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Experimental and Numerical Study of the Unsteady Wake of a Supercritical Airfoil in a Compressible Flow

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ABSTRACT: Experimental investigations were carried out to study the wake profile of a supercritical airfoil at Mach numbers of 0.4 and 0.6 in a pitching motion. Both static and dynamic tests were conducted in a tri-sonic wind tunnel. Flow field inside the wake was measured by hot wire anemometry at downstream distances of 0.25 and 0.5 times the chord length from trailing edge. All data were taken at mean incidence angle of 3°; the amplitude of oscillation was 3° and the oscillation frequencies were 3 and 6 Hz. Moreover, numerical study was applied for the same airfoil under similar experimental test conditions; finally, wake profiles obtained from both numerical and experimental methods were compared.

KEYWORDS: Supercritical airfoil, Wake, Wind tunnel, Compressible flow, Pitching motion, Hot wire sensor.

INTRODUCTION

It is important to consider the unsteady aerodynamic behavior of airfoils to understand the problems associated with flutter and buffet. The problems are more complicated at high-speed flows due to shock waves and associated separation.

Hot wire anemometry has been used widely in subsonic flow and sometimes in supersonic flow. However, major problems such as wire breakage due to high dynamic pressures, dust particles and vibrations limit the application of hot wires in transonic flows. Signal interpretation is also very complicated in such flows as the output voltage depends on density, velocity, and temperature, each having independently variable sensitivity.

Although much research has been conducted into the study of unsteady flow wake, there is still much to do to investigate the wake profiles by hot wire anemometry in compressible flows. Bodapatti and Lee (1984) studied wake profiles of an airfoil along with an oscillating flap in a transonic flow. They used pressure sensors besides hot wires and compared the results.

Park *et al.* (1990) experimentally studied the wake of a pitching airfoil using hot wire at two Reynolds numbers of 27000 and 47000. The airfoil oscillation amplitude was 7.4°, and the tests were carried out at two reduced frequencies of 0.1 and 0.2 in average angles of attack of 0 – 4°. Reduced frequency is a parameter that defines the degree of unsteadiness and is written as ω , ω is angular velocity, c is airfoil chord and U is freestream velocity. The tests results showed that when the mean incidence was 4°, the airfoil experienced a deep stall. The near wake measurements made it possible to detect and characterize the emergence of unsteady separation; as the reduced frequency increased, the phase angle at which unsteady boundary layer separation occurred was found to be raised.

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Huang and Lin (1995) studied several features of oscillating unsteady flow at a low Reynolds number and angle of attack; they showed that the features had a close relationship with boundary layer behavior on airfoil's surface.

Jung and Park (2005) studied the characteristics of vortices shedding into the wake of an oscillating airfoil under a pitch oscillation at four reduced frequencies of 0.1, 0.2, 0.3, and 0.4, an average angle of attack of 0° , and oscillation amplitude of 3° . To measure the velocity in wake region, they used hot wire anemometry and applied smoke wire visualization method to illustrate the flow. Their observations revealed that the shedding frequency in wake region of an oscillating airfoil was quite different from that of a fixed airfoil at a specified angle of attack; moreover, variation of shedding frequency was diminished as the reduced frequency of oscillation increased.

Zhang and Ligrani (2006) experimentally studied the wake turbulence structure of a cambered airfoil. Hot wire anemometry was used for the measurement of wake turbulence quantities. The results showed that as the level of surface roughness increased, all wake profile quantities broadened significantly and non-dimensional vortex shedding frequencies decreased.

Sadeghi *et al.* (2010) studied the wake characteristics of an oscillating airfoil. The experiments were conducted in a low speed wind tunnel and the velocity field was measured by hot wire anemometry. The airfoil was given a harmonic pitching motion about its half-chord at two reduced frequencies of 0.09 and 0.273. The amplitude of oscillations was 8° and the mean angle of attack was altered from 2.5 to 10° . It was found that the velocity field of the wake is strongly affected by operating condition of airfoil, mean angle of attack, reduced frequency and instantaneous angle of attack. Huge variation in wake profiles was observed at high instantaneous angle of attack when the airfoil experienced significant oscillations beyond static stall which, in turn, was due to dynamic stall.

Zanotti *et al.* (2013) studied the unsteady flow field in the wake of a NACA 23012 pitching airfoil by means of triple hot wire probe measurements. Wind tunnel tests were carried out both in light and deep dynamic stall regimes. In light dynamic stall condition, the wake velocity profiles showed a similar behavior both in upstroke and downstroke motions; the flow on the airfoil upper surface was attached for almost the whole pitching cycle and the airloads showed a small amount of hysteresis. The deep dynamic stall measurements in downstroke showed a large extent of wake and a high value of turbulent kinetic energy due to the passage of strong vortical structures, typical of this dynamic stall regime.

Haghiri *et al.* (2015a; 2015b) and Fallahpour *et al.* (2015) studied boundary layer and transition in transonic unsteady flow. The effects of compressibility, reduced frequency, mean angle of attack, oscillation amplitude and free stream Mach number were investigated. Model of the airfoil besides all oscillation conditions were the same as the present paper.

Boroumand *et al.* (2017) studied the wake characteristics of a pitching supercritical airfoil. The research results could be summarized as: observation of hysteresis and how it is affected by frequency and amplitude variations, observation of increasing turbulence intensity by RMS investigation, and also increasing signal energy by means of PSD diagram for those sensors placed inside the wake and study of correlation between wake's interior and exterior sensors. RMS is Root Mean Square and PSD is Power Spectral Density.

As understood from mentioned researches, most studies that employed hot wire sensors were carried out in low velocities. In this research, wake of a supercritical airfoil is measured in compressible flow by means of hot wire sensors in a transonic wind tunnel for both fixed and oscillating airfoil.

- It is shown that the wake study and its behavior in compressible flow could be achieved by statistical and frequency analysis of sensors voltages when the accurate velocity value is not the issue.
- Calibration of sensor voltage is carried out by in-direct method and velocity profiles are obtained inside the wake.
- Mach contours and velocity profiles are obtained from numerical analysis and compared with experimental results.

EXPERIMENTAL SETUP

The test model was a Sc(2)0410 supercritical airfoil made of 2 cm thick VCN steel with chord and span lengths of 0.2 and 0.6 m, respectively.

The tests were carried out in a high-velocity wind tunnel under the following conditions: a test section of 0.6×0.6 m, oscillation amplitude of 3° , mean angle of attack of 3° , Mach numbers of 0.4 and 0.6, and reduced frequencies of 0.0143 and 0.0286.

Walls of test chamber were porous and capable of up to 6% adjustment. The maximum free stream turbulence level (measured by hot wire sensors, 3 layers of wire screen, and 1 honeycomb) was 0.5%. Schematic of wind tunnel is shown in Fig. 1.

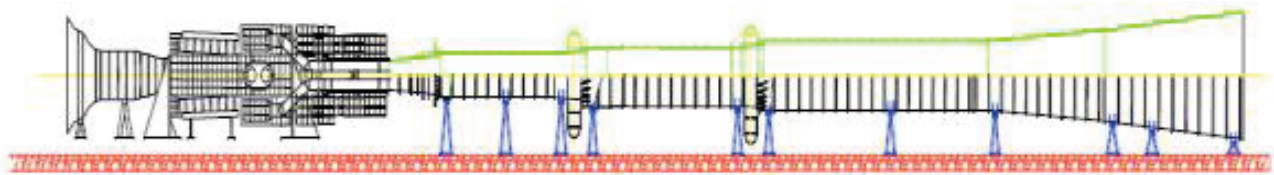


Figure 1. Schematic of wind tunnel.

Figure 2 shows the model mounted in test chamber.

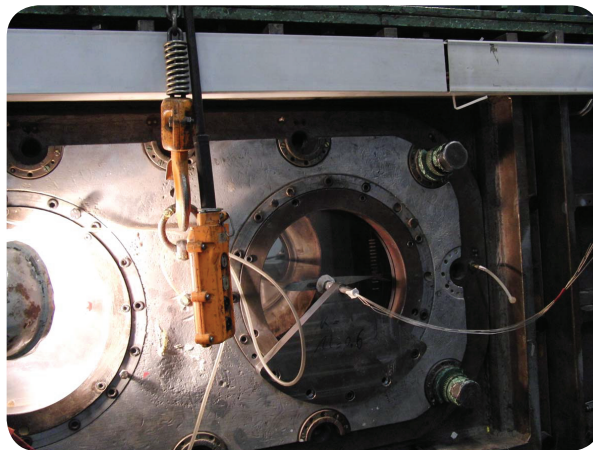


Figure 2. Model in test chamber.

Figure 3 shows the rake including fourteen hot wire sensors. The sensors location detail is listed in Table 1. The sensors, 100 micron in diameter and 0.005 m in length, were made of nickel.

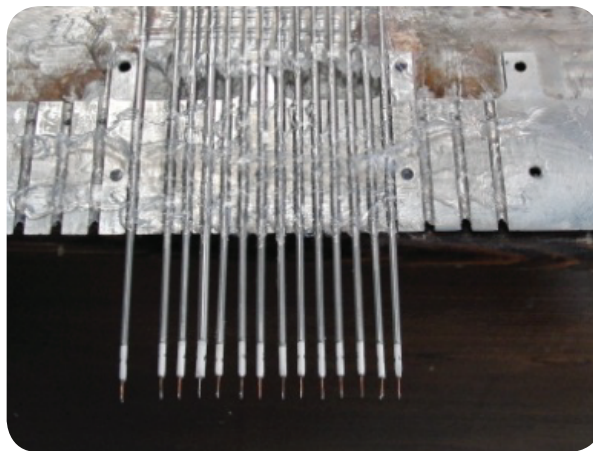


Figure 3. Rake of hot wire sensors.

Table 1. Hot wire sensors location.

Sensor	y/c
S1	-0.245
S2	-0.175
S3	-0.140
S4	-0.105
S5	-0.070
S6	-0.035
S7	0
S8	0.035
S9	0.070
S10	0.105
S11	0.140
S12	0.175
S13	0.210
S14	0.245

Figure 4 shows the airfoil and the rake inside the test chamber.

**Figure 4.** Airfoil, rake and sensors fixed in the test chamber.

In order to record hot wire sensors results, Dantec CTA constant temperature system was applied with overheat of 0.8 and a sampling frequency of 1200 kHz. For each sensor, this frequency was taken to be 5 kHz. CTA is Constant Temperature Anemometry.

Figure 5 shows the block diagram of data acquisition system.

To eliminate the white noise from results, a low-transition filter was used with a cut-off frequency of 300 Hz considering the PSD of curves and the Weiner method. This method is described in detail by Weiner (1949).

Figure 6 shows the energy level curve for a single hot wire sensor to determine the cut-off frequency.

The oscillation mechanism was capable of pitching the model at various amplitudes, mean incidence angles of attack and oscillation frequencies. Since $x/c = 0.4$ was the airfoil aerodynamic center, the pitch rotation axis was fixed at the $x/c = 0.4$ airfoil chord. A hydraulic vibrating system was used to create pitch oscillations that were transmitted to the airfoil through a shaft and extruded from the test chamber window (Fig. 7). The average and instantaneous angle of attack were measured by a linear 0.1° precision potentiometer.

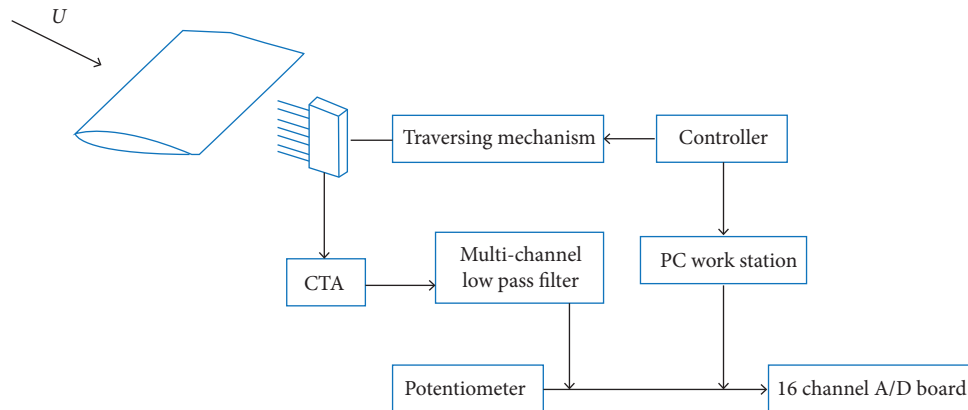


Figure 5. Block diagram of data acquisition system.

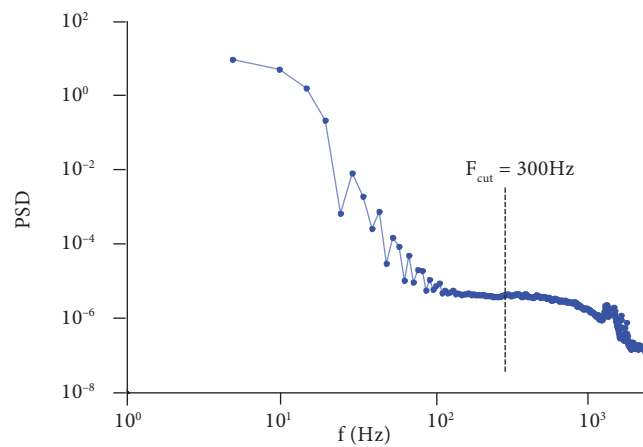


Figure 6. PSD values of a hot wire.



Figure 7. Hydraulic oscillating alpha-mechanism system.

During the tests, Mach number measurements with maximum calculation error of 1% were obtained by means of a pitot-static tube fixed at model's upstream. Pressures were measured using differential pressure sensors with a measurement range of up to 15 psi and maximum error of 0.15% span.

The tests error sources included the flow field (both non-uniformity and turbulence level in the wind tunnel), model installation and α -setting, pressure sensors, airfoil model structure, linear potentiometer, A/D range, hot wires, effects of walls and model blockage. According to Amiri *et al.* (2013), a maximum uncertainty of 4% was calculated.

Wind tunnel was the same for this research and for Amiri's but the NACA0012 airfoil was chosen in Amiri's research because its standard experimental data was available for verification and also to evaluate equipment and wind tunnel precision.

NUMERICAL METHOD

The flow structure around a supercritical airfoil was predicted employing Ansys CFX software and the results were compared with experimental tests.

Turbulence model was Shear Stress Transport (SST $k-\omega$), which was proposed by Menter *et al.* (2003) to combine the precise, powerful $k-\omega$ model (for near wall regions where the Reynolds number is low) with free-stream independent $k-\epsilon$ model (for regions far from the walls where the Reynolds number is high).

Two dimensional simulations were applied as the case study was the main goal and to reduce computational costs. In addition, numerical analysis validation in 2D case is confirmed by some references such as Thiery and Coustols (2006) and Ol *et al.* (2009).

Calculation domain was selected by reviewing some references as Moreau *et al.* (2008) and Ang *et al.* (2004). Dimensions of domain are considered as 4 times of chord length in front, above, and below the leading edge, and 9 times of chord length behind the trailing edge. Moreover, it is sufficiently distanced from airfoil surface to minimize its influence on the solution.

Geometry and computational domain are shown in Fig. 8.

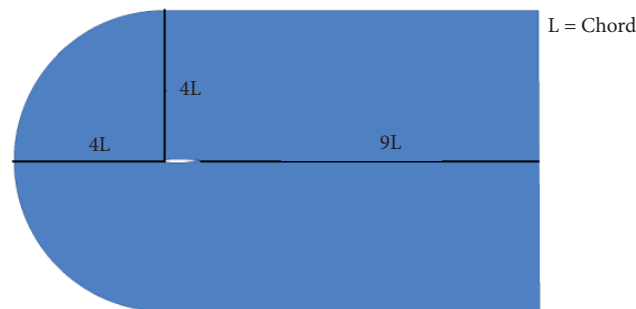


Figure 8. Computational domain.

After grid independency, fine grid was used to predict the flow field around Sc(2)0410 airfoil. Total element of grid is 187220 and total node is 376068.

Figure 9 shows the structured grid used to predict the flow field around the airfoil.

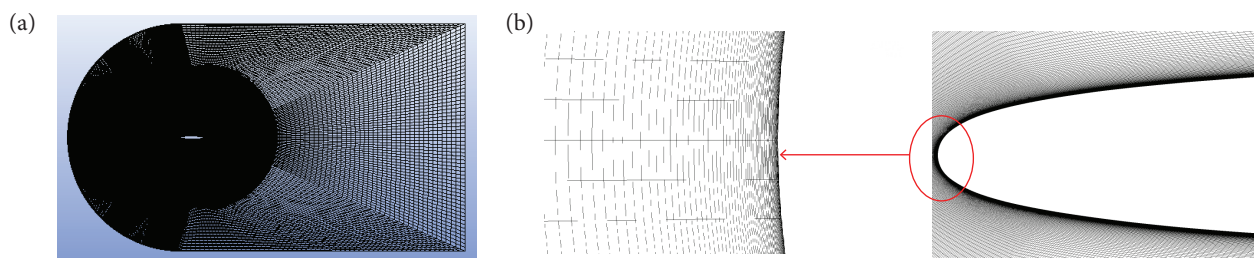


Figure 9. (a) Computational grid; (b) close-up view.

The time step used in unsteady solutions was 0.0005 s. To achieve stable conditions, simulations were carried out for almost 4200 time steps to pass the inlet flow through the entire computational domain for approximately 7 times. The present results are obtained by statistical time averaging of the last 1800 time steps.

The method validity to reach the stable conditions could be carried out by referring to Moghadam *et al.* (2016) and Kiani and Javadi (2016).

Boundary conditions include time-independent uniform-velocity profile for inlets and static pressure for outlets. The airfoil surface is assumed to be non-slip and the reference pressure is considered as zero.

GOVERNING EQUATIONS

Governing equations for this problem are conservation of mass, momentum, and energy for the case of unsteady compressible flow as follows:

Continuity (Eq. 1):

$$\partial \rho / \partial t + \partial / \partial x (\rho u) + \partial / \partial y (\rho v) = 0 \quad (1)$$

x Momentum (Eq. 2):

$$\partial / \partial t (\rho u) + \partial / \partial x (\rho u^2 + p - \tau_{xx}) + \partial / \partial y (\rho uv - \tau_{yx}) = 0 \quad (2)$$

y Momentum (Eq. 3):

$$\partial / \partial t (\rho v) + \partial / \partial x (\rho uv - \tau_{xy}) + \partial / \partial y (\rho v^2 + p - \tau_{yy}) = 0 \quad (3)$$

Energy (Eq. 4):

$$\partial / \partial t (Et) + \partial / \partial x [(Et + p)u + qx - u\tau_{xx} - v\tau_{xy}] + \partial / \partial y [(Et + p)v + qy - u\tau_{yx} - v\tau_{yy}] = 0 \quad (4)$$

where: E_t is the sum of kinetic and internal energy.

The shear stress (τ_{xy}) and normal stress components (τ_{xx} and τ_{yy}) can be expressed in terms of velocity gradients as follows:

Shear stress (Eq. 5):

$$\tau_{xy} = \tau_{yx} = \mu (\partial u / \partial y + \partial v / \partial x) \quad (5)$$

X-normal stress (Eq. 6):

$$\lambda (\nabla \cdot V) + 2\mu \partial u / \partial x \quad (6)$$

Y-normal stress (Eq. 7):

$$\lambda (\nabla \cdot V) + 2\mu \partial v / \partial y \quad (7)$$

where: μ is the dynamic viscosity of the fluid. These equations are described in Detail by Drazin and Riley (2006).

Several researches, as those carried out by Mojiri and Datta (2009) and Eleni *et al.* (2012), showed that by proper grid generation in boundary layer and Y^+ close to 1, SST k- ω model will give more precise results. SST model was applied here since capturing the wake was the main goal of the research in which vortex observation, flow behavior close to walls, and boundary layer analysis were to be focused on.

In SST turbulence model, K- ω and K- ϵ are both multiplied by a blending function and then summed. Blending function is designed so that it equals to 1 in near-wall regions (which activates K- ω model in that region) and equals to zero in regions far from the wall (which activates K- ϵ model in that region). This turbulence model is common for airfoil flow analysis and behaves properly in flow separation and in reverse pressure gradient.

Equations applied for such turbulence model are as follows (Eq. 8):

$$\begin{aligned} \frac{\partial(\rho k)}{\partial t} + \frac{\partial(\rho U_i k)}{\partial x_i} &= \tilde{P}_k - \beta^* \rho k \omega + \frac{\partial}{\partial x_i} \left[(\mu + \sigma_k \mu_t) \frac{\partial k}{\partial x_i} \right] \\ \frac{\partial(\rho \omega)}{\partial t} + \frac{\partial(\rho U_i \omega)}{\partial x_i} &= \alpha \rho S^2 - \beta \rho \omega^2 + \frac{\partial}{\partial x_i} \left[(\mu + \sigma_\omega \mu_t) \frac{\partial \omega}{\partial x_i} \right] + 2(1 - F_1) \rho \sigma_{\omega 2} \frac{1}{\omega} \frac{\partial k}{\partial x_i} \frac{\partial \omega}{\partial x_i} \end{aligned} \quad (8)$$

where the F_1 blending function is (Eq. 9):

$$\begin{aligned} F_1 &= \tanh \left\{ \left\{ \min \left[\max \left(\frac{\sqrt{k}}{\beta^* \omega y}, \frac{500 \nu}{y^2 \omega} \right), \frac{4 \rho \sigma_{\omega 2} k}{CD_{k\omega} y^2} \right] \right\}^4 \right\} \\ CD_{k\omega} &= \max \left(2 \rho \sigma_{\omega 2} \frac{1}{\omega} \frac{\partial k}{\partial x_i} \frac{\partial \omega}{\partial x_i}, 10^{-10} \right) \end{aligned} \quad (9)$$

where y is the distance from closest wall.

Turbulence viscosity is defined as follows (Eq. 10):

$$\nu_t = \frac{a_1 k}{\max(a_1 \omega, S F_2)} \quad ; \quad \nu_t = \frac{\mu_t}{\rho} \quad (10)$$

where: S is the shear stress value and F_2 is the second blending function that is defined as follows (Eq. 11):

$$F_2 = \tanh \left\{ \left[\max \left(\frac{2\sqrt{k}}{\beta^* \omega y}, \frac{500 \nu}{y^2 \omega} \right) \right]^2 \right\} \quad (11)$$

This method is described in detail by Menter *et al.* (1993,1994).

Figure 10 shows the calculated Y^+ in airfoil wall simulation.



Figure 10. Y^+ calculated on the airfoil wall.

High-resolution second order upwind method was used for numerical solution of partial differential equations where high accuracy was required in the presence of shocks or discontinuities.

The method is described in detail by Barth and Jespersen (1989), Ferziger and Perić (2009) and ANSYS Fluent (2009).

RESULTS

All tests were carried out under static and dynamic conditions both experimentally and numerically. Velocity profiles, Mach contours, statistical and frequency analysis of hot wire outputs were used to identify the wake behavior.

The research results are categorized in two sections: statistical and frequency analysis of hot wire sensors voltages and velocity profiles (derived from calibration).

Before exploring the mentioned parts, it is preferred to show the lift coefficient diagrams in Figs. 11 and 12 for flows with Mach numbers of 0.4 and 0.6, which are sketched to prove the results consistency between numerical analysis and experimental tests, and also to determine the angle of static stall.

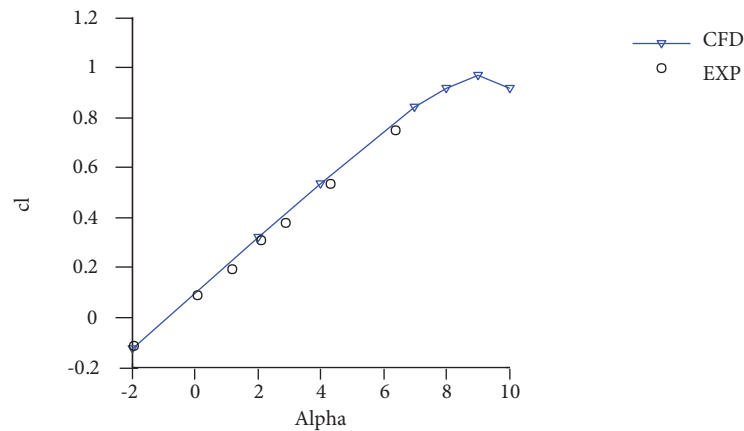


Figure 11. Lift coefficient distribution, Mach = 0.4.

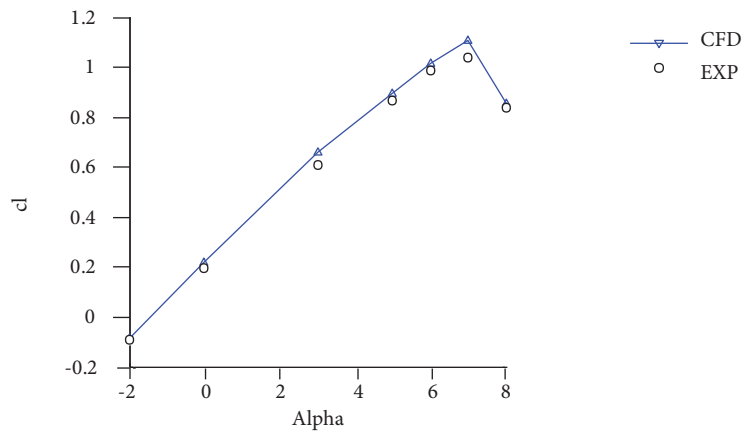


Figure 12. Lift coefficient distribution, Mach = 0.6.

As it is shown in Figs. 5 and 6, the angle of static stall for Mach number of 0.4 is 9° and for Mach number of 0.6 is 7°. Therefore, experimental tests are carried out below stall angle for both Mach numbers of 0.4 and 0.6; a near stall state occurs only in the case of 0.6, oscillation amplitude of 3° and mean angle of attack of 3°.

STATISTICAL AND FREQUENCY ANALYSIS OF HOT WIRE SENSORS VOLTAGES

Results in this section show that the study of wake and its thickness in various cases are possible by statistical and frequency analysis of hot wires output voltages.

Static Part

Figure 13 indicates linear correlation coefficient diagram for hot wire sensors. Correlation coefficient is a value between +1 and -1 calculated so as to represent the linear interdependence of two variables or sets of data. Therefore, in this research, correlation coefficient between two adjacent sensors shows the flow behavior at sensor locations. As it is shown in Fig. 13, the coefficient is maximized for a couple of sensors located outside the wake and decreases when they are not at the same region (i.e., one sensor locates inside the wake region and the other locates outside).

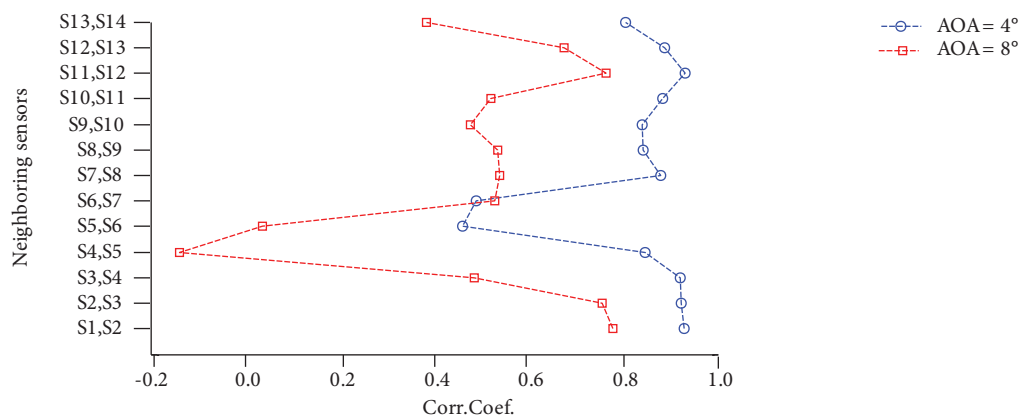


Figure 13. Linear correlation coefficient diagram for hot wire sensors.

For angle of 4° for example, sensor S6 achieves minimum correlation with S7 and S5 since it is located inside the wake at the mentioned angle. This also occurs for sensor S5 at angle of 8° .

As mentioned before, the wake region could be estimated by depicting the Correlation coefficient parameter for adjacent sensors and studying their behavior.

Figure 14 shows the time history of hot wires signals at $AOA = 4^\circ$; qualitative investigation of signals reveals that the wake sensor fluctuations are by far higher than those of other sensors; therefore, the wake location determination becomes possible through a voltage qualitative investigation.

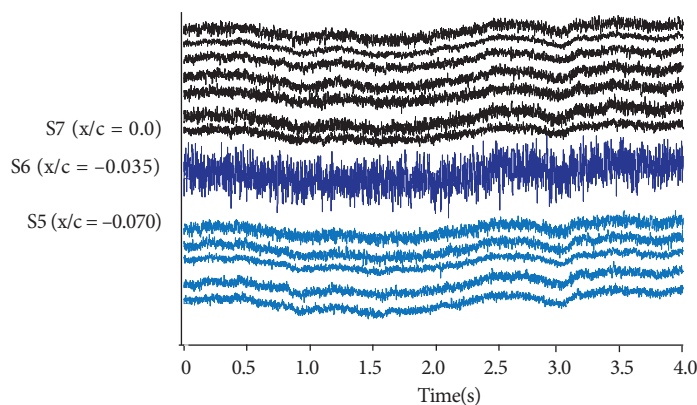


Figure 14. Time history of hot wires output signals at $AOA = 4^\circ$.

As suggested before, entry of one sensor into the wake region could be observed by means of signal analysis of the sensor voltage. Signal energy or PSD is also a significant parameter. Energy level for angles of attack of 3° and 6° are shown in Figs. 15 and 16 for three sensors located at $y/c = 0$, $y/c = -0.035$, and $y/c = -0.07$.

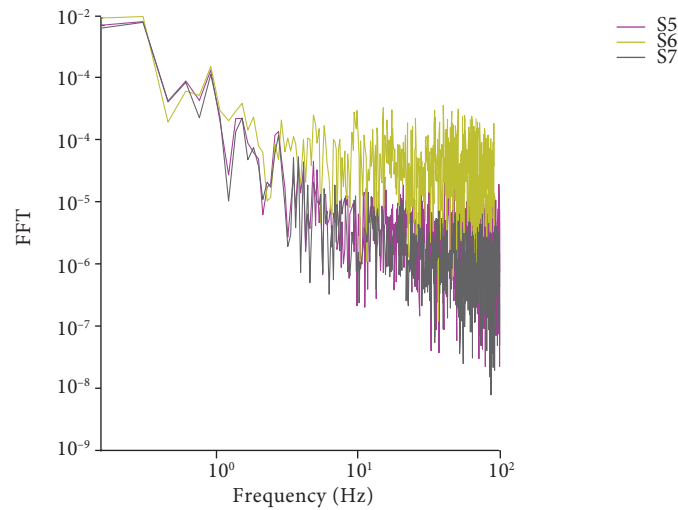


Figure 15. Sensors energy level at angle of attack of 3° .

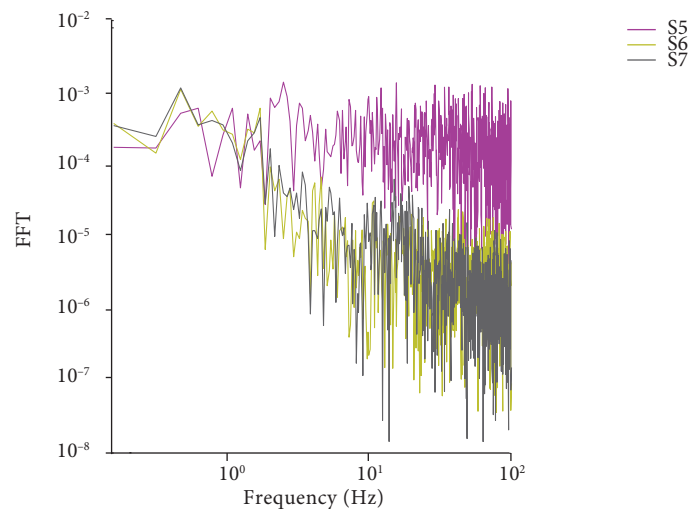


Figure 16. Sensors energy level at angle of attack of 6° .

As observed in Figs. 15 and 16, S6 sensor gains maximum energy level by entering the wake region at angle of 3° , whereas, at angle of 6° , by entry of S5 sensor into the region, it gains the maximum energy level and S6 sensor scores the second place.

Dynamic Part

Focus in this section is on the airfoil wake in a pitch sinusoidal motion. Figure 17 shows the instantaneous voltages of three sensors in $\alpha(t) = 3 + 3 \sin(2\pi t/T - \pi/2)$ pitch oscillation motion at frequency of 3 Hz. Comparing consecutive cycles reveals their repeatability with an appropriate precision; if a complete cycle is considered as a pitch up-pitch down sequence, then every sensor will cover the same pattern through all cycles. Deviations may appear only in very small fluctuations, which are likely related to noise or any other unsteadiness that may instantaneously and irregularly affect the sensors voltages, but not to the flow physics.

Figure 18 shows the RMS variations in a complete cycle. Lines L1, L2, and L3 in a pitch up, are related to states when the wake enters $y/c = 0.0$, minimum voltage level, and when the wake leaves that point, respectively. Lines L4, L5, and L6 show the same states in a pitch down. Related times are printed against each line.

RMS value for each signal increases with an increase in randomness and in amplitude of oscillations around the average value; hence, RMS could be considered equivalent to turbulence intensity in the flow. Variations in Fig. 18 confirm this equivalency; when the sensor enters the wake at L1, RMS value starts increasing and reaches its maximum at point I, then it starts to decrease, getting an extremum at L2, where the voltage is minimum. Afterwards, it starts to increase again, goes up to point II, and finally falls down by getting close to the boundary layer border. Similar behavior is observed in a pitch down.

Figure 19 shows the coefficient of linear correlation between two sensors at $y/c = 0.0$ (inside the wake) and at $y/c = 0.245$ (outside the wake). The coefficient of correlation between S7 and the flow outside the wake does not decrease immediately after the sensor locates inside the wake; rather, it decreases remarkably when it gets close to the minimum voltage zone and finally reaches a value of about -0.9 at L2.

Analysis of results from Figs. 13 to 19 confirms that the study of wake is possible by means of sensor voltage analysis even for oscillating airfoil.

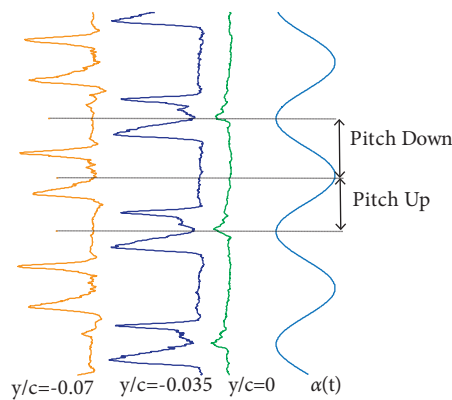


Figure 17. Instantaneous voltages of three sensors, pitch oscillation $\alpha(t) = 3 + 3 \sin(2\pi t/T - \pi/2)$, frequency = 3Hz, Mach = 0.4.

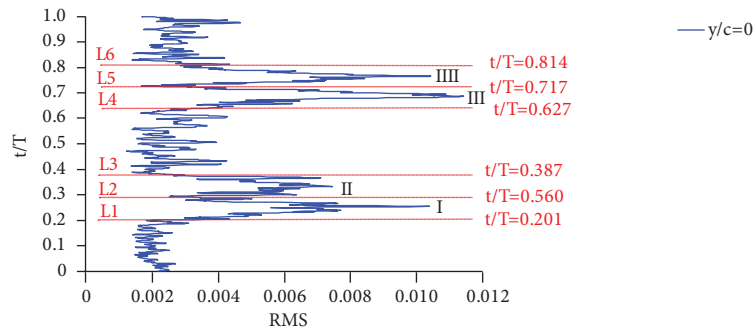


Figure 18. RMS variations in a complete cycle.

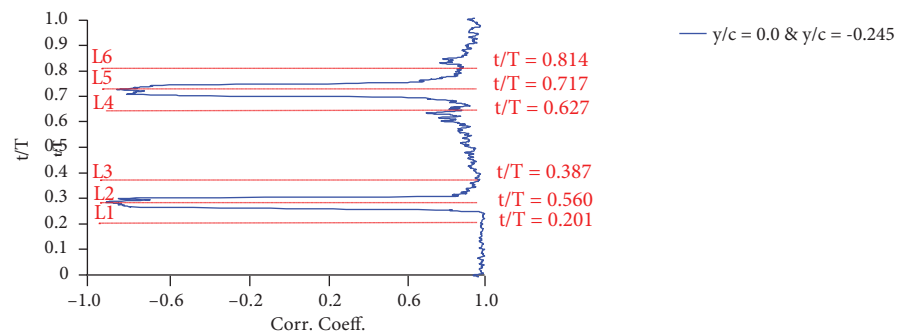


Figure 19. Coefficient of linear correlation between sensors S7 and S14.

VELOCITY PROFILES

Voltage calibration for hot wire sensors was carried out in this research and wake velocity profiles were obtained from hot wire anemometry.

Calibration

According to Motallebi (1994), in high speed flow, due to the compressibility effects, the anemometer is affected not only by changes in flow velocity, but also by density and temperature fluctuations. In other words, for a single normal wire, the output voltage of anemometer is a function of flow velocity, flow density and total temperature (Eq. 12).

$$E = E(U, \rho, T) \quad (12)$$

This equation can be written as (Eq. 13):

$$\text{Log}(E^2 - E_0^2) = S_u \text{Log}(U) + S_\rho \text{Log}(\rho) + S_T \text{Log}(T) + \text{const} \quad (13)$$

If ρ and T are constants (Eq. 14):

$$S_u = \frac{\partial[\text{Log}(E^2 - E_0^2)]}{\partial[\text{Log}(U)]} \quad (14)$$

If U and T are constants (Eq. 15):

$$S_\rho = \frac{\partial[\text{Log}(E^2 - E_0^2)]}{\partial[\text{Log}(\rho)]} \quad (15)$$

If ρ and U are constants (16):

$$S_T = \frac{\partial[\text{Log}(E^2 - E_0^2)]}{\partial[\text{Log}(T)]} \quad (16)$$

Therefore, several tests shall be necessary to calibrate sensor's output and its conversion into velocity. Those tests require to obtain S_u by velocity variation while temperature and density are constants. Also to obtain S_ρ by density variation while temperature and velocity are constants and to obtain S_T by temperature variation while velocity and density are constants.

Generally, experimental calculation of calibration coefficients could be achieved by two methods:

- Direct experimental method
- Indirect or semi-experimental method

In direct method, hot wire is placed in free stream of tunnel and the stagnation pressure is varied while the Mach number and stagnation temperature are kept unchanged. By time averaging, it is then possible to obtain the mean output voltage of the anemometer as a function of mean mass flux.

The slope of a plot of $\ln(E)$ versus $\ln(\rho u)$ will determine $\Delta e_{\rho u}$. The $\Delta e_{\rho u}$ sensitivity coefficient can be determined by a controlled change of gas total temperature while gas density and velocity are kept unchanged. This method is not practiced in conventional wind tunnels, since it requires several tests in special tunnels.

When the possibility of calibrating the hot wire in a controlled flow environment is not feasible in a given test facility, then it is advisable to calibrate the hot wire in wind tunnel by simultaneous variation of density, velocity and temperature.

An indirect calibration method is employed in this research, which was first introduced by Stainback and Nagabushana (1993) and Stainback *et al.* (1983). Applying the mentioned method they calculated, at first, the calibration coefficients by several tests in wind tunnel, and then estimated a statistically optimized equation (Eq. 17):

$$\log(E) = A_1 + A_2 \log(u) + A_3 \log(\rho) + A_4 \log(T_o) + A_5 \log(u) \log(\rho) + A_6 \log(u) \log(T_o) + A_7 \log(\rho) \log(T_o) + A_8 \log(u) \log(\rho) \log(T_o) \quad (17)$$

Equations for sensitivity coefficients are as follows (Eqs. 18, 19, and 20):

$$S_u = A_2 + A_5(\log \rho) + A_6 \log(T_o) + A_8 \log(\rho) \ln(T_o) \quad (18)$$

$$S_\rho = A_3 + A_5 \log(u) + A_7 \log(T_o) + A_8 \log(u) \log(T_o) \quad (19)$$

$$S_{T_o} = A_4 + A_6 \log(u) + A_7 \log(\rho) + A_8 \log(u) \log(\rho) \quad (20)$$

In this research, output voltages for each sensor were obtained for eight values of Mach number during several tests in wind tunnel. Fourteen sensors mounted on a rake were placed in wind tunnel for data sampling in various Mach numbers. Mach number varied from 0.35 to 0.75 and sensors outputs were recorded by sampling frequency of 5 kHz.

Obtaining output voltages, a system of equations comprising eight equations and eight unknowns was configured and solved to give the coefficients A_1 to A_8 . Equations 18 to 20, for sensitivity coefficients, were solved to give S_u , S_ρ , and S_{T_o} , consequently. Applying these coefficients in tests helped to benefit from converting the voltage into velocity.

Static Part

Figures 20 to 22 show the velocity diagrams in wake region for Mach number of 0.4 at downstream distance of 0.25 chord.

A significant velocity decrease in wake region is obvious in diagrams. Location of maximum velocity reduction shifts downward as AOA increases. S7 sensor indicates maximum voltage reduction at angle of 0° , which suggests minimum velocity in turn. Mentioned sensor leaves the wake region as the angle of attack varies from 0° to 3° and S6 sensor indicates the minimum velocity instead. That means the wake tends downward.

S5 sensor also enters the wake region by increasing the angle of attack to 6° , which indicates a large velocity reduction. The wake thickness increases at this angle of attack and both S5 and S6 sensors are placed inside the wake region.

Figures 23 to 25 show the velocity diagrams in wake region for Mach number of 0.6 at downstream distance of 0.25 chord. Velocity reduction is observed in the wake. Like in the previous case, the wake rotates clockwise by increasing the angle of attack. Wake thickness and velocity reduction at Mach number of 0.6 is more than those of flow with Mach number of 0.4. This is obvious by comparing Figs. 22 and 25.

Velocity behavior at $x/c = 0.5$ is almost similar to that of $x/c = 0.25$, as shown in Fig. 26; deviations are the rate and slope of voltage reduction which is higher at $x/c = 0.25$, and the wake thickness which is greater at $x/c = 0.5$. This is a result of wake effect weakening as departing longitudinally from airfoil.

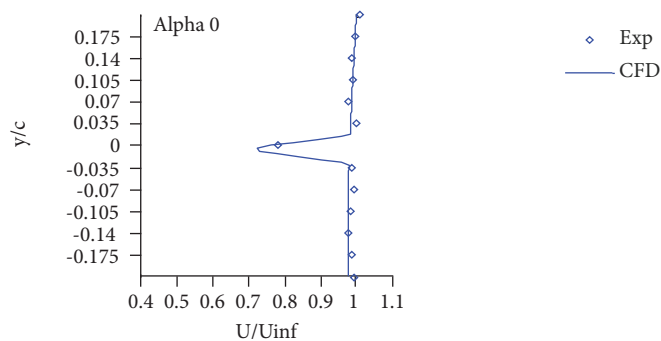


Figure 20. Streamwise velocity profile at $x/c = 0.25$, Mach = 0.4.

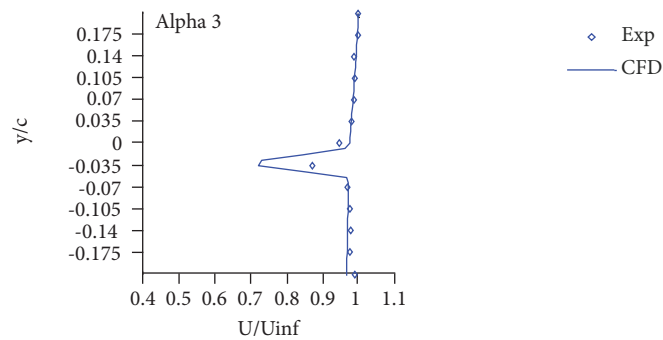


Figure 21. Streamwise velocity profile at $x/c = 0.25$, $Mach = 0.4$.

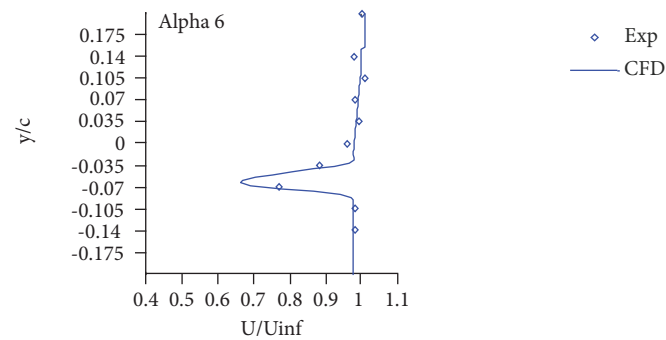


Figure 22. Streamwise velocity profile at $x/c = 0.25$, $Mach = 0.4$.

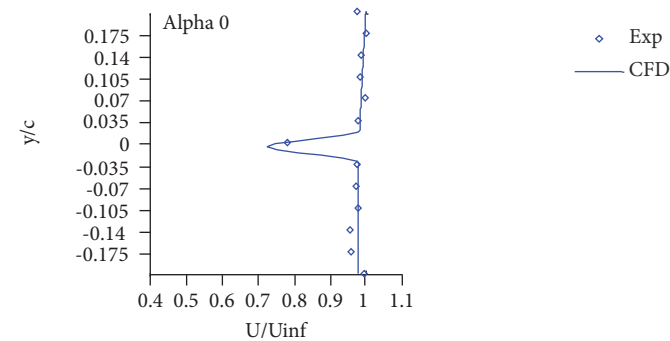


Figure 23. Streamwise velocity profile at $x/c = 0.25$, $Mach = 0.6$.

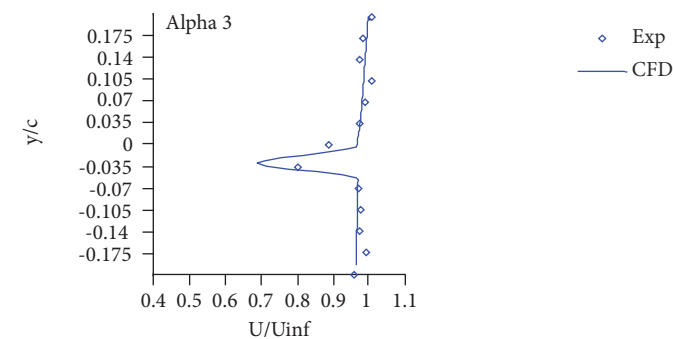


Figure 24. Streamwise velocity profile at $x/c = 0.25$, $Mach = 0.6$.

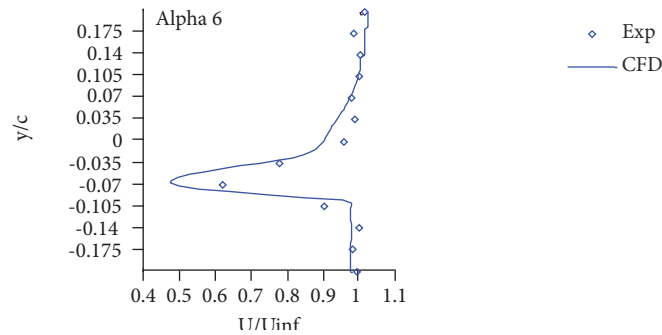


Figure 25. Streamwise velocity profile at $x/c = 0.25$, Mach = 0.6.

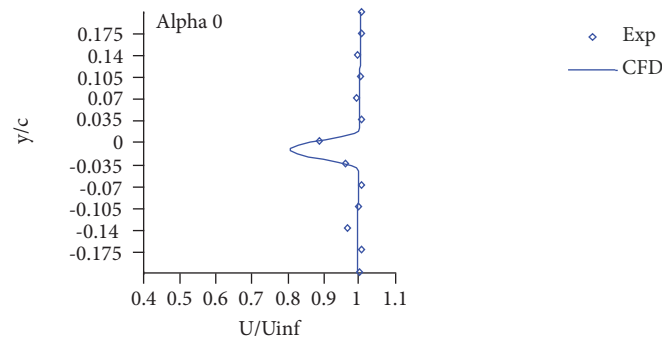


Figure 26. Streamwise velocity profile at $x/c = 0.5$, Mach = 0.4.

As observed from velocity profiles, results obtained from both experimental and numerical analysis are in a good consistence.

Dynamic Part

Figures 27 to 30 show the wake velocity profiles in $\alpha(t) = 3 + 3 \sin(\omega t)$ pitch oscillation. In order to achieve velocity profiles for oscillating airfoil, output signal for each sensor was recorded at each instantaneous angle of attack and averaged for 15 complete oscillating cycles.

At angle of attack of 3° , S6 and S7 sensors are both placed in wake region, while at angle of attack of 6° , S5 sensor indicates velocity reduction from free stream velocity, which implies a notable increase of wake thickness.

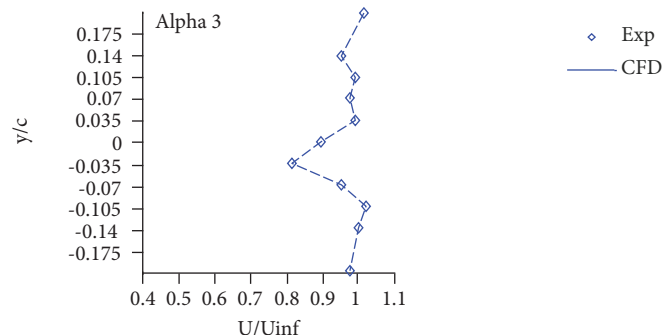


Figure 27. Streamwise velocity profile, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.4.

As observed from velocity profiles, the wake rotates clockwise and tends downward by increasing the angle of attack. At angle of attack of 3° , S6 sensor shows a velocity decrease, while at 6° the wake tends down and S5 sensor shows a velocity decrease instead. Wake thickness also increases due to flow separation at trailing edge and rise of a shock on the airfoil.

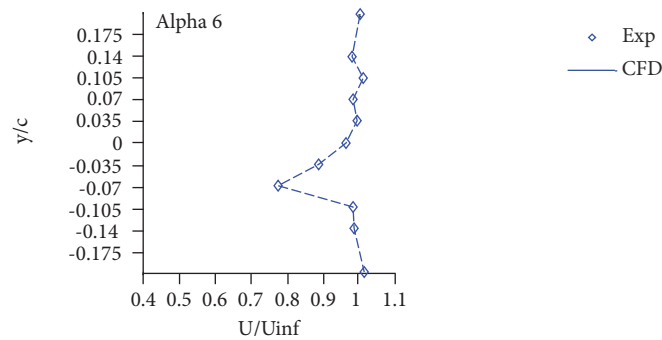


Figure 28. Streamwise velocity profile, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.4.

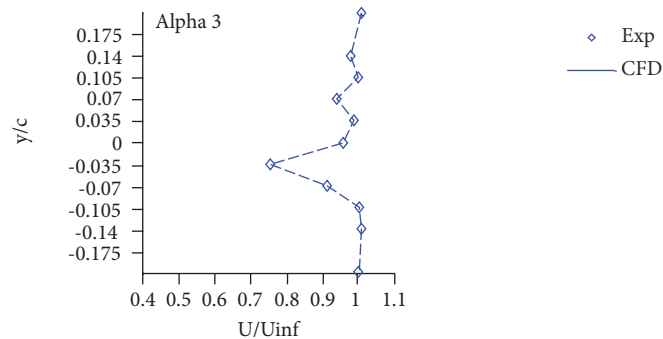


Figure 29. Streamwise velocity profile, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.6.

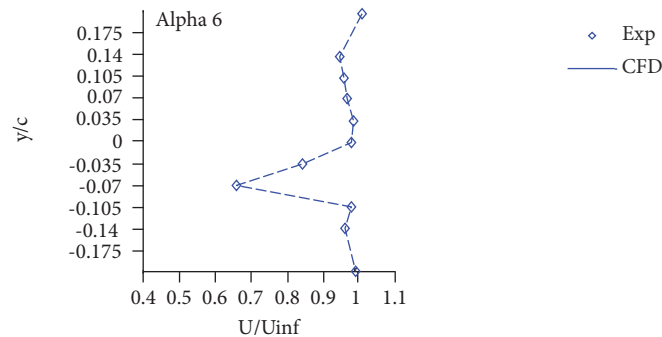


Figure 30. Streamwise velocity profile, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.6.

This could be observed and validated by Mach contours obtained from numerical solution that are shown in Figs. 32 to 35.

Figure 31 shows the pressure coefficient diagram on airfoil surface for angles of 3.8° and 4° in a pitch up motion. The diagram indicates a shock for angles beyond 4° .

A shock occurs on the airfoil for angles above 4° . This is also noticeable by studying the Mach number contours for oscillating airfoil.

As indicated in the diagrams, the vortex created at leading edge moves towards trailing edge by increasing the angle of attack and finally sheds from trailing edge into the wake.

Maximum oscillation of 6° stays far from stall since static stall angle for a flow with Mach number of 0.4 is 9° , as described in lift coefficient diagrams. Although at Mach number of 0.4, separation occurs at trailing edge by increase in oscillation angle, but the airfoil would not experience a shallow stall.

In a flow with Mach number of 0.6, static stall angle is 7° . Oscillating shock occurs on the airfoil in this case, which shows a shallow stall.

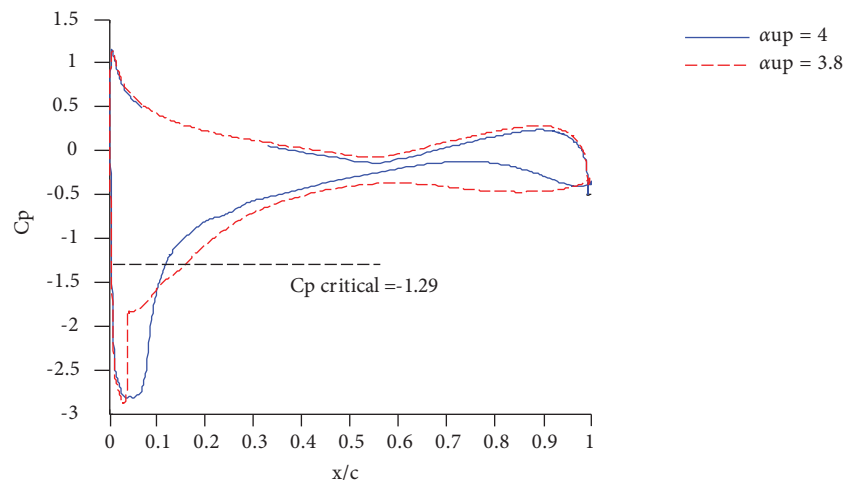


Figure 31. Pressure Coefficient distribution over the airfoil obtained from numerical solution, Mach = 0.6.

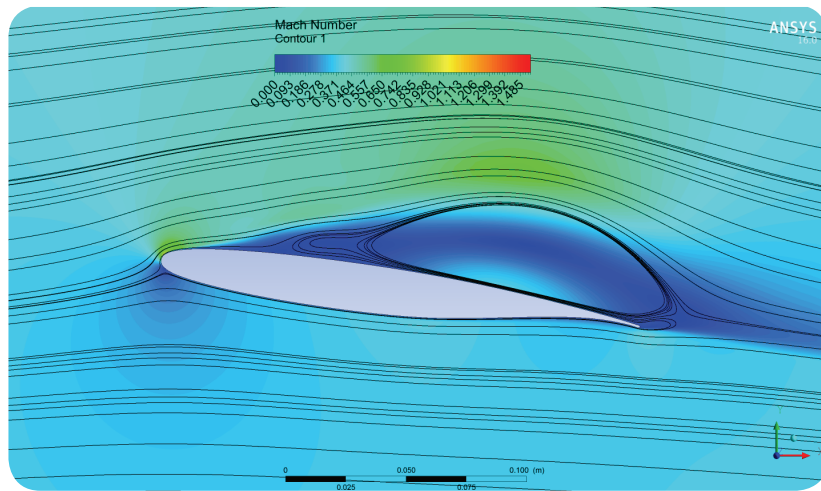


Figure 32. Mach contour, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.4, Alpha = 5° .

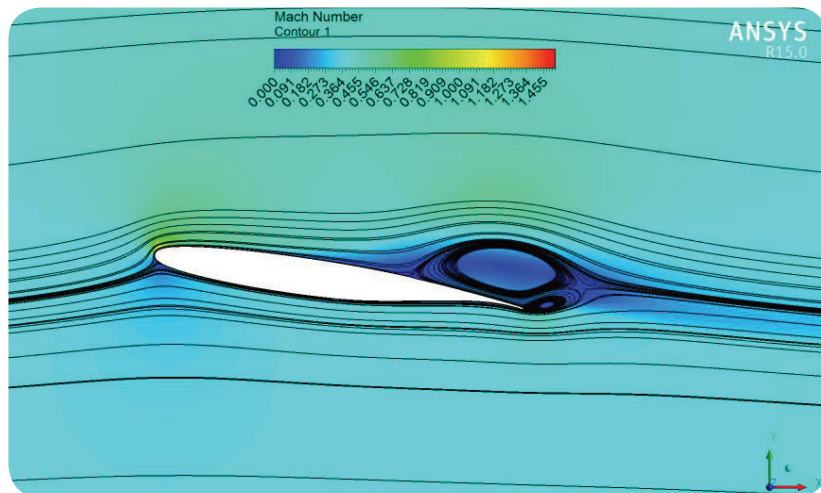


Figure 33. Mach contour, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.4, Alpha = 6°

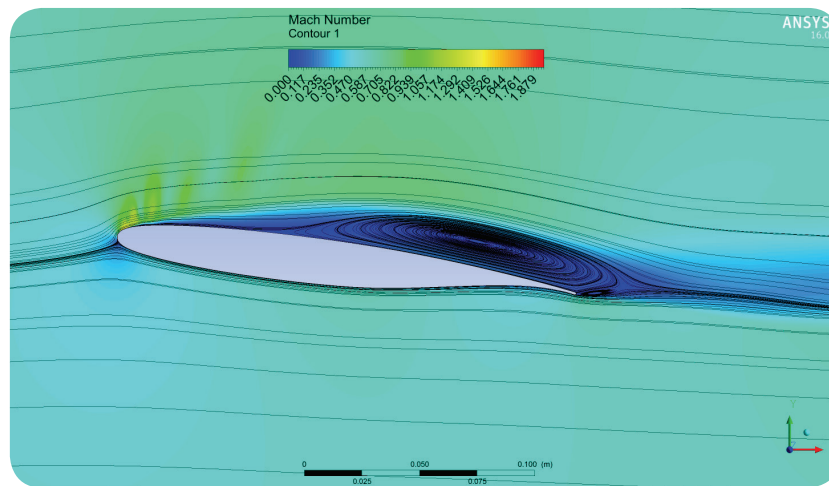


Figure 34. Mach contour, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.6, Alpha = 5°.

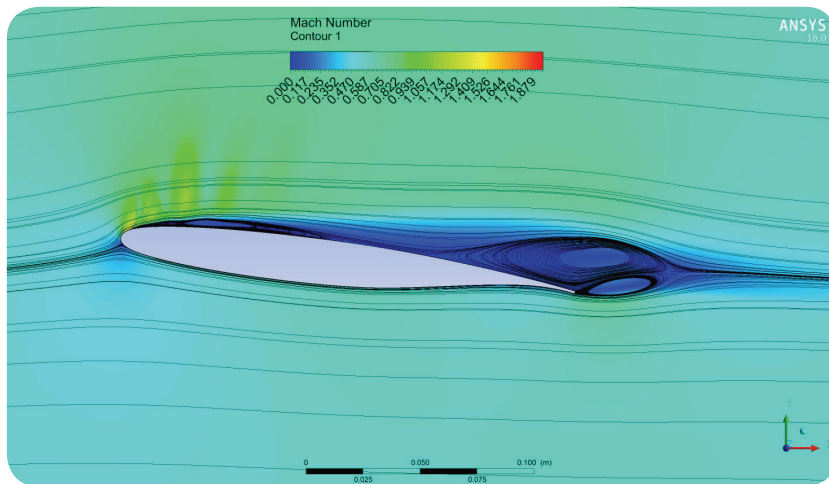


Figure 35. Mach contour, pitch motion $\alpha(t) = 3 + 3 \sin(\omega t)$, frequency = 3 Hz, Mach = 0.6, Alpha = 6°.

Finally, by moving downward and decreasing the angle of attack, the separated flow reattaches to the airfoil surface for both Mach numbers of 0.4 and 0.6.

CONCLUSION

Wake of a supercritical airfoil in a pitching motion was investigated experimentally and numerically in case of compressible flow.

Static stall angle was obtained for Mach numbers of 0.4 and 0.6 by lift coefficient diagram in both experimental and numerical cases. Moreover, results consistency for both cases was indicated by lift coefficient diagram.

By depicting sensors output diagrams like RMS, time history, correlation coefficient and energy level, it was shown that the wake investigation and its behavior in compressible flow could be achieved by frequency and statistical analysis of sensors voltages if the precise velocity value does not matter.

Calibration was carried out despite the troubles in compressible flow and velocity curves were obtained for both fixed and oscillating airfoils.

It was observed that the location of maximum velocity reduction varies and the wake thickens by increasing the angle of attack in unsteady flow because of the shock on airfoil surface and the flow separation at trailing edge.

At high angles of attack, vortex development on trailing edge and formation of shock on the airfoil were illustrated by Mach contours.

Velocity profiles for both fixed and oscillating airfoil were almost consistent for similar angles. A slight deviation of velocity profile in mentioned cases was due to unsteady flow effects.

Comparing the velocity profiles for $x/c = 0.25$ and $x/c = 0.5$ demonstrated that the wake thickens by moving further downstream from trailing edge while the velocity gradient decreases; therefore, the velocity value at $x/c = 0.5$ is higher than the value at $x/c = 0.25$.

AUTHOR'S CONTRIBUTION

Conceptualization, Beheshti B and Mani M; Methodology, Beheshti B and Mani M; Investigation, Beheshti B; Writing – Original Draft, Beheshti B; Writing – Review and Editing, Beheshti B and Mani M; Resources, Beheshti B; Supervision, Mani M.

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