

Journal of Aerospace Technology and Management ISSN: 2175-9146

Departamento de Ciência e Tecnologia Aeroespacial

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Journal of Aerospace Technology and Management, vol. 11, e2119, 2019
Departamento de Ciência e Tecnologia Aeroespacial

DOI: https://doi.org/10.5028/jatm.v11.1003

Available in: https://www.redalyc.org/articulo.oa?id=309457690021



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Integrated Guidance and Control of Multiple Interceptor Missiles Based on Improved Distributed Cooperative Control Strategy

Xiang Liu*1, Xiaogeng Liang1

How to cite

Liu X (b) https://orcid.org/0000-0003-4456-2091 Liang X (b) https://orcid.org/0000-0002-7153-6668 Liu X; Liang X (2019) Integrated Guidance and Control of Multiple Interceptor Missiles Based on Improved Distributed Cooperative Control Strategy. J Aerosp Technol Manag, 11: e2119. https://doi.org/10.5028/jatm.v11.1003

ABSTRACT: In this study, an improved cooperative integrated guidance and control (IGC) design method is proposed based on distributed networks to address the guidance and control problem of multiple interceptor missiles. An IGC model for a leading interceptor is constructed based on the relative kinematic relations between missiles and a target and the kinematic equations of the missiles in a pitch channel. The unknown disturbances of the model are estimated using a finite-time disturbance observer (FTDO). Then, the control algorithm for the leading interceptor is designed according to the disturbance estimation and nonsingular fast dynamic surface sliding mode control (SMC). To enhance the rate of convergence of the cooperative control commands for the interceptors, an improved cooperative control strategy is proposed based on the leader-follower distributed network. Consequently, the two velocity components of the interceptor in the pitch channel can be obtained, which are subsequently converted to the total velocity and flight path angle commands of the interceptor using kinematic relations. The control algorithm for the following interceptor is similarly designed using an FTDO and dynamic surface SMC. The effectiveness of the improved distributed cooperative control strategy for multiple interceptors is validated through simulations.

KEYWORDS: Integrated guidance and control, Finite-time disturbance observer (FTDO), Nonsingular fast dynamic surface sliding mode, Distributed network, Improved cooperative control strategy

INTRODUCTION

With the advancement of anti-missile technology, cooperative multi-missile attack and defense is attracting increasing attention owing to its unique strengths. As a result, the development of cooperative multi-missile guidance and control technology, which is a key element for ensuring the attack and defense performance of a weapon system, has gained momentum. Through coordination between missiles, cooperative engagement integrates multiple interceptor missiles as a united combat group that is information-sharing, function-complementary, and tactics-cooperative. Using the group advantage, a multi-missile system can execute a multi-layer all-around attack on an enemy's defense system or a target with overall-promoted penetration capabilities and carries out tasks that are difficult for a single interceptor missile to perform. Therefore, it is of practical significance to study the cooperative guidance and control of multiple interceptors (Zhao and Yang 2017; Daughtery and Qu 2014).

With respect to the cooperative guidance and control of multi-interceptors, Jeon *et al.* (2010) and Lee *et al.* (2007) propose a guidance law with controllable attack time and angle-of-attack constraint and apply it to the salvo attack of anti-ship missiles.

1.Northwestern Polytechnical University - School of Automation - Xi'an/Shanxi - China.

*Correspondence author: lx861002@163.com
Received: Feb. 14, 2018 | Accepted: Apr. 17, 2018

Section Editor: Luiz Martins-Filho



Based on this idea, researchers subsequently introduced other guidance and control methods, including sliding mode control (SMC) (Hail and Balakrishnan 2012; Cho *et al.* 2016), optimal control (Nikusokhan and Nobahari 2016), differential game (Kang and Kim 2011), and dynamic surface control (Wang *et al.* 2015). These methods rely on specifying attack time before launching to achieve coordination. As no information exchange occurs between missiles during flight, these methods apparently have temporal limitations. With progress in the consensus of multi-agent systems, researchers have begun to use the consensus theory to study the cooperative guidance and control of multi-interceptors. Using the coordination strategy under the cooperative guidance framework, Kumar and Ghose (2014) adjust missile trajectories so that the coordination variable of each missile can approach the expected coordination variable for realizing cooperative guidance. Zhao *et al.* (2014) apply leader-follower formation control to the cooperative guidance of multi-interceptors by employing an analogous leader-follower cooperative guidance framework. Sun *et al.* (2014) and Zhao *et al.* (2016) explore the guidance and control law of the leader-follower topology considering time delay and topology switch. By constructing an integrated cost function for multiple missiles, Shaferman and Shima (2015) design a cooperative guidance law for multiple missiles for intercepting a maneuvering target. However, the application of this function is faced with multiple constraints, as each missile requires the global information of all participating partners. Balhance *et al.* (2017) study the cooperative guidance law using the optimal control theory and improves communication between multiple missiles. These consensus-based cooperative guidance and control approaches typically employ the regular form of the cooperative control commands.

Conventionally, in the design of the guidance and control system of interceptors, a control loop is set as a fast loop whereas a guidance loop is set as a slow loop. The basis of these methods is to design two subsystems independently, without considering the coupling between the two loops. On the contrary, integrated guidance and control (IGC) design depends on the control force generated from the engagement information between an interceptor and a target and the kinematic information of the interceptor per se to drive the interceptor to hit the target. This can ensure the stability of interceptor flight attitude and improve guidance accuracy (Menon and Ohlmeyer 2001; Shtessel *et al.* 2009). In recent years, researchers have integrated IGC design with various control theories, such as SMC (Shtessel *et al.* 2009; Lee *et al.* 2016), back-stepping control (Seyedipour *et al.* 2017; Ran *et al.* 2014), optimal control (Vaddi *et al.* 2009), and predictive control (Shamaghdari *et al.* 2015), for creating a suite of aircraft IGC design methods with diverse features. Even though it is well known that the advantages of IGC methods can be utilized to enhance the stability of multi-interceptor systems, research in this area is still inadequate at the moment.

Therefore, by adopting the above-discussed IGC method, an improved distributed cooperative IGC algorithm for multiple interceptor missiles featuring the leader-follower topology is proposed in this study based on the distributed network cooperative control strategy and SMC theory, with the aim of improving the rate of convergence of inceptor missiles to cooperative control commands.

IGC MODEL FOR THE LEADING INTERCEPTOR

The engagement geometry of the leading interceptor and target in the pitch channel are shown in Fig. 1.

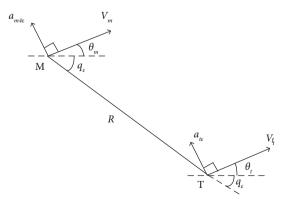


Figure 1. Engagement geometry of the leading interceptor and target.

In Fig. 1, M and T denote the interceptor missile and target, respectively; $a_{md\varepsilon}$ and $a_{t\varepsilon}$ are the accelerations of the missile and target, respectively; V_m and V_t represent missile velocity and target velocity, respectively; θ_m and θ_t are the flight path angles of the missile and target, respectively; q_{ε} is the missile/target LOS angle; R is the distance between the missile and target. The relative kinematic model of the interceptor in the longitudinal plane can be obtained as (Eq. 1):

$$\begin{cases} \dot{r} = V_t \cos(q_{\varepsilon} - \theta_t) - V_m \cos(q_{\varepsilon} - \theta_m) \\ r\dot{q}_{\varepsilon} = V_m \sin(q_{\varepsilon} - \theta_m) - V_t \sin(q_{\varepsilon} - \theta_t) \end{cases}$$
(1)

The kinematic model of the leading interceptor in the pitch channel is expressed as (Eq. 2):

$$\begin{cases} \dot{\alpha} = \omega_z - \frac{qSC_y^{\alpha}\alpha\cos\alpha}{mV_m} + d_{\alpha} \\ \omega_z = \frac{qS\overline{L}m_z^{\alpha}\alpha}{J_z} + \frac{qS\overline{L}m_z^{\omega_z}\omega_z}{J_z} + \frac{M_z}{J_z} + d_{\omega_z} \\ a_{m3\varepsilon} = \frac{qSC_y^{\alpha}\alpha}{m} \end{cases}$$
(2)

where S is the reference area of the missile; m the missile mass; α is the angle of attack (AOA); ω_z is the pitch angular velocity; q is the dynamic pressure; d_α and d_{ω_z} are the perturbation and uncertain disturbance in each part of the system, respectively; J_z is the rotational inertia of the missile; C_y^a , m_z^a , and $m_z^{\omega_z}$ denote the aerodynamic force and moment coefficients; and M_z is the control moment of the missile in the pitch channel.

Based on Eqs. 1 and 2, if we define $x_1 = q_{\varepsilon}$, $x_2 = \dot{q}_{\varepsilon}$, $x_3 = \alpha$, and $x_4 = \omega_z$, the nonlinear IGC model of the leading interceptor in the pitch channel can be written as (Eq. 3):

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = a_{22}x_2 + a_{23}x_3 + \frac{a_{t\varepsilon}}{r} \\ \dot{x}_3 = a_{33}x_3 + x_4 + d_{\alpha} \\ \dot{x}_4 = a_{43}x_3 + a_{44}x_4 + b_4u + d_{\omega_z} \\ y_2 = x_2 \end{cases}$$
(3)

where
$$a_{22} = -\frac{2\dot{r}}{r}$$
, $a_{23} = -\frac{qSC_y^{\alpha}}{mr}$, $a_{33} = -\frac{qSC_y^{\alpha}}{mV_m}$, $a_{43} = \frac{qS\overline{L}m_z^{\alpha}}{J_z}$, $a_{44} = \frac{qS\overline{L}m_z^{\omega_z}}{J_z}$, $b_4 = \frac{1}{J_z}$, and $u = M_z$.

Assumption 1: The LOS angle of the interceptor varies insignificantly during the terminal phase of guidance. In addition, the angle between the SOL direction and velocity direction is small; hence, $a_{m3\varepsilon} \approx a_{m4\varepsilon}$.

Assumption 2: The unknown disturbances in the IGC system, d_{α} and d_{w_z} , are continuously differentiable and have a bounded first derivative, i.e., $d_i < L$, where L is a positive constant.

FTDO DESIGN

An FTDO estimates the nonlinear uncertain terms in the system model and feeds their estimated values into the control system for compensation. To eliminate the effects of the unknown disturbances involved in model (Eq. 3), viz., a_{tc} , d_{α} , and d_{ω_z} , on the control system of the leading interceptor, an FTDO is designed to estimate these terms.

Defining $v_r = \dot{r}$ and ve = $r\dot{q}_s$, from Eq. 1, we have (Eq. 4)

$$\dot{v}_{\varepsilon} = \dot{r}\dot{q}_{\varepsilon} + r\ddot{q}_{\varepsilon} = \dot{r}\dot{q}_{\varepsilon} - 2\dot{r}\dot{q}_{\varepsilon} + a_{t\varepsilon} - a_{m4\varepsilon} = -\frac{V_{r}V_{\varepsilon}}{r} + a_{t\varepsilon} - a_{m4\varepsilon}$$

$$(4)$$

The longitudinal acceleration of the target, a, can be estimated using the following FTDO (Eq. 5):

$$\begin{cases} \dot{z}_{20} = v_{20} + g_2, \dot{z}_{21} = v_{21}, \dot{z}_{22} = v_{22} \\ v_{20} = -\lambda_{20} I_2^{1/3} |z_{20} - v_{\varepsilon}|^{2/3} \operatorname{sgn}(z_{20} - v_{\varepsilon}) - \sigma_{20}(z_{20} - v_{\varepsilon}) + z_{21} \\ v_{21} = -\lambda_{21} I_2^{1/2} |z_{21} - v_{20}|^{1/2} \operatorname{sgn}(z_{21} - v_{20}) - \sigma_{21}(z_{21} - v_{20}) + z_{22} \\ v_{22} = -\lambda_{22} L_2 |z_{22} - v_{21}|^{g_2/p_2} \operatorname{sgn}(z_{22} - v_{21}) - \sigma_{22}(z_{22} - v_{21}) \\ z_{20} = \tilde{v}_{\varepsilon}, z_{21} = \tilde{a}_{t\varepsilon}, z_{22} = \tilde{a}_{t\varepsilon} \end{cases}$$
(5)

where $g_2 = -(v_r v_\epsilon/r) - (qSC_y^a/m)a$; \tilde{v}_ϵ and $\tilde{a}_{t\epsilon}$ are the disturbance estimates of v_ϵ and $a_{t\epsilon}$, respectively; λ_{20} , λ_{21} , λ_{22} , σ_{20} , σ_{21} , and σ_{22} are the design parameters of the FTDO; q_2 and p_3 are terminal parameters with $0 < p_2 < q_3$.

According Shtessel *et al.* (2007), the FTDO error system is stable during finite time; thus, we define the estimation error of the target acceleration as $e_{21} = z_{21} - a_{10}$.

Similarly, the disturbances of the leading interceptor in the AOA loop and pitch angular velocity loop, d_{α} and d_{ω_z} , can be estimated by (Eqs. 6 and 7):

$$\begin{cases} \dot{z}_{30} = v_{30} + g_3, \dot{z}_{31} = v_{31}, \dot{z}_{32} = v_{32} \\ v_{30} = -\lambda_{30} L_3^{1/3} \mid z_{30} - x_3 \mid^{2/3} \operatorname{sgn}(z_{30} - x_3) - \sigma_{30}(z_{30} - x_3) + z_{31} \\ v_{31} = -\lambda_{31} L_3^{1/2} \mid z_{31} - v_{30} \mid^{1/2} \operatorname{sgn}(z_{31} - v_{30}) - \sigma_{31}(z_{31} - v_{30}) + z_{32} \\ v_{32} = -\lambda_{32} L_3 \mid z_{32} - v_{31} \mid^{q_3/p_3} \operatorname{sgn}(z_{32} - v_{31}) - \sigma_{32}(z_{32} - v_{31}) \\ z_{30} = \tilde{x}_3, z_{31} = \tilde{d}_{\alpha}, z_{32} = \tilde{d}_{\alpha} \end{cases}$$

$$(6)$$

$$\begin{cases} \dot{z}_{40} = v_{40} + g_4, \dot{z}_{41} = v_{41}, \dot{z}_{42} = v_{42} \\ v_{40} = -\lambda_{40} L_4^{1/3} \mid z_{40} - x_4 \mid^{2/3} \operatorname{sgn}(z_{40} - x_4) - \sigma_{40}(z_{40} - x_4) + z_{41} \\ v_{41} = -\lambda_{41} L_4^{1/2} \mid z_{41} - v_{40} \mid^{1/2} \operatorname{sgn}(z_{41} - v_{40}) - \sigma_{41}(z_{41} - v_{40}) + z_{42} \\ v_{42} = -\lambda_{42} L_4 \mid z_{42} - v_{41} \mid^{q_4/p_4} \operatorname{sgn}(z_{42} - v_{41}) - \sigma_{42}(z_{42} - v_{41}) \\ z_{40} = \tilde{x}_4, z_{41} = \tilde{d}_{\omega_4}, z_{32} = \tilde{d}_{\omega_6} \end{cases}$$
 (7)

where $g_3 = a_{33}x_3 + x_4$; $g_4 = a_{43}x_3 + a_{44}x_4 + b_4u$; \tilde{d}_a and \tilde{d}_{ω_z} are the estimated values of d_α and d_{ω_z} with estimation errors of $e_{31} = z_{31} - d_\alpha$ and $e_{41} = z_{41} - d_{\omega_z}$, respectively.

DESIGN OF THE NONSINGULAR FAST DYNAMIC SMC CONTROLLER

The interceptor IGC model is a mismatched uncertain system; we designed a nonsingular fast dynamic surface SMC model as the control algorithm for the leading interceptor, based on the IGC model (Eq. 3) and FTDO estimations (Eqs. 5 to 7).

• According to dynamic surface SMC design, the second subsystem in Eq. 3 is considered. x_{2d} is defined as the system tracking command signal.

The first dynamic error surface is defined as (Eq. 8):

$$s_2 = -a_{23}^{-1}(x_2 - x_{2d}) (8)$$

The derivative of s_2 is determined to obtain the error dynamic equation (Eq. 9):

$$\dot{s}_2 = a_{23}^{-2} \dot{a}_{23} (x_2 - x_{2d}) - a_{23}^{-1} (a_{22} x_2 + \frac{a_{tE}}{r} - \dot{x}_{2d}) - x_3 \tag{9}$$

The FTDO-estimated $\tilde{a}_{t\varepsilon}$ from Eq. 5 is substituted into Eq. 9 to acquire the virtual control input of the first dynamic surface (Eq. 10):

$$x_3^* = a_{23}^{-2} \dot{a}_{23} (x_2 - x_{2d}) + k_2 s_2 - a_{23}^{-1} (a_{22} x_2 + \frac{\tilde{a}_{t\varepsilon}}{r} - \dot{x}_{2d})$$
(10)

where $k_2 > 0$. To prevent the increase in computational complexity owing to the 'explosion of terms' when finding the derivative of the virtual control input, x_3^* is fed through a first-order low-pass filter to obtain the filtered virtual control input (Eq. 11):

$$\tau_3 \dot{\bar{x}}_3^* + \bar{x}_3^* = x_3^*, \bar{x}_3^*(0) = x_3^*(0) \tag{11}$$

where τ_3 is the time constant of the filter. Hence, the derivative of the virtual control input after error surface filtering is (Eq. 12):

$$\dot{\overline{x}}_3^* = -\tau_3^{-1}(\overline{x}_3^* - x_3^*) \tag{12}$$

• The second dynamic error surface is defined as (Eq. 13):

$$s_3 = x_3 - \overline{x}_3^* \tag{13}$$

The derivative of s_3 is determined to obtain the error dynamic equation (Eq. 14):

$$\dot{s}_3 = \dot{x}_3 - \dot{\bar{x}}_3^* = a_{33}x_3 + x_4 + d_\alpha - \dot{\bar{x}}_3^* \tag{14}$$

Based on the design approach of the first dynamic surface, the FTDO-estimated \tilde{d}_a from Eq. 6 is substituted into Eq. 14 to acquire the virtual control input for the second dynamic surface (Eq. 15):

$$x_4^* = -a_{33}x_3 - \tilde{d}_\alpha + \dot{\bar{x}}_3^* - k_3 s_3 \tag{15}$$

where $k_3 > 0$. x_4^* is fed through a low-pass filter to obtain (Eq. 16):

$$\tau_4 \dot{\overline{x}}_4^* + \overline{x}_4^* = x_4^*, \overline{x}_4^*(0) = x_4^*(0) \tag{16}$$

where τ_4 is the time constant of the filter. Hence, the derivative of the virtual control input after error surface filtering is (Eq. 17):

$$\dot{\bar{x}}_4^* = -\tau_4^{-1} (\bar{x}_4^* - x_4^*) \tag{17}$$

• The third dynamic error surface is defined as (Eq. 18):

$$s_4 = x_4 - \overline{x}_4^* \tag{18}$$

The derivative of s_4 is determined to obtain the error dynamic equation (Eq. 19):

$$\dot{s}_4 = \dot{x}_4 - \dot{\bar{x}}_4^* = a_{43}x_3 + a_{44}x_4 + b_4u + d_{\omega_z} - \dot{\bar{x}}_4^*$$
(19)

To prevent singularity in the leading interceptor system and to converge to the equilibrium position within limited time, we design a nonsingular fast sliding mode reaching law (Eq. 20):

$$\dot{s} = -|x_a|^{p/q-1} [k_a s + k_b |s|^{\hat{\sigma}} \operatorname{sgn}(s)]$$
(20)

where $p, q \in N^+$ and odd, $1 < p/q < 2, k_a > 0, k_b > 0$, and $0 < \partial < 1$.

Based on Eqs. 19 and 20 and the FTDO-estimated \tilde{d}_{ω_z} from Eq. 7, the improved nonsingular fast dynamic surface SMC law of the leading interceptor is (Eq. 21):

$$u = b_4^{-1} \left[-a_{43} x_3 - a_{44} x_4 - \tilde{d}_{\omega_*} + \dot{\bar{x}}_4^* - k_4 |x_4|^{p/q-1} s_4 - k_5 |x_4|^{p/q-1} |s_4|^{\delta} \operatorname{sgn}(s_4) \right]$$
 (21)

where $k_4 > 0$, $k_5 > 0$, 1 < p/q < 2, and $0 < \partial < 1$.

STABILITY ANALYSIS

It is assumed that the estimation errors of the FTDO system satisfy (Eq. 22):

$$|e_{21}| < N_2, |e_{31}| < N_3, |e_{41}| < N_4$$
 (22)

where N_2 , N_3 , and N_4 are positive constants.

Filtering errors are defined as follows (Eq. 23):

$$y_3 = \overline{x}_3^* - x_3^*, y_4 = \overline{x}_4^* - x_4^*$$
 (23)

The derivatives of y_3 and y_4 are determined to obtain the dynamic errors of filtering (Eq. 24):

$$\dot{y}_3 = -\tau_3^{-1} y_3 - \dot{x}_3^*, \ \dot{y}_4 = -\tau_4^{-1} y_4 - \dot{x}_4^* \tag{24}$$

Based on Eqs. 8 to 18 and 23, we have:

$$\begin{cases} x_2 = -a_{23}s_2 + x_2 d \\ x_3 = s_3 + \overline{x}_3^* = s_3 + y_3 + x_3^* \\ x_4 = s_4 + \overline{x}_4^* = s_4 + y_4 + x_4^* \end{cases}$$
(25)

Based on Eqs. 3, 8 to 18, and 23 to 25, we have (Eq. 26 to 28):

$$\dot{s}_2 = a_{23}\dot{a}_{23}(x_2 - x_{2d}) - a_{23}^{-1}(a_{22}x_2 + \frac{a_{t\varepsilon}}{r} - \dot{x}_{2d}) - s_3 - y_3 - x_3^* = -s_3 - y_3 - k_2s_2 + \tilde{e}_{21}$$
(26)

where $\tilde{e}_{21} = \frac{m}{qSC_v^{\alpha}}(\tilde{a}_{t\varepsilon} - a_{t\varepsilon})$.

It is assumed that $|\tilde{e}_{21}| < \tilde{N}_2$, where \tilde{N}_2 is a positive constant.

$$\dot{s}_3 = a_{33}x_3 + s_4 + y_4 + x_4^* + d_\alpha - \dot{x}_3^* = s_4 + y_4 - k_3s_3 - e_{31}$$
(27)

$$\dot{s}_4 = a_{43}x_3 + a_{44}x_4 + b_4u + d_{\omega_c} - x_4^* = -k_4 |x_4|^{p/q-1} s_4 - k_5 |x_4|^{p/q-1} |s_4|^{\delta} \operatorname{sgn}(s_4) - e_{41}$$
(28)

As all variables and their derivatives in the system model are bounded, there exist continuous functions $\tilde{z}_3 < 0$ and $\tilde{z}_4 < 0$ such that variables \dot{x}_3^* and \dot{x}_4^* satisfy (Eq. 29):

$$|\dot{x}_{3}^{*}| \leq \tilde{z}_{3}(s_{2}, s_{3}, y_{3}, y_{4}, e_{21}, e_{31}, k_{2}, k_{3}, x_{2d}, \dot{x}_{2d}, \ddot{x}_{2d})$$

$$|\dot{x}_{4}^{*}| \leq \tilde{z}_{4}(s_{2}, s_{3}, s_{4}, y_{3}, y_{4}, e_{21}, e_{31}, k_{2}, k_{3}, x_{2d}, \dot{x}_{2d}, \ddot{x}_{2d})$$
(29)

Given constants χ and R^* , where $\chi > 0$ and $R^* > 0$, the following compact sets are defined: $B_2 = [x_{2d}, \dot{x_{2d}}, \dot{x_{2d}}]^T$, $x_{2d} + \dot{x}_{2d} + \dot{x}_{2d} \leq \chi$ and $B_2 = [s_2, s_3, s_4, y_3, y_4, e_{21}, e_{31}]^T$, s_2^2 , s_3^2 , s_4^2 , y_3^2 , $y_4^2 \leq R^*$. Moreover, we know that $B_1 \times B_2$ is a compact set. Let constants M_3 and M_4 be the maxima of \tilde{z}_3 and \tilde{z}_4 on $B_1 \times B_2$, respectively, where $M_3 > 0$ and $M_4 > 0$. We have (Eq. 30):

$$|\dot{x}_{3}^{*}| \leq M_{3}, |\dot{x}_{4}^{*}| \leq M_{4} \tag{30}$$

Based on Eqs. 25 to 28, the following can be obtained (Eqs. 31 to 35):

$$s_2\dot{s}_2 = s_2(-s_3 - y_3 - k_2s_2 + \tilde{e}_{21}) \le (\frac{3}{2} - k_2)s_2^2 + \frac{1}{2}s_3^2 + \frac{1}{2}y_3^2 + \frac{1}{2}\tilde{N}_2^2$$
(31)

$$s_3 \dot{s}_3 = s_3 (s_4 + y_4 - k_3 s_3 - e_{31}) \le (\frac{3}{2} - k_3) s_3^2 + \frac{1}{2} s_4^2 + \frac{1}{2} y_4^2 + \frac{1}{2} N_3^2$$
(32)

$$s_{4}\dot{s}_{4} = s_{4}(-k_{4} | x_{4} |^{p/q-1} s_{4} - k_{5} | x_{4} |^{p/q-1} | s_{4} |^{\partial} \operatorname{sgn}(s_{4}) - e_{41}) \le -k_{4} | x_{4} |^{p/q-1} s_{4}^{2} - k_{5} | x_{4} |^{p/q-1} | s_{4} |^{\partial+1} + \frac{1}{2} s_{4}^{2} + \frac{1}{2} e_{41}^{2} \le \frac{1}{2} - k_{4} | x_{4} |^{p/q-1} + \frac{3}{2} k_{5} | x_{4} |^{p/q-1} s_{4}^{2} + \frac{1}{2} k_{5} | x_{4} |^{p/q-1}$$

$$(33)$$

$$y_3 \dot{y}_3 = y_3 \left(-\tau_3^{-1} y_3 - \dot{x}_3^* \right) \le -\tau_3^{-1} y_3^2 + \frac{1}{2} \left(y_3^2 + M_3^2 \right) \tag{34}$$

$$y_4 \dot{y}_4 = y_4 \left(-\tau_4^{-1} y_4 - \dot{x}_4^* \right) \le -\tau_4^{-1} y_4^2 + \frac{1}{2} \left(y_4^2 + M_4^2 \right) \tag{35}$$

According to the nonlinear IGC model in Eq. 3, the Lyapunov function is considered as:

$$V = \frac{1}{2}(s_2^2 + s_3^2 + s_4^2 + y_3^2 + y_4^2)$$
(36)

The derivatives of both sides of Eq. (36) are determined to obtain (Eq. 37):

$$\dot{V} = s_2 \dot{s}_2 + s_3 \dot{s}_3 + s_4 \dot{s}_4 + y_3 \dot{y}_3 + y_4 \dot{y}_4 \le \left(\frac{3}{2} - k_2\right) s_2^2 + \frac{1}{2} s_3^2 + \frac{1}{2} y_3^2 + \frac{1}{2} \tilde{N}_2^2 + \left(\frac{3}{2} - k_3\right) s_3^2 + \frac{1}{2} s_4^2 + \frac{1}{2} y_4^2 + \frac{1}{2} N_3^2 + \left(\frac{1}{2} - k_4 + \frac{3}{2} k_5\right) s_4^2 + \frac{1}{2} N_4^2 + \frac{1}{2} k_5 - \tau_3^{-1} y_3^2 + \frac{1}{2} \left(y_3^2 + M_3^2\right) + -\tau_4^{-1} y_4^2 + \frac{1}{2} \left(y_4^2 + M_4^2\right)$$
(37)

The design parameters should satisfy (Eq. 38):

$$\begin{cases} k_{2} \ge \frac{3}{2} + \frac{1}{2}\kappa, k_{3} \ge 2 + \frac{1}{2}\kappa, k_{4} \ge \frac{3}{2}k_{5} + 1 + \frac{1}{2}\kappa \\ \tau_{3}^{-1} \ge 1 + \frac{1}{2}\kappa, \tau_{4}^{-1} \ge 1 + \frac{1}{2}\kappa \end{cases}$$
(38)

where κ is a constant, and $\kappa > 0$. Thus, we have:

$$\dot{V} \le \kappa V + \hat{A} \tag{39}$$

where
$$\hat{A} = \frac{1}{2}\tilde{N}_2^2 + \frac{1}{2}N_3^2 + \frac{1}{2}N_4^2 + \frac{1}{2}M_3^2 + \frac{1}{2}M_4^2 + \frac{1}{2}k_5$$
.

From Eq. 39, we finally have (Eq. 40):

$$V(t) \le \{ \lceil \kappa V(0) - \widehat{A} \rceil e^{-\kappa t} + \widehat{A} \} / \kappa \tag{40}$$

Therefore, system convergence can be ensured by appropriately adjusting design parameters k_2 , k_3 , k_4 , k_5 , τ_3 , and τ_4 . If k_2 , k_3 , k_4 , and k_5 are increased while τ_3 and τ_4 are reduced, a sufficiently large κ can be ensured so that filtering error and error surface are sufficiently small. This ensures control accuracy.

DESIGN OF DISTRIBUTED NETWORK BASED COOPERATIVE CONTROL STRATEGY

The problem of the cooperative control of multiple intelligent agents can be described as a graph, which can be analyzed using graph theory. For the guidance and control of multiple interceptor missiles, one missile acquires the state information of other missiles through information exchange to achieve coordination among them. Therefore, a leader-follower topological structure that consists of one leading interceptor and n following interceptors can be built. This structure is described using an undirected graph. Regarding each missile as a communication node, the information exchange between missiles is expressed as $\bar{G} = \{\bar{V}, \bar{E}, \bar{A}\}$, where $\bar{V} = \{\bar{v}_1, \bar{v}_2, \bar{v}_3, \dots, \bar{v}_n\}$ represents the set formed by all missile nodes, \bar{E} denotes the links between nodes, and $\bar{A} = [\bar{a}_{ij}] \in R^n \times^n$ is the adjacency matrix of the undirected graph. If information exchange exists between nodes i and j, then $\bar{a}_{ij} > 0$; otherwise, $\bar{a}_{ij} = 0$. \bar{L} is the Laplace matrix of \bar{G} , the elements of which satisfy (Eq. 41):

$$\begin{cases} \overline{l}_{ii} = \sum_{j=1, j \neq i}^{n} \overline{a}_{ij} \\ \overline{l}_{ij} = -\overline{a}_{ij}, j \neq i \end{cases}$$

$$(41)$$

In a multi-missile topology with a leading interceptor, the leading interceptor features an independent state that does not change with followers. The purpose of including the leader state into the synchronization algorithm as part of the cooperative control strategy is that follower states should approach the leader state.

Let $\overline{B} = \text{diag } \{\overline{b}_1, \overline{b}_2,\overline{b}_n\}$ represent whether each follower can acquire the information of the leader, where $\overline{b}_i > 0, i \in \{1, 2, 3,, n\}$ implies yes and $\overline{b}_i = 0, i \in \{1, 2, 3,, n\}$ implies no.

Based on the fixed leader-follower topology, an improved cooperative control strategy for multiple interceptors can be designed using the distributed network method, as follows (Eq. 42):

$$v_{i} = \overline{k}_{i1} \left(\sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{0} - x_{i}) \right) + \overline{k}_{i2} \left| \sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{0} - x_{i}) \right|^{\hat{c}_{i}} \operatorname{sgn} \left(\sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{0} - x_{i}) \right) + \dot{x}_{0}$$

$$(42)$$

where x_0 denotes the position of the leader; x_i , $i \in \{1, 2, 3,, n\}$ denotes the position of a follower; $v_i = \dot{x}_i$ denotes the velocity of a follower; $\partial_i > 0$; $\bar{k}_{i1} > 0$ and $\bar{k}_{i2} > 0$ are constants.

Proof:

Lemma 1(Zou *et al.* 2010): Laplace matrix \bar{L} has the following properties:

- If \bar{G} is connected, the eigenvalue of \bar{L} is , which is referred to as the algebraic connectivity of the graph; a larger value indicates a more connected network.
- 0 is one eigenvalue of \bar{L} , and the corresponding eigenvector is 1.

Defining an error variable, $e_i = x_i - x_0$, we have (Eq. 43):

$$\dot{e}_{i} = \dot{x}_{i} - \dot{x}_{0} = \overline{k}_{i1} \left(\sum_{j=1}^{n} \overline{a}_{ij} (e_{j} - e_{i}) + \overline{b}_{i} e_{i} \right) + \overline{k}_{i2} \left| \sum_{j=1}^{n} \overline{a}_{ij} (e_{j} - e_{i}) + \overline{b}_{i} e_{i} \right|^{\partial_{i}} \operatorname{sgn} \left(\sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{0} - x_{i}) \right)$$

$$(43)$$

The Lyapunov function is defined as (Eq. 44):

$$V = \frac{1}{2}e^{T}(\overline{L} + \overline{B})e \tag{44}$$

where $e = [e_1, e_2, ..., e_n]^T$.

We define $\bar{k}_1 = \min\{\bar{k}_{i1}\}$, $\bar{k}_2 = \min\{\bar{k}_{i2}\}$, and $\bar{\partial} = \min\{\bar{\partial}_i\}$. The derivatives of Eq. 44 are determined to obtain (Eq. 45):

$$\dot{V} = \dot{e}^{T}(\bar{L} + \bar{B})e = -\sum_{i=1}^{n} \left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]\dot{e}_{i} = -\sum_{i=1}^{n} \left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]\left[\bar{k}_{i1}\left(\sum_{j=1}^{n} \bar{a}_{ij}(e_{j} - e_{i}) + \bar{b}_{i}e_{j}\right) + \\
+ \bar{k}_{i2}\left|\sum_{j=1}^{n} \bar{a}_{ij}(e_{j} - e_{i}) + \bar{b}_{i}e_{j}\right|^{\hat{c}_{i}} \operatorname{sgn}\left(\sum_{j=1}^{n} \bar{a}_{ij}(x_{j} - x_{i}) + \bar{b}_{i}(x_{0} - x_{i})\right) = -\sum_{i=1}^{n} \bar{k}_{i1}\left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]^{2} - \sum_{i=1}^{n} \bar{k}_{i2}\left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]^{1+\hat{c}_{i}} \leq \\
\leq -\bar{k}_{1}\sum_{i=1}^{n}\left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]^{2} - \bar{k}_{2}\sum_{i=1}^{n}\left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]^{1+\hat{c}_{i}} \leq -\bar{k}_{1}\sum_{i=1}^{n}\left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]^{2} - \bar{k}_{2}\left(\sum_{i=1}^{n}\left[\sum_{j=1}^{n} a_{ij}(e_{j} - e_{i}) - \bar{b}_{i}e_{i}\right]^{2}\right)^{\frac{1+\hat{c}_{i}}{2}}\right]$$

Considering $V(e) \neq 0$, Eq. 45 can be rewritten as:

$$\frac{\sum_{i=1}^{n} \left[\sum_{j=1}^{n} a_{ij} (e_{j} - e_{i}) - \overline{b}_{i} e_{i}\right]^{2}}{V(e)} = \frac{e^{T} (\overline{L} + \overline{B})^{T} (\overline{L} + \overline{B}) e}{\frac{1}{2} (e^{T} (\overline{L} + \overline{B})^{T} e)} \ge 2\lambda_{\min}(\overline{L} + \overline{B})$$
(46)

From Eqs. 46 to 47:

$$\dot{V}(t) \le -\overline{k}_1[2\lambda_{\min}(\overline{L} + \overline{B})] - \overline{k}_2[2\lambda_{\min}(\overline{L} + \overline{B})]^{\frac{1+\partial}{2}}$$

$$\tag{47}$$

It is known from Lemma 1 that V(t) can converge within finite time. That is, followers can converge to the state of the leader, achieving successful cooperative guidance and control for multiple interceptors.

REALIZATION OF THE DISTRIBUTED NETWORK BASED COOPERATIVE CONTROL STRATEGY

The essence of multi-interceptor cooperative attack is to coordinate the positions of following interceptors and the leading interceptor. Therefore, to realize the distributed network synchronization strategy, each interceptor in the network must follow the velocity commands provided by the synchronization strategy given by Eq. 42.

The kinematic relations of the interceptors in the network that participate in coordinated attack are (Eq. 48):

$$\begin{cases} \dot{x}_i = V_i \cos \theta_i \\ \dot{y}_i = V_i \sin \theta_i \end{cases}$$
(48)

where \dot{x}_i and \dot{y}_i represent the two velocity components within the inertial frame of interceptor i in the pitch channel. Based on the distributed network synchronization strategy given in Eq. 42, the missile velocity reference commands are:

$$\begin{cases}
\overline{V}_{mxi} = \overline{k}_{i1} \left(\sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{m} - x_{i}) \right) \\
+ \overline{k}_{i2} \left| \sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{m} - x_{i}) \right|^{\hat{c}_{i}} \\
\operatorname{sgn} \left(\sum_{j=1}^{n} \overline{a}_{ij} (x_{j} - x_{i}) + \overline{b}_{i} (x_{m} - x_{i}) \right) + \dot{x}_{m}
\end{cases}$$

$$\begin{cases}
\overline{V}_{myi} = \overline{k}_{i1} \left(\sum_{j=1}^{n} \overline{a}_{ij} (y_{j} - y_{i}) + \overline{b}_{i} (y_{m} - y_{i}) \right) \\
+ \overline{k}_{i2} \left| \sum_{j=1}^{n} \overline{a}_{ij} (y_{j} - y_{i}) + \overline{b}_{i} (y_{m} - y_{i}) \right|^{\hat{c}_{i}} \\
\operatorname{sgn} \left(\sum_{j=1}^{n} \overline{a}_{ij} (y_{j} - y_{i}) + \overline{b}_{i} (y_{m} - y_{i}) \right) + \dot{y}_{m}
\end{cases}$$

$$(49)$$

Using Eqs. 48 and 49, the total velocity and flight path angle of the interceptor are obtained as (Eq. 50):

$$\begin{cases}
\overline{V}_{mi}^* = \sqrt{(\overline{V}_{mxi})^2 + (\overline{V}_{myi})^2} \\
\overline{\theta}_{mi}^* = \arctan\left(\frac{\overline{V}_{myi}}{\overline{V}_{mxi}}\right)
\end{cases}$$
(50)

The signal must be filtered to obtain the derivative of the total velocity and flight path angle, \dot{x} . Let \bar{x} and \bar{x}_1^* be the actual command and ideal command of the required signal, respectively. We obtain (Eq. 51):

$$\ddot{\overline{x}} = -2\zeta_n \omega_n \dot{\overline{x}} - \omega_n^2 \overline{x} + \omega_n^2 \overline{x}_1^* \tag{51}$$

where ζ_n and ω_n are the damping and bandwidth of the filter, respectively. The use of the filter can effectively address the differentiation problem of the command signals without affecting the amplitudes of the commands and their derivatives.

DESIGN OF FOLLOWING INTERCEPTOR CONTROLLER

It can be seen that the commands provided by the cooperative control strategy can be converted to velocity and flight path angle commands. The controller for following interceptors adopts the dynamic surface SMC algorithm to achieve command signal tracking for the missiles in the cooperative network. Assuming that missile velocities are controllable and air resistance and gravity can be neglected, the flight velocity of a follower can be expressed as (Eq. 52):

$$\dot{V}_m = \frac{\cos \alpha_i}{m} P_i \tag{52}$$

where P_i is engine thrust.

From Eq. 53, an error surface is defined as:

$$s_{v} = V_{m} - \overline{V}_{mi} \tag{53}$$

where \bar{V}_{mi} is the filtered total velocity of the interceptor. The derivative of s_v is obtained as (Eq. 54):

$$\dot{s}_{v} = \frac{\cos \alpha_{i}}{m} P_{i} - \dot{\overline{V}}_{mi} \tag{54}$$

where \dot{V}_{mi} is the derivative of \dot{V}_{mi} .

The sliding mode reaching law provided below is used to ensure that interceptor velocity can rapidly follow the system command.

$$\dot{s} = -k_a s - k_b |s|^{\lambda} \operatorname{sgn}(s) \tag{55}$$

Based on Eqs. 53 to 56, the engine thrust of a follower is (Eq. 56):

$$P_{i} = \frac{m}{\cos \alpha_{i}} [\dot{V}_{mi} - k_{v1} s_{v} - k_{v2} | s_{v}|^{\lambda_{v}} \operatorname{sgn}(s_{v})]$$
(56)

Let $x_{i1} = \theta_{mi}$, $x_{i2} = \alpha_{i2}$ and $x_{i3} = \omega_{i1}$. The kinematic equation of interceptor *i* in the pitch channel is (Eq. 57):

$$\begin{cases} \dot{x}_{i1} = a_{i23}x_{i2} + d_{i1} \\ \dot{x}_{i2} = a_{i33}x_{i2} + d_{i2} \\ \dot{x}_{i3} = a_{i43}x_{i2} + a_{i44}x_{i3} + b_{i3}u_{i} + d_{i3} \end{cases}$$
(57)

where
$$a_{i23} = \frac{q_i S C_{yi}^{\alpha_i}}{m V_m}$$
, $a_{i33} = -\frac{q_i S C_{yi}^{\alpha_i}}{m V_m}$, $a_{i43} = \frac{q_i S \overline{L} m_{zi}^{\alpha_i}}{J_z}$, $a_{i44} = \frac{q_i S \overline{L} m_{zi}^{\omega_{zi}}}{J_z}$, $b_{i4} = \frac{1}{J_z}$.

Following the FTDO used above for the leader, an FTDO is designed to estimate disturbance d_{ij} (Eq. 58):

$$\begin{cases} \dot{z}_{i10} = v_{i10} + a_{i23}x_{i2}, \dot{z}_{i11} = v_{i11}, \dot{z}_{i12} = v_{i22} \\ v_{i10} = -\lambda_{i10}L_{i1}^{1/3} \mid z_{i10} - x_{i1} \mid^{2/3} \operatorname{sgn}(z_{i10} - x_{i1}) + z_{i11} \\ v_{i11} = -\lambda_{i11}L_{i1}^{1/2} \mid z_{i11} - v_{i10} \mid^{1/2} \operatorname{sgn}(z_{i11} - v_{i10}) + z_{i12} \\ v_{i12} = -\lambda_{i12}L_{i1} \mid z_{i12} - v_{i11} \mid^{q_{i1}/p_{i1}} \operatorname{sgn}(z_{i12} - v_{i11}) \\ z_{i10} = \tilde{x}_{i1}, z_{i11} = \tilde{d}_{i1}, z_{i12} = \dot{d}_{i1} \end{cases}$$

$$(58)$$

where the estimated value of d_{i1} is \tilde{d}_{i1} and the estimation errors are $e_{i11} = z_{i11} - d_{i1}$.

Similarly, unknown disturbances d_{i2} and d_{i3} are estimated with estimation errors of $e_{i12} = z_{i12} - d_{i2}$ and $e_{i13} = z_{i13} - d_{i3}$, respectively. Based on the FTDO estimates and kinematic model in the pitch channel, the controller for following interceptors is designed using the dynamic surface SMC law.

• The first dynamic error surface is defined as (Eq. 59):

$$s_{i1} = a_{i23}^{-1}(x_{i1} - \overline{\theta}_m) \tag{59}$$

The derivative of s_{ij} is obtained (Eq. 60):

$$\dot{s}_{i1} = x_{i2} + a_{i23}^{-1} (d_{i1} - \dot{\overline{\theta}}_m) \tag{60}$$

Based on the dynamic surface design method and FTDO, the virtual control input of the first dynamic surface is (Eq. 61):

$$x_{i2}^* = a_{i23}^{-1} (-\tilde{d}_{i1} + \dot{\bar{\theta}}_m) - k_{i1} s_{i1}$$
(61)

where $k_{i1} > 0$. To prevent the increase in computational complexity owing to the 'explosion of terms' while finding the derivative of the virtual control input, x_3^* is fed through a first-order low-pass filter to obtain the filtered virtual control input (Eq. 62):

$$\tau_{i2}\dot{\bar{x}}_{i2}^* + \bar{\bar{x}}_{i2}^* = \bar{x}_{i2}^*, \bar{\bar{x}}_{i2}^*(0) = \bar{x}_{i2}^*(0) \qquad \qquad \dot{\bar{x}}_{i2}^* = -\tau_{i2}^{-1}(\bar{\bar{x}}_{i2}^* - \bar{x}_{i2}^*)$$
(62)

where $\tau_{i2} > 0$ is the time constant of the filter.

• The second dynamic error surface is defined as (Eq. 63):

$$s_{i2} = x_{i2} - \overline{x}_{i2}^* \tag{63}$$

The derivate of s_{i2} is determined (Eq. 64):

$$\dot{s}_{i2} = a_{i33}x_{i2} + x_{i3} + d_{i2} - \dot{\bar{x}}_{i2}^* \tag{64}$$

Similar to the first dynamic surface, the virtual control input of the second dynamic surface is (Eq. 65):

$$x_{i3}^* = -a_{i33}x_{i2} - \tilde{d}_{i2} + \dot{\bar{x}}_{i2}^* - k_{i2}s_{i2}$$
(65)

where $k_{i2} > 0$. x_{i3}^* is fed through the following low-pass filter to obtain (Eq. 66):

$$\tau_{i3}\dot{\bar{x}}_{i3}^* + \bar{x}_{i3}^* = x_{i3}^*, \bar{x}_{i3}^*(0) = x_{i3}^*(0)$$

$$\dot{\bar{x}}_{i3}^* = -\tau_{i3}^{-1}(\bar{x}_{i3}^* - x_{i3}^*)$$
(66)

where $\tau_{i3} > 0$ is the time constant of the filter.

• The third dynamic error surface is defined as (Eq. 67):

$$s_{i3} = x_{i3} - \overline{x}_{i3}^* \tag{67}$$

The derivative of s_{i3} is determined (Eq. 68):

$$\dot{s}_{i3} = a_{i43}x_{i2} + a_{i44}x_{i3} + b_{i3}u_i + d_{i3} - \dot{\bar{x}}_{i3}^*$$
(68)

The following sliding mode reaching law is used to ensure a high rate of convergence for the system (Eq. 69):

$$\dot{s} = -k_a s - k_b \left| s \right|^{\lambda} \operatorname{sgn}(s) \tag{69}$$

The dynamic surface SMC law for following interceptors is (Eq. 70):

$$u_{i} = b_{i3}^{-1} \left[-a_{i43} x_{i2} - a_{i44} x_{i3} - \tilde{d}_{i3} + \dot{\bar{x}}_{i3}^{*} - k_{i31} s_{i3} - k_{i32} \left| s_{i3} \right|^{\lambda_{i3}} \operatorname{sgn}(s_{i3}) \right]$$
 (70)

where $k_{i31} > 0$, $k_{i32} > 0$, and $0 < \lambda_{i3} < 1$.

The stability of the control algorithm for followers can be proved using Eqs. 20 to 40.

SIMULATION VALIDATION

To validate the effectiveness of the improved distributed cooperative IGC algorithm, we assume a communication topology in which the leader can communicate with three other followers and neighboring communication exists between the followers, as shown in Fig. 2. The initial conditions of the leader, followers, and target are listed in Table 1.

The parameters of the FTDO are provided below.

1) FTDO parameters of the leader:
$$\lambda_{20} = \lambda_{30} = \lambda_{40} = 2$$
, $\lambda_{21} = \lambda_{31} = \lambda_{41} = 1.5$, $\lambda_{22} = \lambda_{32} = \lambda_{42} = 2$, $q_2 = q_3 = q_4 = 0.5$, $p_2 = p_3 = p_4 = 8$, $\sigma_{20} = \sigma_{21} = \sigma_{22} = \sigma_{30} = \sigma_{31} = \sigma_{32} = \sigma_{40} = \sigma_{41} = \sigma_{42} = 0.1$, $L_2 = 100$, $L_3 = 10$, and $L_4 = 50$.

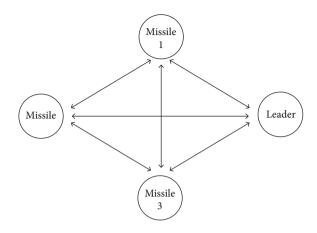


Figure 2. Communication topology of the leader and followers.

Table 1. Initial conditions of the leading interceptor, following interceptors, and target.
--

No.	ID	Parameter	Value	Parameter	Value	Parameter	Value
1	Leader	\mathcal{X}_{m0}	0 m	\mathcal{Y}_{m0}	3300 m	V_{m0}	400 m/s
2	Missile 1	x_{1m0}	100 m	\mathcal{Y}_{1m0}	2400 m	$V_{_{1m0}}$	400 m/s
3	Missile 2	x_{2m0}	300 m	$y_{_{2m0}}$	2700 m	$V_{_{2m0}}$	400 m/s
4	Missile 3	x_{3m0}	200 m	$y_{_{3m0}}$	2600 m	$V_{_{3m0}}$	400 m/s
5	Target	\mathcal{X}_{t0}	3000 m	\mathcal{Y}_{t0}	380 m	$V_{_{t0}}$	240 m/s

2) FTDO parameters of the followers: $\lambda_{i10} = \lambda_{i11} = \lambda_{i12} = 2$, $\lambda_{i11} = \lambda_{i21} = \lambda_{i31} = 1.5$, $\lambda_{i12} = \lambda_{i22} = \lambda_{i32} = 1.5$, $q_{i1} = q_{i2} = q_{i3}$ 0.5, $p_{i1} = p_{i2} = p_{i3} = 8$, and $L_{i1} = L_{i2} = L_{i3} = 10$.

Parameters of the dynamic surface SMC algorithm:

- 1) Parameters for the leader control law: $k_2 = 5$, $k_3 = 10$, $k_4 = 12$, $k_5 = 16$, $\delta = 0.6$, and $x_{2d} = 0$.
- 2) Parameters for the follower control law: $k_{v1} = k_{v2} = 2.5$, $k_{i1} = 5$, $k_{i2} = 2.5$, $k_{i3} = 10$, $k_{i31} = 40$, $k_{i32} = 5$, and $\lambda_{i1} = \lambda_{i3} = \lambda_{v} = 0.6$.

Parameters for the filter: $\tau_3 = \tau_4 = \tau_{i2} = \tau_{i3} = 0.002$, $\zeta_n = 0.8$, and $\omega_n = 40$.

Parameters for the distributed cooperative control strategy: ; $\bar{k}_{_{i1}} = 0.2$, $\bar{k}_{_{i2}} = 0.5$, and $\partial_{_i} = 0.6$.

It is assumed that the disturbance in the system is $d_3 = d_4 = d_{11} = d_{12} = d_{13} = 0.1\sin(t)$ and the target acceleration is a = 5 m/s².

The regular and improved distributed cooperative control strategies are examined in the simulations. The formula for the former is (Eq. 71):

$$v_i = \bar{k}_{j1} \left(\sum_{i=1}^n \bar{a}_{ij} (x_j - x_i) + \bar{b}_i (x_0 - x_i) \right) + \dot{x}_0 \tag{71}$$

where ; $\bar{k}_{i1} > 0.8$.

Simulation results are obtained using the parameters given above, and they are compared in Figs. 3 to 12.

The trajectories of the interceptors and target obtained using the two strategies are shown in Figs. 3 and 8. A comparison between the figures shows that when the improved strategy is used, follower trajectories gradually approach the target trajectory with a higher rate of convergence and smoother trajectory curves, and followers are able to hit the target by following the leader.

The velocity curves of the interceptors obtained using the two strategies are shown in Figs. 4 and 9. Convergence is reached at 6-8 s using the improved strategy, whereas it is reached at 8-10 s using the regular strategy. Comparisons between Figs. 5 and 10, 6 and 11, and 7 and 12 suggest that the improved strategy proposed in this study provides a higher rate of convergence and smoother transition with strong robustness.

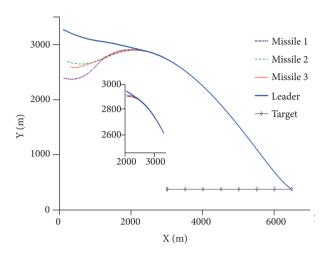


Figure 3. Trajectories of the interceptors and target obtained using the improved cooperative control strategy.

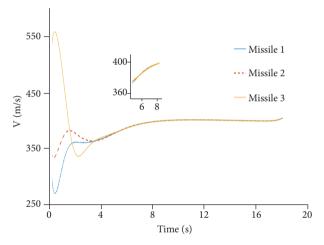


Figure 4. Velocity curves of the following interceptors obtained using the improved cooperative control strategy.

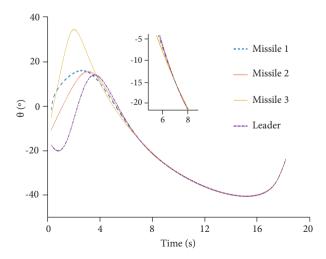


Figure 5. Flight path angles of the interceptors obtained using the improved cooperative control strategy.

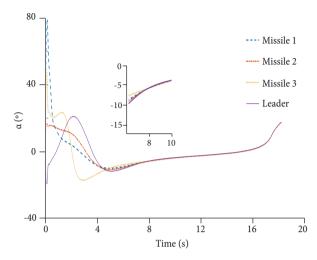


Figure 6. AOA curves of the interceptors obtained using the improved cooperative control strategy.

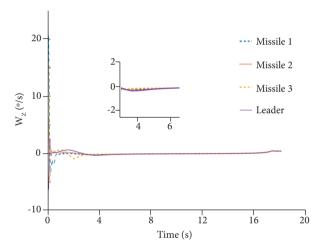


Figure 7. Pitch angular velocities of the interceptors obtained using the improved cooperative control strategy.

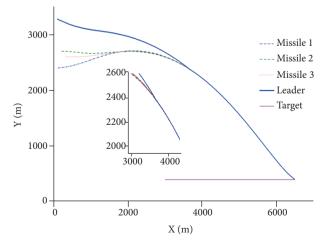


Figure 8. Trajectories of the interceptors and target obtained using the regular cooperative control strategy.

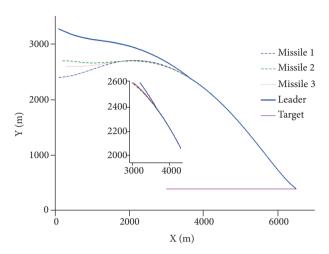


Figure 9. Velocity curves of the following interceptors obtained using the regular cooperative control strategy.

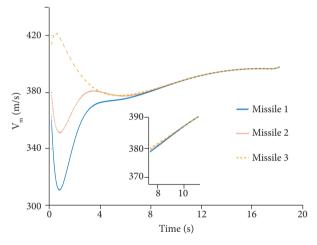


Figure 10. Flight path angles of the interceptors obtained using the regular cooperative control strategy.

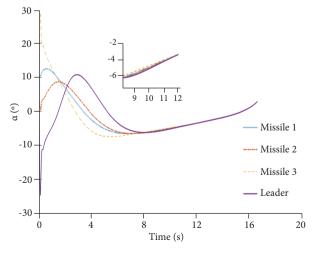


Figure 11. AOA curves of the interceptors obtained using the regular cooperative control strategy.

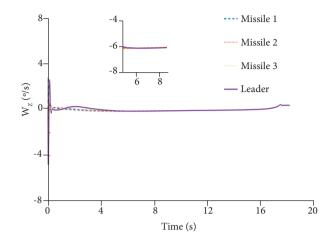


Figure 12. Pitch angular velocities of the interceptors obtained using the regular cooperative control strategy.

CONCLUSION

An improved distributed network cooperative IGC algorithm is developed based on the leader-follower topology to address the multi-interceptor IGC problem. The controller for the leading interceptor is designed based on an FTDO and the nonsingular fast dynamic surface SMC law, whose stability is proved using the Lyapunov principle. An improved multi-interceptor cooperative control strategy is proposed based on distributed network cooperative control. The following interceptor controller is similarly designed using an FTDO and dynamic surface SMC. The algorithm is validated using simulations. It is demonstrated that the developed algorithm can meet the cooperative guidance and control requirements of multiple interceptors while increasing the rate of convergence for the interceptors that react to cooperative control commands.

AUTHORS' CONTRIBUTION

Conceptualization, Liu X and Liang X; Methodology, Liu X; Investigation, Liu X; Writing – Original Draft, Liu X; Writing – Review and Editing, Liu X and Liang X; Funding Acquisition, Liang X; Resources, Liang X; Supervision, Liang X.

FUNDING

Aeronautical Science Foundation of China [http://dx.doi.org/10.13039/501100004750] Grant No 2016ZC12005

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