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Global optimization algorithms applied in a parameter estimation strategy

Algoritmos de optimización global aplicados en una estrategia de estimación de parámetros

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ABSTRACT:

This article presents a comparative study using two global optimization algorithms, Electromagnetic Field Optimization (EFO) and Heat Transfer Search (HTS). These techniques are efficient alternatives when classical methods find limitations to solve real problems. To verify methods performance, the rectangular microchannel heat sink design was implemented formulating the respective Inverse Heat Transfer Problem (IHTP). Experimental results were competitively compared with the traditional Levenberg-Marquardt (LM) outcomes. Moreover, global algorithms achieved estimations with errors lower than 5%, and they converged at least three times faster than LM.

KEYWORDS: Electromagnetic field optimization (EFO), entropy generation minimization (EGM), heat transfer search (HTS), inverse heat transfer problem (IHTP), Levenberg-Marquardt method (LM), ordinary least squares norm (OLSN).

RESUMEN:

Este artículo presenta un estudio comparativo utilizando dos algoritmos de optimización global, el de Optimización por Campo Electromagnético (EFO) y el de Búsqueda por Transferencia de Calor (HTS). Estas técnicas alternativas son eficientes cuando los métodos clásicos encuentran limitaciones para resolver problemas reales. Para verificar el desempeño de los métodos, se implementó el diseño de un disipador de calor de microcanales rectangulares formulando el respectivo problema inverso de transferencia de calor (IHTP). Los resultados experimentales se compararon competitivamente con los resultados tradicionales de Levenberg-Marquardt (LM). Además, los algoritmos globales lograron estimaciones con errores inferiores al 5%, y convergieron al menos tres veces más rápido que LM.

PALABRAS CLAVE: Optimización por campo electromagnético, minimización de la generación de entropía, búsqueda por transferencia de calor, problema inverso de la transferencia de calor, método de Levenberg-Marquardt, norma de los mínimos cuadrados ordinarios.

1. INTRODUCTION

The modern optimization methods allow us to find accurate enough solutions [7], with a wide variety of applications in design problems and the availability of powerful computers [8]. One of these applications is the thermal design through the Inverse Heat Transfer Problem (IHTP), which can be a effective tool in situations where other methods are incapable or inapplicable to find a solution [1, 2, 3]. IHTP is a



methodology that consists of estimating unknown parameters involved in the physical process; it uses the information provided by a given number of measurements profiles, obtained by external sensors, (e.g., temperature or heat flux) [4][6]. One of the most important characteristics of this methodology is that the solution includes not only practical data (i.e., by experimental procedures as direct or indirect measurements) but also theoretical information about the physical process, (i.e., design and modeling) [5], [6]. Generally, this methodology needs to apply an optimization algorithm to minimize some criteria as the Ordinary Least Square Norm (OLSN).

This manuscript presents a comparative numerical study using two modern optimization algorithms, i.e., Electromagnetic Field Optimization (EFO) and Heat Transfer Search (HTS), to tackle Inverse Heat Transfer Problems (IHTPs). As an illustrative example, the parameter estimation of a rectangular microchannel heat sink was analyzed, and the results were compared with the traditional Levenberg-Marquardt (LM). Obtained data showed competitive results against traditional methods. Both methodologies (EFO and HTS) achieved estimations with errors lower than 5%, and they converged at least three times faster than LM.

This document is organized as follows: methodologies are presented in Section 2; experimental results are described in Section 3; and finally, conclusions are discussed in Section 4.

2. METHODS

2.1. Electromagnetic Field Optimization (EFO)

EFO was proposed by Abedinpourshotorban et al. in 2015, as a metaheuristic optimization algorithm inspired on the electromagnets' behavior [21]. The number of design variables defines the number of electromagnets. An electromagnetic particle (Nomp), composed by electromagnets interacting with others, is a candidate solution. Three possible interaction fields, positive, negative and, neutral allow the mentioned interaction. Thus, the attraction and repulsion forces address suitable particles to the global minimal.



```
Require: Objective function f(x) and x_{min} \le x_s \le x_{max}
Set Nemps Pfield Nfield Prates Rrate
Ensure: Best solution to x,
1. Initialize N<sub>emp</sub> and Evaluate f(N<sub>emp</sub>)

 Sort N<sub>emp</sub> from best to worst according to f(N<sub>emp</sub>)

3. Classify into Positive, Negative or Neutral fields
4. if Stopping criteria are satisfied then
            print Best solution x_s \leftarrow N_{emp}(1)
5. else
6. end if
7. Select a random N_{emp}(i) from each field
8. if rand(0, 1) < P_{rate} then
             Set new position as selected electromagnet from positive
9. else
             Set new position by Equation (3)
             Go to 12.
10. end if
12. if i ≤ Electromagnets then
             Go to 8.
13. else
             if rand(0, 1) < R_{rate} then
                          Change from Nemp with a randomly generated
                          N_{emp}(0)
                          Go to 16.
             end if
14. end if
15. Evaluate f(N_{emp}(0))
16. if f(N_{emp}(0)) < f(N_{emp}(end)) then
             Insert N_{emp}(0) into N_{emp}
            Discard worst N<sub>emp</sub>(end)
             Go to 5.
17. else
             Discard (N_{emp}(0))
             Go to 5.
18. end if
```

PSEUDOCODE 1
Electromagnetic Field Optimization (EFO)
Source. Own creation.

EFO Search Process: Optimization process in EFO (see Pseudocode 1) starts generating a random population N_{emp} . The fitness function allows to evaluate the population, which is ordered into the three possible electromagnetic fields. Best particles go to the positive field (P_{field}) where this portion is defined by (1),

$$0.05 \le P_{field} \le 0.10 \tag{1}$$

the worst ones to the negative (N_{field}) . This portion of population is given by (2),

$$0.40 \le N_{field} \le 0.50 \tag{2}$$

The remaining population goes to the neutral field. Then positive and negative random forces appear i.e., attraction or repulsion. A neutral electromagnetic particle is randomly generated to replace the worst particle



of N_{emp} , which is eliminated at each iteration. This particle interacts with the forces and depending on the selected electromagnet polarity; it can be either attracted (to good solution, positive field) or repulsed (from bad solution, negative field). New position of the generated electromagnet is determined by Equation (3),

$$\begin{split} N_{emp}(new,i) &= N_{emp}(neu,k) \\ &+ \left\{ (\varphi r) [N_{emp}(pos,i) \\ &- N_{emp}(neu,k)] \right\} \\ &- \left\{ r [N_{emp}(neg,i) - N_{emp}(neu,k)] \right\} \end{split} \tag{3}$$

where $N_{emp}(new,i)$ is the new electromagnet position for design variable i, k is the neutral field index for an electromagnet randomly generated, pos and neg, the positive and negative field indexes, respectively. Likewise, r is a random value between [0,1] and, φ represents a ratio of the attraction and repulsion forces (given by the golden ratio 1.6180), due to the repulsion force is weaker than attraction in about 5.0 and 10.0%. Finally, some important EFO parameters are P_{rate} , the probability of selecting electromagnets of the generated N_{emp} of the positive field without changing them. Otherwise, R_{rate} is the possibility of changing one electromagnet of the generated N_{emp} by a randomly generated electromagnet. EFO randomness plays an important role in the exploration and exploitation of searching space, promote the diversity and avoids falling in local minima.

TABLE 1
EFO Performance test results (five best parameters combination for Rosenbrock function)

Rrate	Prate	Pfield	Nield	Nemp	$f(x^*)$ (10 ⁻²)	i	t (s) (10 ⁻²)
_		_	_		$\mu \pm \sigma$	$\mu \pm \sigma$	$\mu \pm \sigma$
0.40	0.40	0.10	0.40	100	1.27± 1.62	543.4± 263.9	8.86± 6.33
0.30	0.10	0.05	0.40	100	3.10 <u>+</u> 4.86	464.4 <u>+</u> 334.1	4.38 <u>+</u> 2.19
0.40	0.30	0.05	0.40	50	4.97 <u>+</u> 5.86	304.6 <u>+</u> 113.8	3.91 <u>±</u> 1.13
0.20	0.10	0.05	0.50	150	6.50 <u>+</u> 5.68	218.6± 52.93	3.00 <u>±</u> 0.73
0.10	0.20	0.10	0.50	100	9.44 <u>+</u> 7.20	262.0± 90.60	3.75± 1.55

Source. Own creation.

TABLE 2 Control parameters for EFO

Method	Parameter	Possible values		Selected
		Min	Max	values
	N_{emp}	50.0	Dim	100
	P_{field}	0.05	0.10	0.10
EFO	N_{field}	0.40	0.50	0.40
	Prate	0.10	0.40	0.40
	R_{rate}	0.10	0.40	0.40

Source. Own creation.



In Table 2, Dim represents the design variables number of the problem. If this number is less than 50, the N_{emp} to choose must be 50, on the contrary N_{emp} must be equal to the design variables number.

2.2. Heat Transfer Search (HTS)

It is a metaheuristic optimization algorithm proposed by Patel and Savsani in 2015 [22]. HTS is inspired by the fundamental thermodynamics laws, where the searching agents emulate systems interacting with other systems, and their surrounding environment exchanging energy. HTS aims at reaching the thermal equilibrium, and interactions of the systems are made of the three different heat transfer mechanisms: conduction, convection, and radiation. HTS is based on the following statement: "any system tries to reach the equilibrium with itself and its surrounding".

```
Require: Objective function f(x) and x_{min} \le x_s \le x_{max},
Set N<sub>mob</sub> Cd<sub>factor</sub>, CV<sub>factor</sub>, Rd<sub>factor</sub>
Ensure: Best solution to x_s

    Initialize N<sub>mol</sub> and Evaluate f(N<sub>mol</sub>)

Generate randomly R
3. if 0.0000 \le R \le 0.3333 then
            if Iteration < (G_{max}/Cd_{factor}) then
                        Select a solution randomly and modify by
                        Equation (5)
                        Select a solution randomly and modify by
                        Equation (6)
            end if
                        Go to 7.
4. else
            if 0.3333 < R < 0.6667 then
                        if Iteration < (G_{max}/Rd_{factor}) then
                                    Select a solution randomly and
                                    modify by Equation (10)
                        else
                                    Select a solution randomly and
                                    modify by Equation (11)
            end if
            Go to 7.
            else
                        Select the best solution
                        Calculate COS by Equation (8)
                        Modify solutions according to best solution
            by
                        Equation (7)
                        Go to 7.
            end if
5. end if
6. if f(new solution) < f(best solution) then
            best solution ← new solution
7. else
            best solution ← best solution
9. Replace worst solution with current solution
10. Modify duplicate solutions
11. if Stopping criteria are satisfied then
           print Best solution x_s \leftarrow N_{mol}(iteration)
            Go to 3
13. end if
```

PSEUDOCODE 2
Heat Transfer Search (HTS)
Source. Own creation.

HTS Search Process: Its process begins (see Pseudocode 2) generating a random population (N_{mol}) which is evaluated by a fitness function. If an improvement exists, the population is updated (until G_{max}). This updated can be done through three steps such as conduction, radiation, and convection (sequence steps are empirically



serialized). Each one of these steps has the same probability and, to ensure an exploration and exploitation balance, the variable R is used. R is a random number with a uniform distribution between [0,1]; each step is linked with R as shown in Equation (4),

$$\begin{array}{ll} for\ conduction & 0.00 \leq R \leq 0.33 \\ for\ radiation & 0.33 < R \leq 0.67 \\ for\ convection & 0.67 < R \leq 1.00 \end{array} \tag{4}$$

once R is generated randolmly; depending on its value, each step works as follows:

2.2.1. Conduction step

The Equations (5) and (6) for this step are inspired by the Fourier law. If $iteration \le (G_{max}/cd_{factor})$,

$$N_{mol}(new, z) = N_{mol}(old, \overline{z}) - R^2 N_{mol}(old, \overline{z})$$

$$for z = \begin{cases} j & \text{if } f(N_{mol}(j)) > f(N_{mol}(k)) \\ k & \text{if } f(N_{mol}(k)) > f(N_{mol}(j)) \end{cases}$$
(5)

where j=1,2,3,...,n, since n is the maximum number of molecules and k is a randomly select solution from N_{mol} . The typical value for Cd_{factor} is 2. By the way, if $iteration > (G_{max}/Cd_{factor})$,

$$N_{mol}(new, z) = N_{mol}(old, \overline{z}) - r_i N_{mol}(old, \overline{z})$$

$$for z = \begin{cases} j & \text{if } f(N_{mol}(j)) > f(N_{mol}(k)) \\ k & \text{if } f(N_{mol}(k)) > f(N_{mol}(j)) \end{cases}$$
(6)

where r_i is a random number uniformly distributed in [0,1].

2.2.2. Convection step

The Equations (7) and (8) are inspired by Newton law,

$$N_{mol}(new, j) = N_{mol}(old, j) + COS$$
(7)

$$COS = R\{N_{mol}(s) - TCF[N_{mol}(ms)]\}$$
(8)

where index # represents the surrondings temperature and ## the mean system temperature, and *cos* is the convection stride. *TcF* is the temperature change factor given by (9),



$$TCF = \begin{cases} |(R - r_i)| & \text{if iteration} \le (G_{max}/Cv_{factor}) \\ |(1 + r_i)| & \text{if iteration} > (G_{max}/Cv_{factor}) \end{cases}$$
(9)

Extensive experimental trials shown that $c_{v_{factor}}$ has a typical value of 10.

2.2.3. Radiation step

Inspired by Stefan-Boltzmann law, it is described by Equations (10) and (11). After many trials, typical value of Rd_{factor} is 2. Otherwise, if $iteration \leq (G_{max}/Rd_{factor})$

$$\begin{split} \textit{N}_{mol}(\textit{new}, \textit{j}) &= \textit{N}_{mol}(\textit{old}, \textit{j}) \\ &- zR[\textit{N}_{mol}(\textit{old}, \textit{k}) - \textit{N}_{mol}(\textit{old}, \textit{j})] \end{split}$$

$$for \ z = \begin{cases} +1 \ if \ f(\textit{N}_{mol}(\textit{j})) > f(\textit{N}_{mol}(\textit{k})) \\ -1 \ if \ f(\textit{N}_{mol}(\textit{k})) > f(\textit{N}_{mol}(\textit{j})) \end{cases} \tag{10}$$

now, if iteration > (G_{max}/Rd_{factor}) ,

$$\begin{split} N_{mol}(new,j) &= N_{mol}(old,j) \\ &-zr_i[N_{mol}(old,k) - N_{mol}(old,j)] \end{split}$$

$$for \ z = \begin{cases} +1 \ if \ f(N_{mol}(j)) > f(N_{mol}(k)) \\ -1 \ if \ f(N_{mol}(k)) > f(N_{mol}(j)) \end{cases} \tag{11}$$

Equations (4) and (11) permit to calculate molecules new position to HTS algorithm for each step.

TABLE 3
HTS Performance test results (five best parameters combination for Rosenbrock function)

ъ С	ځ	Rd	N	f(x*) (10 ⁻⁵)	i	t (s)
_	S.T. 75.		~	$\mu \pm \sigma$	$\mu \pm \sigma$	μ±σ
2.0	10	2.0	50	4.17 <u>+</u> 4.94	160.4± 36.58	1.05± 0.24
1.5	10	2.0	50	14.5 <u>+</u> 16.97	169.4 <u>+</u> 25.14	1.09 <u>+</u> 0.16
1.0	10	1.5	200	18.23 <u>+</u> 14.07	193.4 <u>+</u> 89.34	1.84 <u>+</u> 0.83
2.0	1.0	2.0	150	21.17± 17.91	175.2± 19.23	1.14 <u>+</u> 0.12
2.0	5.0	1.0	100	45.87 <u>+</u> 62.27	169.8± 61.15	1.11± 0.40

Source. Own creation.



TABLE 4 Control parameters for HTS

Method	Parameter	Pos va	Selected	
		Min	Max	values
	N_{mol}	10.0	2500	50.0
TITTO	Cd_{factor}	1.00	2.00	2.00
HTS	Cv_{factor}	1.00	10.0	10.0
	Rd_{factor}	1.00	2.00	2.00

Source. Own creation.

In Table 1 and Table 3, i represents the required iterations to converge. Similarly, those tables show the results from performance tests on Rosenbrock function to determine the best combination of parameters to ensure the convergence of the algorithms. x^* represents the optimal value from Rosenbrock function, in this case $x^* = [1.00, 1.00, 1.00, 1.00, \dots, 1.00]$, From these tests, the configuration parameters were selected.

2.3. Rectangular Micro-Channel Heat Sink Model

The used model for a Rectangular Micro-Channel Heat Sink was studied by Cruz et al. [19]. The Equation (12) describes the total entropy generation rate \$\sigma_{gen}[WK]\$ in the RMCHS model,

$$\dot{S}_{gen} = \frac{\dot{Q}_d^2}{T_a T_i} R_{eq} + \frac{G_d}{T_a} \Delta P \tag{12}$$

Where $\dot{\varrho}_{a}[w]$ is the heat power dissipated by the electronic device, $R_{eq}[K/W]$ is the equivalent thermal resistance, $T_{a}[K]$ and $T_{i}[K]$ are the surrounding and interface temperatures, respectively, $G_{a}[m^{2}/s]$ is the volume flow rate, and $\Delta P[Pa]$ is the total pressure drop. Geometrical characteristics, material and fluid type are the design variables. The geometrical ones are,

$$\alpha_c = \frac{W_c}{H_c} \tag{13}$$

$$\beta = \frac{W_c}{W_p} \tag{14}$$

where $w_{e}[m]$ represents the channel width, $H_{e}[m]$ the channel height, and $w_{e}[m]$ the wall width.

2.4. Inverse Heat Transfer Problem

This methodology has four different techniques to solve inverse problems. Levenberg-Marquardt (LM) [20], is the main method used for solving IP parameters estimation in the Technique I, according to Ozisik et al. [6]. The current inverse problem can be solved via the Technique I, which is composed of five



phases depicted in Figure 1. Once the direct and inverse problem statements are mathematically defined, an efficient optimization method is proposed to minimize the Ordinary Least Squares Norm (OLSN) using the measurements profile and the process model. The procedure iterates to converge until the stopping criteria are fulfilled. The phases sequence concludes with a computational algorithm, which wraps the previous phases to obtain the complete and particular IP solution.

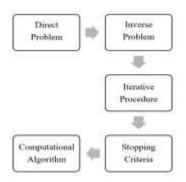


FIGURE 1
Inverse Heat Transfer Problem methodology scheme
Source. Own creation.

The direct problem (DP) requires to minimize the entropy generation of a RMCHS. The other variables are assumed as known with an adequate precision degree. The DP uses as design variables a set of parameters related to the device geometry and, it is mathematically expressed by Equation (15),

$$\begin{split} \min_{\{\theta_D\}} \{\dot{S}_{gen}\} &= \min_{\{\theta_D\}} \left\{ \frac{\dot{Q}_d^2}{T_a T_i(\theta_D)} R_{eq}(\theta_D) + \frac{G_d}{T_a} \Delta P(\theta_D) \right\} \\ & subject \ to \ \begin{cases} g_1 &= \frac{W_c}{H_c} - 1 \leq 0 \\ g_2 &= 1 - \frac{W_c}{W_p} \leq 0 \end{cases} \end{split} \tag{15}$$

where $\theta_D = (\alpha_c, \beta)^T$ and T means the transposed vector.

The inverse problem (IP) requires to estimate the parameters of a RMCHS, which produce the minimal entropy generation. The other variables are assumed as known with an adequate precision degree. Additional data are τ_i (given by an external sensor), as a function of G_{ad} . For all set of parameters linked to the RMCHS geometry, the IP formulation based on the OLSN is shown in Equation (16),

$$\min_{(\theta_I)} \{S(\mathbf{P})\} = \min_{(\theta_I)} \left\{ \sum_{i=1}^{M} \left[T_i \left(G_d(i) \right) - \hat{T}_i(\mathbf{P}, G_d(i)) \right]^2 \right\}$$

$$subject \ to \begin{cases} g_1 = \frac{W_c}{H_c} - 1 \le 0 \\ g_2 = 1 - \frac{W_c}{W_p} \le 0 \end{cases}$$
(16)

where θ_i is $(\alpha_c, \beta)^T$.

The fundamental element of the iterative procedure to get a reliable solution, through the recurrent minimization of the OLSN is formally expressed by Equation (17),



$$S(\mathbf{P}) = \sum_{i=1}^{M} \left[T_i \left(G_d(i) \right) - \hat{T}_i(\mathbf{P}, G_d(i)) \right]^2$$
(17)

where # represents the squared errors sum, and $T_i(G_d(i))$ gives the measured temperature in the interface between the electronic device and the heat sink. T_i is recurrently measured by a sensor for different values of G_d . Likewise, P_i is the unknown parameters vector, which is defined as $P = (P_1, P_2, P_3, ..., P_N)^T$. $\hat{T}_i(P_i, G_d(i))$ is the estimated temperature by using the RMCHS model that is updated according to current parameters at each iteration i. N represents the number of unknown parameters, and M is the number of measurements. The condition, $M \ge N$, guarantees an adequate estimation. In the experiments, this condition is valid because of the maximum number of parameters is set to two (N = 2), and the number of measurements is one hundred (M = 100). The minimization is achieved by means of the evaluation of two recent optimization algorithms: the Electromagnetic Field Optimization (EFO) and the Heat Transfer Search (HTS), which substitute the traditional LM method.

The first criterion (Equation (18)) is the saturation condition (also known as stagnation state). The second one (Equation (19)), shows the criterion based on the statistical treatment of solution. μ and σ are the mean and the standard deviation of the solutions from the objective function. The tolerance value δ must be defined by the user. In our experiments, this value was defined as 1.0, arbitrarily.

$$m_{sat} \le M_{max} \wedge f(\mathbf{P}^{i+1}) = f(\mathbf{P}^i)$$
 (18)

$$|f(\mathbf{P}^i) - \mu| < \delta\sigma \tag{19}$$

The serial and the parallel strategies are proposed to look for reliable results in heat sink parameters estimation. For the former (Serial Strategy), the tests were performed (its sequence depends on the model variable influence, starting with the most sensitive). The test estimates a couple of geometric characteristics parameters (α_c , β). For the latter, the Parallel Strategy, also known as multiparametric, the geometric parameters (α_c , β) are simultaneously estimated. In the experiments, the design variables are: the channel aspect ratio α_c , width ratio of channel to pitch β . Additionally, some constraints are included to ensure algorithmic convergence. Therefore, main searching space is detailed in Equation (20).

$$\begin{array}{c} 1.0(10^{-3}) \leq \alpha_c \leq 10(10^{-3}) \\ 1.0 \leq \beta \leq 5.0 \\ 0.1(10^{-3})[m^3/s] \leq G_d \leq 10(10^{-3})[m^3/s] \end{array} \tag{20}$$

Reference values to the thermophysical and geometric variables are shown in Table 5. The number of chosen repetitions (Rep) is 50, with a maximum number of iterations (M_{max}) predefined at 100000. For evaluation purposes, synthetic data were contaminated with additive white gaussian noise (AWGN) at ten different levels of signal-to-noise ratio, $10 \text{ dB} \leq \text{SNR} \leq 100 \text{ dB}$.



TABLE 5
Reference and average values for thermophysical properties to aluminum and air

Parameter	Reference value
α_c	3.61(10-3)
β	2.074
S _{gen}	379(10-3)
G_d	5.45(10-3)

Source. Own creation.

3. EXPERIMENTAL RESULTS

A desktop iMac, Processor Intel CoreTM i5 @ 2.7-3.2 GHz, 8 GB RAM @ 1600 MHz, 64 bit with macOS Sierra was used for the experimental procedures. Table 2 and Table 3 presents the representative control parameters values used in the experiment. These data show the typical value and warranted range to obtain a fast convergence. Selected values experimentally determined from the performance output from a testing study using ten different standard benchmark functions (See Table 1, Table 3 and, Table 6).

TABLE 6
Standard benchmark functions and tested dimensions

Function	Dimensions
Ackley	2, 5, 10
Bird	2
Bukin #6	2
Carrom Table	2
Chichinadze	2
Goldstein-Price	2
Helical Valley	2
Plateau	2, 5, 10
Rosenbrock	2, 5, 10
Test Tube Holder	2

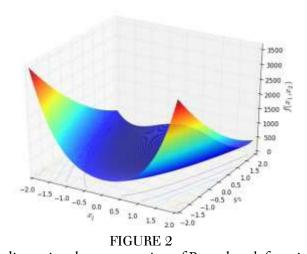
Source. Own creation.

The results on the Rosenbrock function (21) are shown as examples of the algorithms performances.

$$f(\mathbf{x}) = \sum_{i=1}^{n-1} [100(x_i^2 - x_{i+1})^2 + (x_i - 1)^2]$$
(21)

- Searching domain: $x_i \in [-5.00, 5.00]$ for i = 1, 2, 3, ..., n.
- Global optimum: $f(x_i) = 0.00$ for $x_i = [1.00, 1.00, 1.00, ..., 1.00]$ when i = 1, 2, 3, ..., n
- Dimensions: n.





Three-dimensional representation of Rosenbrock function
Source. Own creation.

3.1. Performance test

The convergence of the algorithms was tested with the standard benchmark functions. Figure 3 and Figure 4 show the convergence of EFO and HTS, respectively.

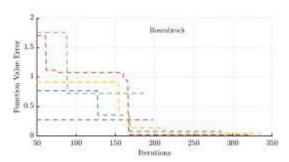


FIGURE 3 EFO algorithm convergence Source. Own creation.

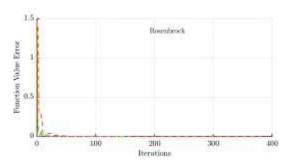


FIGURE 4 HTS algorithm convergence Source. Own creation.



3.2. Total entropy generation rate estimation

The estimation of the total entropy generation rate (\hat{s}_{gen} that was obtained compiling the individual parameters estimations. Therefore, Figure 5 shows that estimation to EFO and HTS algorithms for 50 dB of SNR. Before 0.4 of G_d , the estimation error was fewer than 1.00%, it was a reiterative result for all the SNR levels. The cause of that result is due to the RMCHS model depends on conduction and convection heat transfer mechanisms. The convection mode is directly related to the G_d value, when this value is near to zero, the conduction mode takes over the process and the heat transfer is almost constant because of the material body heat sink nature. Conduction mode is independent of the work substance quantity flowing through the heat sink microchannels. In this part, the estimation process can be achieved without clear complications. But the estimation in that part is not relevant because the optimal points are in another zone. Once the G_d value increases both heat transfer modes are present and the high non-linearity is more remarkable. Thus, the estimation process shows differences regard to the reference values.

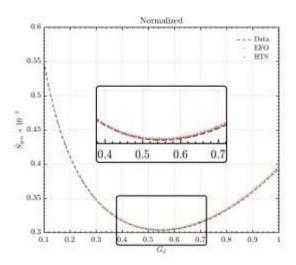


FIGURE 5
Estimation of ##### (Normalized) with reference value to 50 dB of SNR
Source. Own creation.

Besides, the process was observed stable to SNR greater than 30 dB. However, estimations from EFO algorithm had relative errors of at least 112%, with quantities of noise between 10 and 20 dB, this is mainly due to high noise levels.

Estimated relative errors (ϵ_r) were inferior to 5.00% when SNR is equals 50 dB. Relative errors was calculated by (22),

$$\epsilon_r = \frac{Value_{theoretical} - Value_{practical}}{Value_{theoretical}} \times 100$$
(22)

3.3. Comparative serial and parallel strategies

For inverse problems, the multi-parametric optimization is the common strategy when it is required to estimate a high quantity of parameters. Thus, the parameters estimation is made in simultaneous (or parallel), decreasing the processing time, and affecting some other parameters. However, the precision is one of the



most important characteristics to be considered, i.e., it is a decisive variable between the serial strategy (above analyzed) and the multi-parametric (parallel strategy). Table 7 shows a comparison between serial and parallel strategies for each parameter. Both, EFO and HTS working in serial strategy reached estimations with relative errors smaller than 5.50% (5.47% with HTS for k_f) for the majority of parameters. For three over eight parameters (α_c , β , and ρ_m), the parallel strategy with EFO, produces errors between 5.50% and 11.5%. Contrarily, HTS with the same parallel strategy gives relative errors in the interval of 1.00% and 28.0%. The smallest errors were obtained for ρ_f , ν , and ϵ_p independently of the chosen strategy or algorithm. Statistical analysis exhibits that standard deviations are bigger in the parallel than in the serial strategy. In other words, the reliability of a solution increases by using the serial strategy.

TABLE 7
Relative errors (#r%) for serial and parallel strategies for the estimation of ##, # at 50 dB of SNR

		Stra	tegy	-100-gen 100
	Sei	rial	Parallel	
	EFO	HTS	EFO	HTS
α_c	4.58	4.89	5.66	27.9
β	3.41	3.97	8.65	2.14

Source. Own creation.

3.4. Comparative with other Non-traditional Algorithms

For comparative purposes, similar reference patterns are used to evaluate selected methods with well-known nontraditional optimization algorithms (i.e., Unified Particle Swarm Optimization (UPSO), Simulated Annealing (SA) and Spiral Optimization (SO)). This comparison is fundamental to detect particular features of each algorithm. The experimental analysis showed that EFO gave the best results, HTS followed it for each G_d value. Figure 6 show a comparison of relative errors of the entropy generation rate estimation at 50 dB. Therefore, EFO and HTS had best relative errors, their processing times are lower than others.

3.5. Comparative with the Traditional Algorithm

The Figure 7 presents a comparative analysis between proposed and the traditional method, which was used to estimate the unknown parameters. Results obtained from Levenberg-Marquardt method were taken as a reference to evaluate EFO and HTS results.



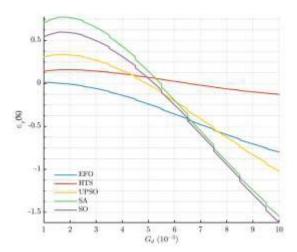


FIGURE 6
Relative errors comparative with non-traditional algorithms against reference value of ## ### for each ## value at 50 dB of SNR Source. Own creation.

Experiences show that LM obtains better estimations over studied methods, but differences between them are inferior to 3.50% (e.g., for β parameter using HTS). However, selected algorithms were at least three times faster than LM. The estimation precision is similar for the three compared algorithms. EFO and HTS utilized a number of iterations inferior to LM; and consequently, the number evaluations associated with the objective function is also inferior.

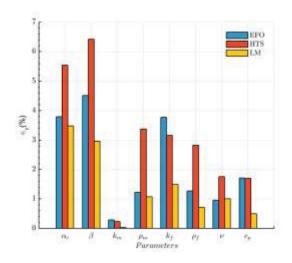


FIGURE 7 Comparison of relative errors of ##### estimation between EFO, HTS and LM at 50 db of SNR for each parameter Source. Own creation.

4. CONCLUSIONS

This paper presented a comparative numerical study using two modern optimization algorithms, i.e., Electromagnetic Field Optimization (EFO) and Heat Transfer Search (HTS), to tackle Inverse Heat Transfer Problems (IHTPs). As an illustrative example, the parameter estimation of a rectangular



microchannel heat sink was analyzed, and the results were compared with the traditional Levenberg-Marquardt (LM) method. Additionally, two estimation strategies were studied: serial and parallel. Obtained data showed competitive results against traditional methods. Both methodologies (EFO and HTS) achieved estimations with errors lower than 5%, and they converged at least three times faster than LM. It was found that EFO is seven times faster than HTS. Furthermore, several differences among the two estimation strategies were noticed, i.e., parallel strategy was almost three times faster and had greater errors (between 0.10% and 5.5%) than the serial one. Specifically, the parallel strategy implemented with EFO showed smaller errors than using HTS. Moreover, the methodologies implemented in this work were compared with commonly used optimization algorithms, such as Simulated Annealing (SA), Unified Particle Swarm Optimization (UPSO) and Spiral Optimization (SO). This comparative study gave us negligible differences between their relative errors, but EFO and HTS spent at least half of time than the required by SA, UPSO and SO.

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ADDITIONAL INFORMATION

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