as a child, and as U-node otherwise. An argument \( \langle A_0, Q_0 \rangle \) is ultimately accepted as valid (or warranted) wrt a DeLP program \( \mathcal{P} \) iff the root of its associated dialectical tree \( T_{\langle A_0, Q_0 \rangle} \) is labelled as U-node.

Given a DeLP program \( \mathcal{P} \), solving a query \( Q \) w.r.t. \( \mathcal{P} \) accounts for determining whether \( Q \) is supported by (at least) one warranted argument. Different doxastic attitudes can be distinguished as follows: Yes, accounts for believing \( Q \) iff there is at least one warranted argument supporting \( Q \) on the basis of \( \mathcal{P} \); No, accounts for believing \( \neg Q \) iff there is at least one warranted argument supporting \( \neg Q \) on the basis of \( \mathcal{P} \); Undecided, neither \( Q \) nor \( \neg Q \) are warranted w.r.t. \( \mathcal{P} \), and Unknown, \( Q \) does not belong to the signature of \( \mathcal{P} \).

For an example of DeLP, see Examples 2 and 3 in Sections 4 and 5, resp.

### 4 Translating from DL to DeLP for Reasoning with Individuals

As explained above DL ontologies can be inconsistent. Notably DL reasoners such as RACER [14] are incapable of dealing with such situations. When presented with such inconsistent ontologies, RACER will issue an error message and will stop further processing.

Grosop et al. [13] have identified a subset of DL languages that can be effectively mapped into a Horn-clause logics. Accordingly, our work is based on such research by adapting it to the DeLP framework. We therefore propose translating a DL ontology \( \mathcal{KB} = (T, A) \) into a DeLP
program \( P = (\Pi, \Delta) \) by means of a mapping \( T \) such that \( P = T(KB) \). Intuitively the set \( \Pi \) of strict rules in \( P \) will correspond to the Abox \( A \) in \( KB \) while the set \( \Delta \) of defeasible rules will correspond to the Tbox \( T \) in \( KB \). In the rest of this section, we will explain how to achieve the translation of DL KB into DeLP programs exemplifying the process with the DL KB described in Example 1. Moreover, defeasible rules of the form "\( H \leftarrow B_1, \ldots, B_n \)" will be written for clarity as "\( H \leftarrow B_1 \wedge \ldots \wedge B_n \)".

4.1 Translating Statements

For maintaining backward compatibility with previous knowledge representation languages, part of OWL-DL constructs are based on RDF Schema (RDFS). RDFS provides a subset of the DL statements (subclass, subproperty, range, and domain statements), which in a DL setting are called Tbox axioms, and asserted class-instance (type) and instance-property-instance relationships (which in a DL setting are called Abox axioms). A DL inclusion axiom \( C \subseteq D \) corresponds to a first-order logic (FOL) implication \( (\forall x)(C(x) \rightarrow D(x)) \). Then class and property axioms maps to DeLP axioms as: Class \( C \) is subclass of class \( D \) maps to "\( D(X) \leftarrow C(X) \)" and property \( P \) is a subproperty of property \( P \) maps to "\( P(X,Y) \leftarrow Q(X,Y) \)" where \( X \) and \( Y \) are variable names. The range and domain statements map as follows: the range of property \( P \) is class \( C \) (noted as \( \Pi \subseteq \forall P.C \)) maps to "\( C(Y) \leftarrow P(X,Y) \)" and the domain of property \( P \) is in class \( C \) (noted as \( \forall \exists P.C \)) maps to "\( C(Y) \rightarrow P(X,Y) \)". Asserted class-instance (type) and instance-property-instance relationships, which correspond to DL axioms of the form "\( C(a) \)" and "\( P(a,b) \)" , where \( a \) and \( b \) are constants.

Class and property equivalence axioms can be replaced with a symmetrical pair of inclusion axioms, so they can be mapped to a symmetrical pair of DeLP rules as follows: the class \( C \) is equivalent to the class \( D \) (noted as \( C \equiv D \)) maps to the set of DeLP rules \( \{ C(X) \leftarrow D(X); D(X) \rightarrow C(X) \} \) and the property \( P \) is equivalent to the property \( Q \) (noted as \( P \equiv Q \)) maps to the set of DeLP rules \( \{ P(X,Y) \leftarrow Q(X,Y); Q(X,Y) \rightarrow P(X,Y) \} \). Inverse and transitivity axioms can also be translated: the property \( P \) is the inverse of the property \( Q \) (noted as \( P \equiv Q^- \)) maps to the set of DeLP rules \( \{ Q(Y,X) \leftarrow P(X,Y); P(X,Y) \leftarrow Q(Y,X) \} \) and the property \( P \) is transitive (noted as \( P^+ \subseteq P \)) maps to "\( P(X,Z) \leftarrow P(X,Y) \wedge P(Y,Z) \)".

4.2 Translating Class Constructors

In the previous section we showed how DL axioms correspond with DeLP rules, and how these can be used to make statements about classes and properties. In DL the classes appearing in such axioms need not be atomic, but can be complex compound expressions built up from atomic classes and properties using a variety of constructors. Next we will show how these DL expressions correspond to expressions in the body of DeLP rules. We will use \( C, D \) to denote classes, and \( P, Q \) to denote properties.

Conjunctions: A DL class can be formed by conjoining existing classes (noted as \( C \cap D \)), which corresponds to a conjunction of unary predicates. Conjunction can be directly expressed in the body of a DeLP rule. When a conjunction occurs on the left-hand side (l.h.s.) of a subclass axiom (as in \( C_1 \cap C_2 \subseteq D \)) it becomes a conjunction in the body of the corresponding rule "\( D(X) \leftarrow C_1(X) \wedge C_2(X) \)". When a conjunction occurs on the right-hand side (r.h.s.) of a subclass axiom (as in \( C \subseteq D_1 \cap D_2 \)), it becomes conjunction in the head of the rule "\( D_1(X) \wedge D_2(X) \rightarrow C(X) \)"; this can be transformed (via Lloyd-Topor transformations) into a set of DeLP rules \( \{(D_1(X) \leftarrow C(X)) ; (D_2(X) \leftarrow C(X)) \} \).

Disjunctions: A DL class can be formed from a disjunction of existing classes (noted as \( C \sqcup D \)), which corresponds to a disjunction of unary predicates. When a disjunction occurs on the l.h.s. of a subclass axiom (as in \( C_1 \sqcup C_2 \subseteq D \)) it becomes a disjunction in the body of the rule "\( D(X) \leftarrow C_1(X) \vee C_2(X) \)"; this is transformed (by Lloyd-Topor) into a pair of DeLP rules \( \{ (D(X) \leftarrow C_1(X)) ; (D(X) \leftarrow C_2(X)) \} \). Notice that when a disjunction occurs on the r.h.s. of a subclass axiom, it becomes a disjunction in the head of the corresponding rule, and this cannot be represented in DeLP.

Universal restrictions: In a DL, the universal quantifier can only be used in restrictions
Consider the DL knowledge base (expressions of the form $\forall P.C$, where $P$ must be a single primitive property but $C$ can be a compound expression). So when a universal restriction occurs on the r.h.s. of a subclass axiom ($C \subseteq \forall P.D$), it is expressed as a DeLP rule “$D(Y) \prec C(X) \land P(X,Y)$”. When a universal restriction occurs on the l.h.s. of a subclass axiom (as in $\forall P.C \subseteq D$), it is equivalent to the rule “$C(Y) \prec P(X,Y) \prec D(Y)$” which is transformed into the set of rules \{(D(Y) \prec P(X,Y)); (D(Y) \prec C(Y))\}.

**Existential restrictions:** In a DL, the existential quantifier is used in an expression of the form $\exists P.C$, where $P$ must be a single primitive property, but $C$ may be a compound expression. When an existential restriction occurs on the l.h.s. of a subclass axiom (as in $\exists P.C \subseteq D$), it is expressed as a conjunction in the body of a DeLP rule “$(D(X) \prec P(X,Y)) \land C(Y)$”. When an existential restriction occurs on the r.h.s. of a subclass axiom, it should be expressed as a conjunction in the head of the corresponding rule, with a variable that is existentially quantified. This cannot be represented in DeLP.

**4.3 A Recursive Mapping from DL to DeLP**

In [13], Grosof et al. present a mapping from DL to a subset of Logic Programming. In this section, we will present an adaptation of such mapping for translating DL KBs into DeLP programs.

In the previous sections, we have defined all the cases regarding the translation of DL sentences and axioms into DeLP. Using those definitions as guidelines and assuming that every DL sentence is normalized w.r.t. negation, every DL axiom is mapped into one or more DeLP rules.

**Example 2** Consider the DL knowledge base KB shown in Example 1, the DeLP $\mathcal{P}$ in Figure 2 is obtained by applying the mapping $T$ to KB. Rules are numbered in Roman and each rule corresponds to the equivalent rule numbered in Arabic in Figure 1. (e.g., $T((3)) = (iii)$). Moreover when one rule from Example 1 generates more than one rule in $\mathcal{P}$ according to $T$, the resulting rules are superscripted to show their origin (e.g., $T((10)) = (\{x\}, \{x', x''\})$).

For the sake of example, rule (6) in Figure 1 expressing that every penguin which was operated by a genetic surgeon is a genetically altered penguin is now mapped into rule (vi) in Figure 2:

$$\text{geneticallyAlteredPenguin}(X) \prec \text{penguin}(X),$$
$$\text{isOperatedBy}(X, Y),$$
$$\text{geneticSurgeon}(Y)$$

which now expresses that every penguin which was operated by a genetic surgeon is usually a genetically altered penguin.

Moreover, rule (10) in Figure 1 saying that the set of genetic surgeons is exactly the intersection of the set of geneticists and the set of surgeons is
now expressed as the three rules:

\[
\begin{align*}
(x) & \quad \text{geneticSurgeon}(X) \rightarrow \text{geneticist}(X), \text{surgeon}(X); \\
(x') & \quad \text{geneticist}(X) \rightarrow \text{geneticSurgeon}(X); \\
(x'') & \quad \text{surgeon}(X) \rightarrow \text{geneticSurgeon}(X)
\end{align*}
\]

expressing that (x) an individual is usually a genetic surgeon every time she is both a geneticist and a surgeon, (x') an individual is usually a geneticist if she is a genetic surgeon, and (x'') an individual is usually a surgeon when she is a genetic surgeon.

Set \(\Delta\) of defeasible rules:

- (i) \(\text{animal}(X) \rightarrow \text{bird}(X)\);
- (ii) \(\text{fly}(X) \rightarrow \text{bird}(X)\);
- (iii) \(\text{bird}(X) \rightarrow \text{eagle}(X)\);
- (iv) \(\text{bird}(X) \rightarrow \text{penguin}(X)\);
- (v) \(\sim \text{fly}(X) \rightarrow \text{penguin}(X)\);
- (vi) \(\text{geneticallyAlteredPenguin}(X) \rightarrow \text{penguin}(X), \text{isOperatedBy}(X,Y), \text{geneticSurgeon}(Y)\);
- (vii) \(\text{fly}(X) \rightarrow \text{geneticallyAlteredPenguin}(X)\);
- (viii) \(\sim \text{fly}(X) \rightarrow \text{eagle}(X), \text{hasBrokenWing}(X)\);
- (ix) \(\text{isOperate}(X,Y) \rightarrow \text{isOperatedBy}(Y,X)\);
- (ix') \(\text{isOperatedBy}(X,Y) \rightarrow \text{operates}(Y,X)\);
- (x) \(\text{geneticSurgeon}(X) \rightarrow \text{geneticist}(X), \text{surgeon}(X)\);
- (x') \(\text{geneticist}(X) \rightarrow \text{geneticSurgeon}(X)\);
- (x'') \(\text{surgeon}(X) \rightarrow \text{geneticSurgeon}(X)\);

Set \(\Pi\) of facts:

- (xi) \(\text{penguin}(\text{opus})\);
- (xii) \(\text{eagle}(\text{avenger})\);
- (xiii) \(\text{hasBrokenWing}(\text{avenger})\);
- (xiv) \(\text{geneticist}(<\text{frankenstein})\);
- (xv) \(\text{surgeon}(\text{frankenstein})\);
- (xvi) \(\text{operates}(\text{frankenstein}, \text{opus})\)

Figure 2. DeLP knowledge base \(\mathcal{P} = (\Pi, \Delta)\) obtained from \(KB = (T, A)\) via \(T\)

5 An Approach to Handling Inconsistencies in Ontology Definitions based on DeLP

It is known that ontologies expressed in ontology languages such as OWL-DL can be expressed as equivalent DL ontologies. Although there exist implementations of DL reasoners (e.g., RACER [14]), they are incapable of dealing with inconsistent ontologies. As explained above, our proposal consists of transforming an ontology expressed in a DL into a DeLP program. Thus, inconsistencies arising from inconsistent ontology definitions will be handled by the DeLP engine by performing a dialectical analysis in order to determine which conclusions arising from the derived DeLP program (and indirectly from the original ontology) are warranted. In this section, we will address the issues of reasoning about instances provided an inconsistent ontology definition, reasoning about the class structure of an inconsistent ontology definition provided no instance information is given, and finally will discuss a possible architecture for using our approach in the context of the Semantic Web.

5.1 Reasoning about Instances

As explained in Section 1, our proposal consists of transforming an ontology \(O_{DL} = (T, A)\) into a DeLP program \(\mathcal{P} = (\Pi, \Delta)\) where axioms (i.e., the TBox \(T)\) in \(O_{DL}\) will correspond to a set \(\Delta\) of defeasible rules in \(\mathcal{P}\) while information about individuals in \(O_{DL}\) (i.e., the ABox \(A\)) will correspond to the set \(\Pi\) of facts in \(\mathcal{P}\).

As the set \(\Pi\) comes from the transformation of the ABox \(A\), it is solely composed of facts. For the sake of simplicity we will assume that \(\Pi\) is consistent as required for the DeLP framework (that is, the set \(\Phi\) is consistent if there is neither a pair of facts \(C(a)\) and \(\sim C(a)\) nor \(R(a, b)\) and \(\sim R(a, b)\) where \(C\) is a concept name, \(R\) is a property name, and \(a\) and \(b\) are individual constants). Clearly, in case \(\Pi\) is inconsistent, the pair of conflicting literals can be easily detected and removed.

When the original DL ontology \(O_{DL}\) is consistent, the resulting DeLP program \(\mathcal{P}\) is also consistent. In the case that \(O_{DL}\) is inconsistent, this situation is reflected by the fact that contradicting facts can be entailed by \(O_{DL}\). When considering the translated ontology into \(\mathcal{P} = (\Pi, \Delta)\), the situation of \(O_{DL}\) being inconsistent is reflected into an inconsistent \(\Pi \cup \Delta\). This situation will lead to the derivation of conflicting literals as shown in the next example.

Example 3 Consider the DL ontology \(KB = (T, A)\) presented in Example 1. Notice that in
In this case contradictory conclusions are entailed. For example, $KB \models \neg \text{fly}(\text{avenger})$ and that $KB \models \text{fly}(\text{opris})$ are entailed. The same happens with $\text{fly}(\text{opris})$ and $\neg \text{fly}(\text{opris})$. Considering now the DeLP program $P$ presented in Example 2 and obtained from $KB$, this situation is reflected by the existence of arguments $\langle A_1, \text{fly}(\text{avenger}) \rangle$ and $\langle A_2, \neg \text{fly}(\text{avenger}) \rangle$ as well as $\langle B_1, \text{fly}(\text{opris}) \rangle$ and $\langle B_2, \neg \text{fly}(\text{opris}) \rangle$ (see Example 4 for details).

As explained in Section 3, given a query $Q$ in DeLP, consideration of conflicting arguments on behalf and against $Q$ leads to a process known as dialectical argumentation in which defeaters for arguments favoring $Q$ have to be taken into account as well as defeaters for these defeaters and so on. In the case of having an inconsistent DL ontology $O_{DL}$ and given a query $Q$, the resulting DeLP program will be fed into the DeLP engine to carry out such dialectical analysis. The following example depicts the above described situation.

Example 4 Inferences in the DL KB KB, such as $KB \models \text{fly}(\text{opris})$, are modeled in the DeLP program $P$ as $P \models \text{fly}(\text{opris})$. However, as the derived program $P$ is inconsistent, we have that both $P \models \text{fly}(\text{opris})$ and $P \models \neg \text{fly}(\text{opris})$, leading to the construction of conflicting arguments.

Next we will show the arguments arising from $P$ and will characterize their interactions in the dialectical analysis that arises when considering them. There exists an argument $A_1$ supporting the defeasible conclusion that Avenger flies, i.e., $\langle A_1, \text{fly}(\text{avenger}) \rangle$ where:

$$A_1 = \{ (\text{fly}(\text{avenger}) \leftarrow \text{bird}(\text{avenger})) ; \quad (\text{bird}(\text{avenger}) \leftarrow \text{eagle}(\text{avenger})) \}$$

Assuming that the rule comparison establishes that (8) $\succ$ (2), this argument is defeated by an argument $\langle A_2, \neg \text{fly}(\text{avenger}) \rangle$ supporting that Avenger does not fly because he has a broken wing, where:

$$A_2 = \{ \neg \text{fly}(\text{avenger}) \leftarrow \text{eagle}(\text{avenger}), \quad \text{hasBrokenWing}(\text{avenger}) \}$$

Argument $A_2$ has no defeaters, argument $A_1$ is therefore defeated and it is marked as a D-node. The corresponding dialectical tree is depicted in Figure 3.(i).

Likewise there exists an argument $B_1$ supporting the defeasible conclusion that Opus flies, i.e., $\langle B_1, \text{fly}(\text{opris}) \rangle$ where:

$$B_1 = \{ (\text{fly}(\text{opris}) \leftarrow \text{bird}(\text{opris})), \quad (\text{bird}(\text{opris}) \leftarrow \text{penguin}(\text{opris})) \}$$

Another argument $B_2$, $\neg \text{fly}(\text{opris})$ can be derived from $P$, supporting the conclusion that Opus does not fly, with:

$$B_2 = \{ \neg \text{fly}(\text{opris}) \leftarrow \text{penguin}(\text{opris}) \}$$

Argument $B_2$ defeats $B_1$ provided that the rule comparison criterion establishes that $\langle 5 \rangle \succ \langle 2 \rangle$. However, provided that $\langle 7 \rangle \succ \langle 5 \rangle$, argument $B_2$ is defeated by another argument $\langle B_3, \text{fly}(\text{opris}) \rangle$ which restates argument $B_1$, where:

$$B_3 = \{ (\text{fly}(\text{opris}) \leftarrow \text{geneticallyAlteredPenguin}(\text{opris})), \quad (\text{geneticallyAlteredPenguin}(\text{opris}) \leftarrow \text{penguin}(\text{opris})), \quad \text{isOperatedBy}(\text{opris}, \text{frankenstein}), \quad \text{geneticSurgeon}(\text{frankenstein}) \}$$

$$\quad \text{isOperatedBy}(\text{opris}, \text{frankenstein}) \leftarrow \text{operates}(\text{frankenstein}, \text{opris}) \}$$

$$\quad \text{geneticist}(\text{frankenstein}), \quad \text{surgeon}(\text{frankenstein}) \}$$

Hence the associated dialectical tree for $\text{fly}(\text{opris})$ has three nodes, with the root labelled as U-node (see Figure 3.(ii)). The original argument for $\text{fly}(\text{opris})$ is therefore warranted.

There exist two more arguments $\langle C_1, \text{animal}(\text{avenger}) \rangle$ and $\langle D_1, \text{animal}(\text{opris}) \rangle$ supporting the defeasible conclusions that both Avenger and Opus are animals resp., where:

$$C_1 = \{ (\text{animal}(\text{avenger}) \leftarrow \text{bird}(\text{avenger})), \quad (\text{bird}(\text{avenger}) \leftarrow \text{eagle}(\text{avenger})) \}$$

$$D_1 = \{ (\text{animal}(\text{opris}) \leftarrow \text{bird}(\text{opris})), \quad (\text{bird}(\text{penguin}) \leftarrow \text{penguin}(\text{opris})) \}$$

These two arguments have no defeaters, they are therefore warranted and the resulting dialectical trees will have a unique node, as depicted in Figure 3.(iii–iv).
Consider again the DL knowledge base \( KB \) presented in Example 1. Transforming the Abox set \( A \) into \( AnsProlog \) results in the program \( P_{LP} \) presented in Figure 4. Every rule equivalent to the respective rule enumerated with lowercase Romans in Figure 1 is enumerated in uppercase Romans.

Example 5 Consider again the DL knowledge base \( KB \) presented in Example 1. Transforming the Abox set \( A \) into \( AnsProlog \) results in the program \( P_{LP} \) presented in Figure 4. Every rule equivalent to the respective rule enumerated with lowercase Romans in Figure 1 is enumerated in uppercase Romans.

5.3 An Architecture for Handling Inconsistent Ontologies in the Web

In this section we will present a possible architecture based on a mediator agent which integrates a web browser with a web form for interaction with a human user. The web browser will ultimately access a remote database stored in the web whose data is defined according to some ontology definitions that might be inconsistent. Our proposal for inconsistent ontology management therefore consists in proposing a web service to which a web browser can connect on behalf of a human user who wants to query a certain database located somewhere in the web. The architecture for the approach is depicted in Figure 5.

We will assume that the web browser is able to query a remote database \( Db \) in the web where the information contained in its data records must be interpreted according to an ontology definition \( O_{Out} \) also accessible in the web. Incidentally we will also assume the ontology definition \( O_{Out} \) will be stored in an ontology server.

The proposed system works as follows. The user issues through the web browser a query \( Q \) w.r.t. database \( Db \) and ontology \( O_{Out} \). This query is processed by the query solver who asks the AnsProlog reasoner if \( O_{Out} \) is consistent which is retrieved by the OWL-DL to AnsProlog translator from the ontology server. If the ontology \( O_{Out} \) is inconsistent, it is translated to a DeLP program \( P = (\Pi, \Delta) \) along with the records from database \( Db \) by the OWL-DL to DL and DL to DeLP translators. Using \( P \), the DeLP engine performs a dialectical analysis to determine the epistemic status \( A \) of \( Q \) w.r.t. to \( P \). Finally the epistemically consistent part of \( Q \) is retrieved by the OWL-DL to AnsProlog translator.
temic status of $Q$ is returned as answer $A$ which will be displayed in the web browser.

In order to perform the dialectical process of $Q$ w.r.t. $P$, we will also assume that there exists a human expert who provides the comparison criterion $\succ$ for performing rule comparison into the DeLP engine.

![Diagram](image.png)

**Figure 5. A possible architecture for handling inconsistent ontology definitions in DeLP**

## 6 Discussion

Given a DL KB, our current approach does not allow to obtain an equivalent DeLP program. Moreover, given a DL sentence, only defeasible rules are generated. Next we discuss on the soundness and completeness of our approach as well as possible extensions for dealing with both strict and defeasible rules when translating a DL KB into DeLP.

In a DL setting, a Tbox sentence of the form $C \sqsubseteq D$ is equivalent to a FOL sentence of the form $(\forall x)(C(x) \rightarrow D(x))$ [1]. Therefore, from the former FOL sentence and an Abox sentence $C(a)$, the conclusions $D(a)$ can be reached. Moreover, from $\neg D(a)$, $\neg C(a)$ can be obtained too.

In contrast to DL, in our approach a DL sentence $C \sqsubseteq D$ is translated into DeLP as a defeasible rule $D(X) \leftarrow C(X)$. As the notion of defeasible derivation in DeLP corresponds to the usual query-driven SLD derivation used in logic programming, performed by backward chaining on both strict and defeasible rules, a fact $C(a)$ does permit the derivation of $D(a)$ but $\neg D(a)$ does not permit deriving $\neg C(a)$. Based on these observations, in presence of a consistent DL knowledge base our transformation is sound (i.e., warranted DeLP arguments are valid DL inferences) but not complete (i.e., some valid DL inferences are not derivable into DeLP). Moreover, notice that in the case the original DL ontology is consistent, as the DeLP program obtained by our method is also consistent, all of the inferences obtained are going to be warranted arguments [4].

Although our current approach only deals with the generation of defeasible rules, generation of both strict and defeasible rules during the translation would be a desirable feature. A possible solution to this problem consists of partitioning the DL KB into a set of sentences to be translated as strict rules and a set of sentences to be translated as defeasible rules. Then when receiving a DL KB $\mathcal{KB} = (T, A)$, $\mathcal{KB}$ is partitioned into $\mathcal{KB} = (T_S \cup T_D, A)$ such that $T_S$ ($T_D$) stands for DL sentences to be strict (defeasible, resp.) rules, $T = T_S \cup T_D$, and $T_S \cap T_D = \emptyset$. The DeLP program $\mathcal{P}$ obtained from $T$ is now going...
to be $P = (T(T_S) \cup T(A), T(T_D))$. Notice that as DeLP requires that strict knowledge to be non-contradictory, consistency in the set $T(T_S) \cup T(A)$ must be enforced by the knowledge engineer who is making the partitioning.

7 Related Work

RACER [14] implements a TBox and ABox reasoner for the logic $SHIQ$, it was also the first full-fledged ABox description logic system for a very expressive logic and is based on optimized sound and complete algorithms. In constrast to our proposal, it is not able to deal with inconsistent ontology definitions.

Grosos et al. [13] show how to interoperate, semantically and inferentially, between the leading Semantic Web approaches to rules (RuleML Logic Programs) and ontologies (OWL/DAML+OIL Description Logic) via analyzing their expressive intersection. To do so, we define a new intermediate knowledge representation (KR) contained within this intersection: Description Logic Programs (DLP), and the closely related Description Horn Logic (DHL) which is an expressive fragment of first-order logic (FOL). They show how to perform DLP-fusion: the bidirectional translation of premises and inferences (including typical kinds of queries) from the DLP fragment of DL to LP, and vice versa from the DLP fragment of LP to DL. Part of our article is based on Grosos et al. work as we found the algorithm for translating DL ontologies into DeLP on their work. However, as Grosos et al. work uses standard Prolog rules, they are not able to deal with inconsistent DL knowledge bases as our proposal does.

In [15], Heymans and Vermier extend the description logic $SHOQ(D)$ with a preference order on the axioms. With this strict partial order certain axioms can be overruled, if defeated with more preferred ones. They also impose a preferred model semantics, thus effectively introducing nonmonotonicity into $SHOQ(D)$. They argue that since a description logic can be viewed as an ontology language, or a proper translation of one, they obtain a defeasible ontology language. Similarly to Heymans and Vermier’s work we allow for inferencing from inconsistent ontologies by considering subsets of of the original KB (arguments), comparing them in terms of a rule comparison criterion. However, we choose to translate the original DL KB into DeLP.

In [7], Eiter et al. propose a combination of logic programming under the answer set semantics with the description logics $SHOQ(D)$ and $SHOIN(D)$, which underlie the Web ontology languages OWL Lite and OWL DL, resp. This combination allows for building rules on top of ontologies but also, to a limited extent, building ontologies on top of rules. In constrast to our approach, they keep separated rules and ontologies and handle exceptions by codifying them explicitly in programs under answer set semantics.

8 Conclusions

We have presented a novel argument-based approach for handling inconsistent ontology definitions in the Semantic Web. As discussed in the introduction, given an ontology expressed in a DL we proposed translating it into a DeLP program. Then given a query posed w.r.t. the DL ontology, it will be answered w.r.t. to the DeLP program.

Our approach is not able to deal with axioms that requires the construction of rules with a disjunction in the head which are not currently supported by DeLP, a possible extension to this work would consist in enhancing DeLP with the possibility of handling disjunctions in the head of the rules.

Other issue associated with the approach that needs to be addressed is given by the mapping of equivalence DL axioms into DeLP rules. Currently a DL axiom of the form ‘$C \equiv D$’ generates two rules of the form ‘$C(X) \leftarrow D(X)$’ and ‘$D(X) \leftarrow C(X)$’. This situation could clearly produce loops during the argument construction when solving queries in actual DeLP programs.

One of the goals of the Semantic Web initiative consists of providing methods of entailing information from ontologies that scale to the size of the web. Cecchi et al. [5] have proved that the complexity of the decision problems of determining whether a set of defeasible rules is an argument for a literal under a DeLP program and determining whether there exists an argument for a given literal are P-complete and NP, respectively. Other issue to address involves eliminating the assistance of a human user in order to provide a rule comparison criterion for performing the dialectical process. Part of our current research is focused on these issues.
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