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# Levelized avoided cost of electricity model based on power system operation

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## Abstract

This paper presents a methodology to estimate the Levelized Avoided Cost of Electricity (LACE) of new generation projects based on the assessment of economic and operational benefits perceived by an existing power system. The marginal economic benefit caused by the integration of a new generation project is captured using the Differential Revenue Requirement method (DRR); whereas the operational benefits are observed by analyzing the performance of the new project through a preventive DC Security-Constrained Optimal Power Flow (SCOPF) tool. The SCOPF also allows quantifying economic benefits due to replacement of expensive generation, transmission congestion, and N-1 security improvement. Additionally, another metric, called Net Benefit (NB) of a generation project, expressed as the difference between LACE and LCOE (Levelized Cost of Electricity) is also employed in this work. It provides a realistic, easy-to-compute, and intuitive index that helps identifying the most promising generation projects during system expansion planning procedures. Finally, the proposed methodology is applied for computing LACE and NB of different generation projects in Colombia. According to the results, geothermal projects display the most significant LACE and NB. These metrics (LACE and NB) can become useful tools for decision-making in planning process.

**Keywords:** levelized costs of Electricity; avoided costs of electricity; generation expansion planning; power system optimization; security-constrained optimal power flow.

# Modelo de costo evitado nivelado de electricidad basado en la operación del sistema de potencia

## Resumen

Este artículo propone una metodología para estimar el Costo Evitado Nivelado de Electricidad (LACE) de nuevos proyectos de generación basados en la evaluación de beneficios económicos y operacionales, percibidos por un sistema de potencia existente. El beneficio económico marginal causado por la integración de un nuevo proyecto de generación es capturado usando el método Requerimiento de Ingreso Diferencial (DRR); mientras los beneficios operacionales son observados al analizar el desempeño del nuevo proyecto de generación a través un Flujo de Potencia Óptimo DC con Restricciones de Seguridad (SCOPF). SCOPF además permite cuantificar beneficios económicos debido al reemplazo de generación costosa, congestión de la transmisión y mejoramiento de la seguridad N-1. Adicionalmente, en este trabajo se emplea otra métrica, llamada Beneficio Neto (NB) de un proyecto de generación, expresado como la diferencia entre LACE y LCOE (Costo Nivelado de Electricidad). NB proporciona un índice intuitivo, realista y fácil de calcular, que ayuda a identificar los proyectos de generación más promisorios durante los procesos de planeación de la expansión del sistema. Finalmente, la metodología propuesta es aplicada para calcular LACE y NB de diferentes proyectos de generación en Colombia. De acuerdo a los resultados, los proyectos geotérmicos muestran los LACE y NB más significantes. Estas métricas (LACE y NB) pueden llegar a ser útiles herramientas para la toma de decisiones en procesos de planeación.

**Palabras clave:** costo nivelado de electricidad; costo evitado de electricidad; planeación de expansión de generación; optimización de sistemas de potencia; flujo óptimo de potencia con restricciones de seguridad.

## 1. Introduction

During electrical generation expansion planning process, economic benefits, size and operative performance of

different generation alternatives are evaluated by using technical and financial metrics. The well-known Levelized Cost of Electricity (LCOE) is a common financial indicator of different generation projects. According to different authors [1-4], the LCOE is the electricity price, in constant

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currency, at which energy output must be sold over the generation project life cycle for covering investment and O&M expenses, and return of capital to investors.

Although LCOE of different projects can be used to offer indicative signals for generation expansion planning [5], it has also been exposed that LCOE is not useful for comparing financial performance between intermittent and dispatchable generation technologies [6]. Also, according to [5], LCOE does not capture effects of power system dynamics. In order to overcome potential drawbacks of LCOE, the Energy Information Administration [7] has proposed to use the Levelized Avoided Cost of Electricity (LACE) under the context of the US electricity market. The LACE allows to effectively assess the technical-economic performance of a new generation project. Computing LACE requires the concept of Avoided Cost (AC), which represents potential cost savings in a power system once a new generation project is considered in the power system operations. The levelized term indicates an average cost per MWh of generation. This advantages work presents a novel methodology for computing LACE including operational features of a power system. We evaluate the economic benefit (or even disadvantage) of integrating a particular generation project into the power system by considering its technical operational characteristics and its impact on the economic dispatch. Thus, LACE can be used as a complementary indicator that provides decision makers with realistic and representative signals about generation expansion decisions.

The first contribution of this work is the proposed approach based on combining the SCOPF method supported by an operational tool like the SCOPF in order to effectively capture benefits (and/or disadvantages) of new generation projects. Not only does this tool evaluate an optimal power flow under normal conditions, but also N-1 post-contingency states are exhaustively considered. If the new project is a non-dispatchable technology (e.g. solar and wind), typical power output profiles are considered for computing LACE. The second contribution is the consideration of different generation scenarios within the power system for computing LACE of the new project. This approach allows to approximately capture the average value of a specific generation project over a set of generation as opposed to LCOE models that only employ a base case generation scenario of the project.

## 2. Literature review

LACE is conceptually a complementary indicator to LCOE that effectively assesses the technical-economic performance of a generation project [7]. It is based on the concept of AC, which has been a public policy tool within energy efficiency context in the US, and it was stated under the Public Utilities Regulatory Policies Act (PURPA) in 1978 [8]. At the international level, several energy-related institutions [7,9-12], have estimated AC as alternative indicators that provide appropriate signals for investors and planners. Besides, references [8,13] argue that AC is based on marginal cost of the power system, and its calculation can provide useful cost saving indicators to investors.

Estimating the AC of a generation project is important for

identifying the most promising generation choice [14,15]. Several long-term approaches have been proposed to estimate AC [8,14,15]. One of these approaches is the so-called Differential Revenue Requirement (DRR), which, according to [14], is the most comprehensive. In order to determine the economic and technical effect on the system of a new generation project, the DRR method can be employed. It compares the operational cost of a power system with and without the new generation project.

## 3. Proposed LACE methodology

Our LACE approach of a specific generation project is based on finding measures that capture the potential impacts, either advantages or disadvantages that the project can offer to the power system. Authors strongly believe these impacts have to be obtained by looking at the potential power system operation under different conditions. The goal of our approach is, therefore, to identify whether the project construction can replace other generation resources due to economic or technical reasons. A new generation project can improve either system security under N-1 contingencies, provide firm energy, offer support during peak demand periods, or replace a more expensive generation. Thus, our LACE indicator not only assesses the economic performance of the project, but also captures operational characteristics of the same.

## 4. Power system methodology assessment

The power system assessment is performed employing a Preventive DC SCOPF. The SCOPF is an economic dispatch, which ensures a secure power system operation under N-1 transmission contingencies. The interested reader may consult references [16-18] for additional details. Additionally, authors propose the use of generation scenarios to provide a more effective LACE that takes into account the performance of the project under different system operating points.

In this setup, the SCOPF model returns the estimated annual operational cost  $f_0(\omega)$  of the system under generation scenario  $\omega$ , which is the optimal objective of the following mixed-integer linear optimization problem:

$$f_0(\omega) = \min \sum_{b \in B} \sum_{g \in \Psi} c_g(\omega) \cdot P_{g,b,\omega} \cdot h_b \quad (1)$$

subject to:

$$\sum_{g \in \Psi_i} P_{g,b,\omega} - D_{i,b} = \sum_{l \in L_i^+} f_{l,b}^k - \sum_{l \in L_i^-} f_{l,b}^k, \quad \forall i \in \Phi, \forall k \in K, \forall b \in B \quad (2)$$

$$-K_{ol} \cdot F_l^{Max} \leq f_{l,b}^k \leq K_{ol} \cdot F_l^{Max}, \quad \forall l \in L, \forall k \in K, \forall b \in B \quad (3)$$

$$f_{l,b}^k = \frac{I_{lk} \cdot S_{base}}{X_l} \left( \sum_{i \in L_i^-} \theta_{i,b}^k - \sum_{i \in L_i^+} \theta_{i,b}^k \right), \quad \forall l \in L, \forall k \in K, \forall b \in B \quad (4)$$

$$U_g \cdot P_{g \min} \leq P_{g,b,\omega} \leq U_g \cdot A_{g,b}(\omega) \cdot P_{g \max}, \quad \forall g \in \Psi, \forall b \in B \quad (5)$$

$$-\frac{\pi}{2} \leq \theta_{i,b}^k \leq \frac{\pi}{2}, \quad \forall i \in \Phi, \forall k \in K, \forall b \in B \quad (6)$$

Where:

$\Phi$  : is the set of the power system buses.

$\Psi_i$  : is the set of existing generators connected at bus  $i$ .

$\Psi = \bigcup_{i \in \Phi} \Psi_i$  : is the set of generators.

$L$ : is the set of transmission lines.

$K$  is the set of post-contingency states.

$B$ : is the set of demand blocks. A load duration curve that represents annual demand by a sequence of load blocks is employed. A demand level (peak, medium, minimum) and its corresponding number of hours in a year define each demand block  $b$ .

$h_b$  : is the number of hours per year in which demand block  $b$  occurs.

$C_g(\omega)$ : is the operation cost of each generator in generation scenario  $\omega$ .

$S_{base}$ : base power (100 MVA).

$P_{g,b,\omega}$ : is the power generation dispatched by generator  $g$  during demand block  $b$  when generation scenario  $\omega$  is simulated.

$f_{l,b}^k$  : is the power flow through transmission line  $l$  during demand block  $b$  under contingency state  $k$ .  $k=0$  denotes the pre-contingency or normal condition state.

$L_i^+$  : is the transmission line set that ends at bus  $i$ .

$L_i^-$  : is the transmission line set that starts at bus  $i$ .

$D_{i,b}$  : is the power demand at bus  $i$  in block  $b$ .

$\theta_{i,b}^k$ : is the voltage angle at bus  $i$  in block  $b$  under post-contingency state  $k$ .

$X_l$ : is the electrical impedance of the transmission line  $l$ .

$I_{lk}$ : is the transmission line status parameter; it is 0 if transmission line  $l$  is outaged under contingency  $k$ , or 1 otherwise.

$F_l^{Max}$ : represents the maximum power flow on transmission line  $l$ .

$K_{ol}$  : is a long-term overload factor that is usually defined in the range [1, 1.3] [19].

$U_g$  : is a binary decision variable; it is 1 if generator  $g$  is online, or 0 otherwise.

$A_{g,b}(\omega)$  : represents the power availability factor of each generator  $g$ .  $A_{g,b}(\omega)=1$  for dispatchable generators, and  $A_{g,b}(\omega)<1$  for both intermittent and hydro generators only during dry seasons.

$P_{g \max}$  and  $P_{g \min}$ : are the maximum and minimum operating power limits of each generator, respectively.

Constraint eq. (1) describes the operational cost of the power system. Constraint eq. (2) represents the power

balance constraint under normal and post-contingency operating conditions. Constraint eq. (3) limits power flow on each line under normal and post-contingency operating conditions. Constraint eq. (4) displays the definition of active power flow in terms of voltage angle difference. Constraint eq. (5) shows power output limits of generation. And constraint eq. (6) represents voltage angle limits under normal and post-contingency operating conditions.

## 5. LACE formulations

LACE of a new generation project  $p$ , namely  $LACE_p$ , is defined as the annual cost change ( $\Delta S_p$ ) caused by the project per unit of energy ( $E_p$ ) it can produce during the year. Thus, LACE can be computed as:

$$LACE_p = \frac{\Delta S_p}{E_p} \quad (7)$$

If  $\Delta S_p > 0$ , then it can said that project  $p$  replaces expensive generation. If  $\Delta S_p = 0$ , it can said that the project does not offer any economic or operational advantage.  $\Delta S_p$  is computed as the average cost change caused by project  $p$  with respect to the set of generation scenarios  $\Omega$ . That is,

$$\Delta S_p = \sum_{\omega \in \Omega} w_{\omega} (f_0(\omega) - f_0^p(\omega)) \quad (8)$$

Where  $W_{\omega}$  is the weight associated to generation scenario  $\omega$ . Besides,  $\sum_{\omega \in \Omega} w_{\omega} = 1$ .  $f_0^p(\omega)$  represents the resulting operating cost of the system when the generation set considers the new project  $p$ , i.e., when set  $\Psi$  is changed to  $\Psi^+ = \Psi \cup \{p\}$ . In this work, annual energy produced by each new generation project  $p$  is averaged over the generation scenarios, according to the work of [20], as eq. (9) shows:

$$E_p = \sum_{\omega \in \Omega} w_{\omega} \sum_{b \in B} P_{p,b,\omega}^* \cdot h_b \quad (9)$$

Where  $P_{p,b,\omega}^*$  represents the optimal power dispatched by generation project  $p$  in demand block  $b$  under generation scenario  $\omega$ . Finally, LACE can be computed as:

$$LACE_p = \frac{\sum_{\omega \in \Omega} w_{\omega} \sum_{b \in B} \left( \sum_{g \in \Psi} c_g(\omega) \cdot P_{g,b,\omega}^* - \sum_{g \in \Psi^+} c_g(\omega) \cdot P_{g,b,\omega}^* \right) \cdot h_b}{\sum_{\omega \in \Omega} w_{\omega} \sum_{b \in B} P_{p,b,\omega}^* \cdot h_b} \quad (10)$$

## 6. Net Benefit formulations

Another useful indicator for evaluating generation projects is the Net Benefit (NB). The NB of a project can be calculated by subtraction of investment, operating and administrative costs from the cost savings estimated by avoided costs [13]. According to [7],  $NB_p$  of project  $p$  can be computed as:

$$NB_p = LACE_p - LCOE_p \quad (11)$$

When  $LACE_p > LCOE_p$ , the project is attractive for the planer or investor since its levelized cost savings can cover the levelized cost. Otherwise, the project does not offer attractive features and might not be considered as a real expansion option. In general, the higher  $NB_p$  the better.

## 7. Numerical results

Our goal is to illustrate LACE and NB of diverse generation projects located in Colombia, which are listed in Table 1. Generation technologies like wind, solar photovoltaic, thermal solar, biomass, hydro, coal, gas, and geothermal of different size were considered. Table 1 presents the variable operational cost  $C_p$  of each new generation project  $p$  as well as the connection bus. This data were obtained from [21].

Table 1.  
Data of the new generation technologies

Generation Technology and nominal capacity	$C_p$ USD/MWh	Connected to the bus:
Geothermal Single Flash (GT-SF 50MW)	0.00	Enea 115 kV
Geothermal Binary Cycle (GT-BC 20 MW)	0.00	Enea 115 kV
Wind (WIND 400 MW)	0.00	Cuestecitas 220kV
Wind (WIND 100 MW)	0.00	Cuestecitas 220 kV
Optimized Thermosolar (OTS 50 MW)	0.00	Cuestecitas 220 kV
Non-Optimized Thermosolar (NOTS 50 MW)	0.00	Cuestecitas 220 kV
Solar Photovoltaic (PV 150 MW)	0.00	Cuestecitas 220 kV
Solar Photovoltaic (PV 20 MW)	0.00	Cuestecitas 220 kV
Biomass (BM 20 MW)	39.01	Viterbo 115 kV
Biomass (BM 40 MW)	35.42	Cerrito 115 kV
Hydropower (HD 820 MW),	3.05	Sogamoso 220 kV
Conventional Pulverized Coal (CPC 70 MW)	32.53	Cerromatoso 110kV
Fluidized Bed Pulverized Coal (FBPC 164 MW)	30.06	Tasajero 230kV
Fluidized Bed Pulverized Coal (FBPC 161 MW)	30.06	Tasajero 230kV
Natural Gas Simple Cycle (NGSC 89 MW)	32.53	Termocol 220 kV
Natural Gas Combined Cycle (NGCC 390 MW)	32.53	Tebesa 220 kV

Source: The Authors

The Colombian network employed consists of 1,487 transmission lines and power transformers, 1018 buses, with a total system demand of 9,500 MW, approximately. Currently, hydro-generation represents 69.9 % of the installed capacity and thermal generation about 29.7 % [22].

Given the high dependence on hydro power, Colombian power system performance is extremely sensitive to weather fluctuations. Geographic location makes of Colombia a tropical country with only two weather seasons: rainy and dry [20]. These conditions allow us to construct two extreme scenarios that capture hydro generation variability. Our generation scenario set is  $\Omega=\{H, T\}$ , where  $H$  represents a heavy “hydro” power production scenario (typical during rainy seasons) and  $T$  stands for a heavy “thermal” power production scenario (typical during dry seasons).

Three load blocks were used to model hourly demand variation. These blocks represent peak, medium and minimum demand. According to [23], in Colombia each block is allocated with 2,190 hours/year in peak demand, which occurs during the evening (18:00 h to 0:00 h), 4,745 hours/year in medium demand, which occurs during the daytime (5:00 h to 18:00 h), and 1,825 hours/year in minimum demand (0:00 h to 5:00 h). In order to consider hourly production variability of wind and solar resources, the availability factor  $A_{g,b}(\omega)$  was adjusted accordingly to limit power production in the SCOPF model. The availability  $A_{g,b}(\omega)$  used for photovoltaic projects under scenario  $T$  during peak, medium and minimum demand was 0, 0.8, and 0 respectively; whereas in scenario  $H$ , these factors were 0, 0.1 and 0. In the case of wind projects, availability factors were 0.35, 0.45 and 0.2 for each demand block as previously defined for both scenarios. The optimization model presented in section 4 was implemented in GAMS [24].

From Figure 1 some key elements can be highlighted: 1) coal and biomass-based power technologies display a remarkable LACE component during peak hours and under scenario  $T$  compared to renewable projects. Coal and biomass projects displace the most expensive generation in the north and southwest regions of the country. Moreover, some of coal-based technologies such as Fluidized Bed Pulverized Coal (FBPC) and Conventional Pulverized Coal (CPC) have a considerable LACE during medium demand blocks under scenario  $T$ . 2) Photovoltaic, thermal solar, wind and geothermal projects have a significant LACE under  $T$  scenario and medium demand block (when wind availability is high). The displacement of fossil fuel-based expensive generation during dry season is the reason of these results. On the contrary, LACE caused by these projects is low under the  $H$  scenario given the lower displacement of low-cost hydro generation.

Figure 2 shows results of LACE, LCOE, and NB. LACE is averaged over scenarios  $H$  and  $T$ . LCOE data were taken from [4]. The adopted approach is inspired in the work of [1], which facilitates the incorporation of current policy aspects (taxes, incentives). From Figure 2, it can be seen that the geothermal project GT-SF 50 MW reflects the maximum NB given its high LACE. The high availability factor of this resource, its independence from weather conditions to produce energy, and

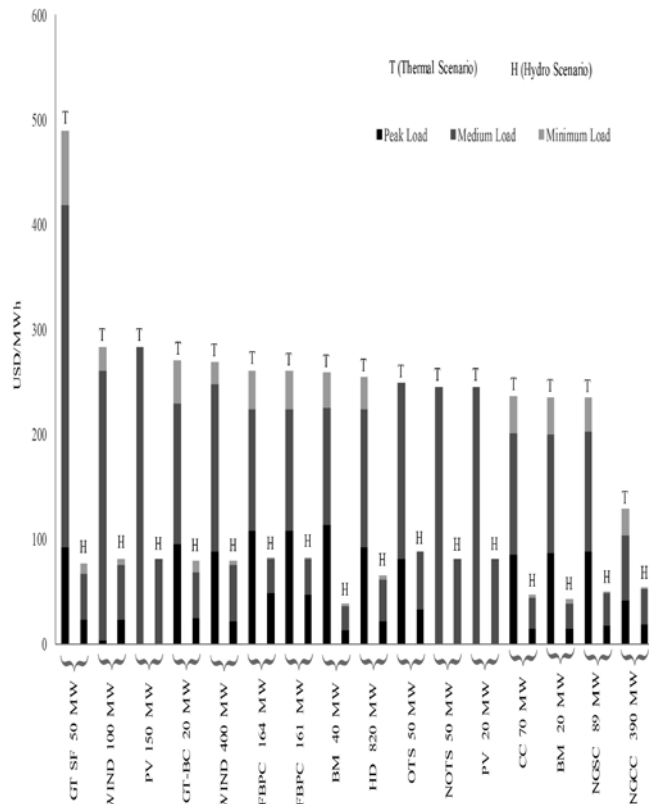


Figure 1. LACE under the different generation and load scenarios  
Source: The authors.

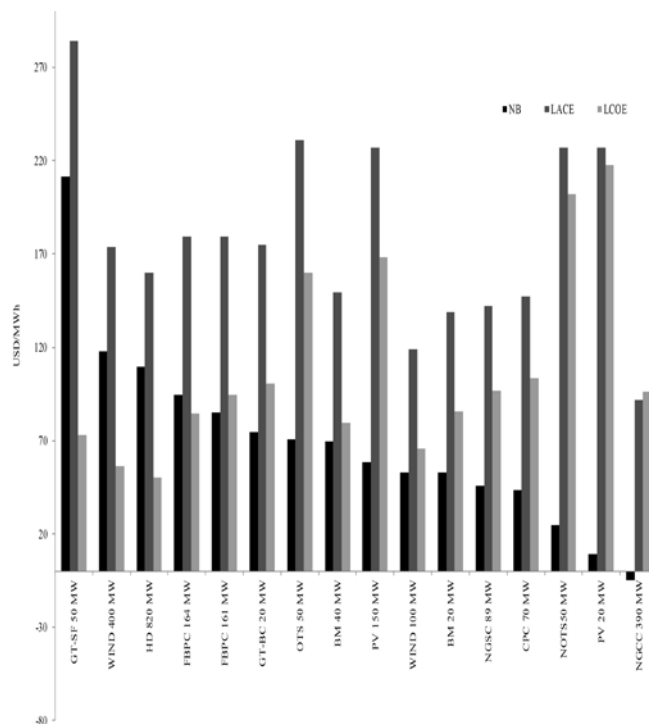


Figure 2. NB, LACE and LCOE of the generation technologies in Colombia  
Source: The authors.

its null production cost are key factors that justify these results. This is finally reflected in significant cost savings. A similar result is observed in the US according to NB analysis performed in reference [7]. Intermittent generation like wind, photovoltaic, and thermal solar have a positive value of NB due to great economic competitiveness under scenario *T*. The project labeled as NGCC 390 MW has a negative NB since its LACE is not as high as its LCOE. This project does not cause any savings under scenario *H* during minimum load periods.

The SCOPF model is useful to detect transmission congestion and security issues due to the occurrence of a specific contingency. In these cases, a specific project, properly located (and not necessarily economic), can improve these security and/or congestion issues. This benefit is ultimately reflected in high LACE. On the contrary, potential operational impact of generation projects on uncongested networks is null. For instance, the installation of the geothermal project GT-SF 50 MW reduced the congestion level on near three-winding transformers under scenario *T* and peak demand block when the outage of other power transformers was analyzed. The economical and operational advantages of this technology is what makes it valuable.

## 8. Conclusions

This work proposed a novel methodology for computing LACE considering operational aspects. LACE is a useful index to estimate the unit cost savings produced by new generation project. Our LACE approach also captures important operational aspects, needed to be considered for making investment decisions, such as system security under N-1 contingencies or generation support during peak demand periods. By using the SCOPF as an evaluation tool, the proposed LACE model identifies differences between the power output profiles of both intermittent and dispatchable generation. The proposed LACE model also allows capturing energy resources geographical dependence as well as electrical network topology. Additionally, the consideration of different generation scenarios provides better LACE results, since different operating points are captured. Through NB, it was also possible to identify those candidate projects that effectively balance savings and cost. This formulation can provide decision and policy makers with additional tools to better design expansion plans and policies. According to our results, most of all the renewable generation projects display high values of LACE and NB, especially geothermal technology (GT-SF 50MW).

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