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A STUDY OF THE SX PHE STAR BL CAM¹

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ABSTRACT

We determined the physical parameters of the SX Phe star BL Cam from newly available times of maximum light and other times from the literature, as well as from *uvby* – β photoelectric photometry. From our analysis we found that this star is a binary system. The mass of the companion star was calculated in term of the mass of the primary star and the orbital angle. For this star we determined a metallicity [Fe/H] of -1.2 ± 0.3 .

RESUMEN

Determinamos los parámetros físicos de la estrella tipo SX Phe BL Cam a partir de nuevos tiempos de máximo observados y otros de la literatura, así como de fotometría fotoeléctrica *uvby* – β . Con nuestro análisis encontramos que esta estrella es un sistema binario. Calculamos la masa de la estrella compañera en términos de la masa de la estrella primaria y el ángulo orbital. Para esta estrella hemos determinado una composición química [Fe/H] de -1.2 ± 0.3 .

Key Words: binaries: eclipsing — stars: individual: BL Cam — stars: variables: Scuti

1. INTRODUCTION

In their article on BL Cam and DY Peg, two SX Phe stars, Blake et al. (2000) reported that Hintz et al. (1997) on studying the rate of period change for BL Cam found that over an observational baseline of 30 years, BL Cam had exhibited a steady period change with no sudden jumps. However, they found that the light curve of BL Cam was exhibiting periodic amplitude variations of up to 0.2 magnitude. Such behavior was unexpected and had not been previously reported.

The most recent study of BL Cam (= 2MASS J03471987+6322422, Gaia DR2 487276688415703040, GD 428 in Simbad) is that of Zong et al. (2019) with observations from 2014 to 2018. They determined that the period content of BL Cam was dominated by a frequency of 25.5790 (3) c/d and its two harmonics, plus an independent frequency of 25.247 (2) c/d, a non-radial mode

frequency detected from the data in 2014. With a O–C analysis of their times of maxima from the literature they determined a periodic change which, if caused by the light-time travel effect (LTTE), made BL Cam a binary system. Besides, they did not find evidence of the triple system suggested by previous authors.

We must remark that despite high quality space missions like TESS and the analysis of their data on A–F stars (Antoci et al. 2019), observational programs that have enough time series data to study the rate of period change must be developed, which is a task not possible to perform with TESS observations.

The Observatorio Astronómico Nacional de Tonantzintla (TNT) finds itself in an analogous situation to that described by Blake et al. (2000) referring to York University Observatory, since they are both located near large metropolitan areas. This restricts the types of research projects that can be conducted to those not requiring absolute photometry. Given the occasional large gaps in observational coverage of HADS and SX Phoenicis stars that have hindered the study of their period changes for several years, we have carried out a long-term monitoring program for such variables. Here we report our observations of BL Cam obtained as part of this program conducted by the staff and students of the Observational As-

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TABLE 1
LOG OF OBSERVING SEASONS AND NEW TIMES OF MAXIMA OF BL CAM

Date yr/month/day	Observers/Reducers	Npoints	Time span day	Nmax	Tmax (HJD-2458000) day	Observatory
20/01/1112	hh,ESAOBELA20/hh,jdp	122	0.0960	3	860.7052 860.7448 860.7842	TNT
20/01/1213	hh,ESAOBELA20/hh,jdp	162	0.1396	3	861.7247 861.7641 861.8022	TNT
20/01/1314	hh,ESAOBELA20/hh,jdp	116	0.0880	3	862.7415 862.7804 862.8204	TNT
20/01/1415	hh,ESAOBELA20/hh,jdp	151	0.1230	3	863.7182 863.7599 863.7959	TNT
20/01/1617	hh,ESAOBELA20/hh,jdp	117	0.0906	2	865.7510 865.7905	TNT
20/01/1718	hh,ESAOBELA20/hh,jdp	146	0.1187	2	866.7287 866.7684	TNT
20/02/2425	dsp/dsp,jdp	40	0.0819	2	904.6927 904.7318	SPM

Notes: dsp, Piña D. S.; hh, Huepa H.; jdp Paredes, J. D.; ESAOBELA20: Carrasco, L.; Vargas, C., Martínez, G., Castellanos, M., Mejía, N., Buenfil, G., Vásquez, F., Martínez, B., León, A., Beato, M. & Paredes, J. D.

tronomy courses of the National University of Mexico at TNT. These observations have been supported with $uvby - \beta$ photometry from the Observatorio Astronómico Nacional de San Pedro Mártir (SPM), México.

The purpose the present paper is to describe the procedure to acquire the new times of maximum, observations and reduction. With the new times of maximum and those found in the literature we analyzed them with an $O-C$ procedure. The residuals derived utilizing the ephemerides values of Zhou et al. (1999) are congruent with a physical explanation, and suggested a periodic function, so we analyzed them with Period04. This package provided the orbital parameters assuming a binary system. The physical parameters are determined from $uvby - \beta$ photoelectric photometry and the unreddening procedure of Nissen (1988). The unreddened values were compared with the grids of Castelli & Kurucz (2006).

A brief summary of the contents of each section is the following: a description of the observations and data reduction is presented; period determination was done by the $O-C$ procedure studying the proposed ephemerides. Our conclusion is that the star behaviour is explained if we assume a binary system, and so we determined the orbital elements and mass of the companion star; to conclude, we de-

termined from $uvby - \beta$ photometry, its metallicity, surface gravity and effective temperature.

2. OBSERVATIONS AND DATA REDUCTION

Although some of the times of maximum light of this star have been reported elsewhere (Peña et al., 2021), here we present new times of maxima and the procedure followed to acquire the data. The observations were done at both the Observatorio Astronómico Nacional of San Pedro Mártir and Tonantzinla, in México. Table 1 presents the log of observations, as well as the new times of maximum light.

A 10-inch Meade telescope equipped with an Andor Apogee CCD camera was utilized at the TNT Observatory. There were around 11,000 counts with an integration time of 1 min, enough to secure high precision. The reduction work was done with AstroImageJ (Collins & Kielkopf 2013) Period determination. This software is relatively easy to use and besides being free, it works satisfactorily on the most common computing platforms. For the CCD photometry two reference stars were utilized in a differential photometry mode. The results were obtained from the difference $V_{\text{variable}} - V_{\text{reference}}$ and the scatter was calculated from the difference $V_{\text{reference1}} - V_{\text{reference2}}$. Light curves were also obtained. The new times of maximum light are listed in Table 1.

TABLE 2
COMPILATION OF THE LITERATURE

Reference	T_0	Period (day)	A	σ
Berg77	2,443,125.80476	0.0390883		
McNamara78	2,443,125.8048	0.03909760		0.0011
Hintz97	2,443,125.8042	0.03909773	6.153×10^{-13}	0.00068
Zhou99	2,443,125.8041	0.03909771	3.5728×10^{-13}	0.0013
Conidis13	2,443,125.8026	0.039097911	2.86×10^{-13}	0.0045
Zong19	2,443,125.7748	0.0390980385	-2×10^{-13}	0.0015

Notes. Berg77: Berg & Duthier (1977); McNamara78: McNamara & Feltz (1978); Hintz97: Hintz et al. (1997); Zhou99: Zhou et al. (1999); Conidis13: Conidis & Delaney (2013); Zong19: Zong et al. (2019).

Notes: Compilation of the literature that presented ephemerides equations with the data available during their analysis.

3. O–C ANALYSIS

3.1. O–C

Before calculating the coefficients of the ephemeris equation, we studied the existing literature related to BL Cam. Several authors have carried out studies of the O–C behavior of this particular object and developed models. When these models were constructed, they were built with the data available to them based on the length of their observation time. However, they often differ in the interpretation of the data.

Hintz et al. (1997) presented a thorough study of this star concluding that BL Cam is a double-mode variable with a primary period of 0.0391 day, with evidence that the fundamental period had increased by 0.009 s in the previous 20 years. Their determined variation differs from that of McNamara and Feltz (1978) who proposed a linear variation. They found that the best fit to the data was given by equation (1), and concluded that the period had changed by 0.009 s in the last 20 years:

$$HJD_{max} = 2443125.8048 + 0.03909760(E). \quad (1)$$

It was Hintz et al. (1997) who decided that this star had an increasing period and Blake et al. (2000) corroborated this assertion. Using their observations those authors proposed that the amplitude of the star's light curve is modulated and that the physical cause may be tied to the fact that the star is known to exhibit the features of double-mode pulsation. However, works such as Wolf et al. (2002) could not confirm the results of Hintz et al. (2000) implying that the star had a constant increasing pulsational period. Their conclusion, as expected, was that this star deserved continuous monitoring. One year later Kim et al. (2003) found that the parabolic period variation had recently reversed.

In view of the discrepancies among the different authors, we did a follow-up of the literature that con-

tained ephemerides equations with the data available at that epoch. Most of the ephemerides equations have been calculated utilizing equation 2, in which P is the period, in days; β is the rate of the variation; Z , is the zero point; B is the amplitude; Ω , the frequency and α , the phase. These ephemerides elements are presented in Table 2.

$$HJD_{max} = T_0 + PE + \frac{1}{2}\beta E^2 + Z + \sum_{i=1}^n B_i \sin [2\pi (\omega_i E + \alpha_i)] \quad (2)$$

with $A = \frac{1}{2}\beta$.

In Table 3, we list the author and the year of publication in Column one, Columns two and three show the initial and final dates of the data they analyzed, Column four shows the time span they considered, in years; the next column shows the number of points in their analysis consisting of the points they obtained combined with those of the literature at that time; the last column lists the number of points each author observed. The behavior of their O–C analysis is shown schematically in Figure 1.

For our analysis we collected a total of 520 times of maximum light from the literature and our observations. To these data we added those of VizieR to get 1985 data points, some of which were duplicated. Removing these repeated values, we got a total of 1606 data points. The elapsed time of observations is from 2443125.8046 to 2458904.7320 for a time span of 15778 days, or forty-three years, a considerable length of time.

The starting point for our O–C analysis was that provided by Zhou et al. (1999), who utilized the ephemerides listed in equation 1 proposed by McNamara et al. (1978). As a first stage, we reproduced what Zhou et al. (1999) obtained in their O–C resid-

TABLE 3
CHRONOLOGY OF THE COMPILATION

Reference	(HJD - 2400000) _{Initial}	(HJD - 2400000) _{final}	Δt (years)	$N(T_{max})$	$N(\text{observed})$
Hintz97	43125.8046	50151.7268	19	69	39
Zhou99	43125.8046	50447.1520	20	136	58
Kim03	43125.8046	52272.1994	25	249	104
Fauvaud06	43125.8046	53478.4921	28	415	105
Conidis13	43125.8046	55635.6073	34	1465	73
Zong19	43125.8046	58413.3119	41	1583	123

Notes: Chronology of the compilation of times of maximum by several authors. The time span and number of points in the database employed in the literature are presented.

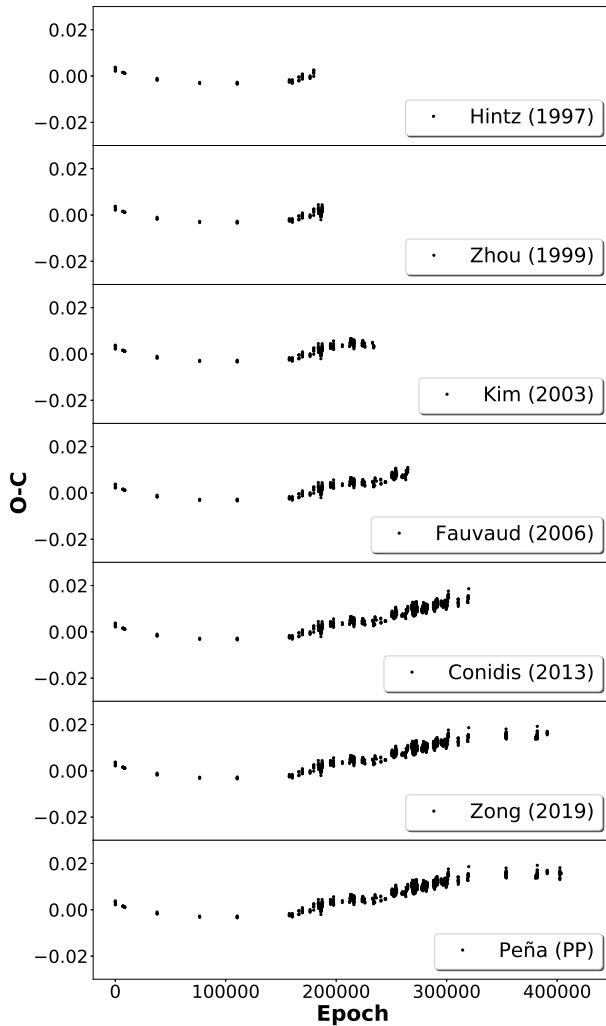


Fig. 1. O–C diagrams calculated with data from different authors (see main text) employing the ephemeris given by Zhou et al. 1999.

uals with their 136 times of maximum light, in which we can see that the parabolic behavior interpretation was logically inferred (see Figure 2). It is impor-

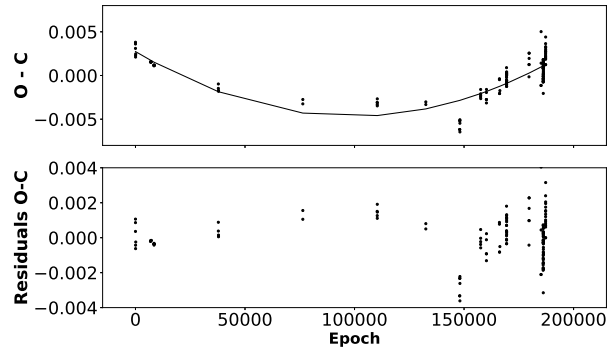


Fig. 2. Behaviour of the data points of Zhou et al. (1999) calculated reproducing their results: Top, the logically inferred parabolic behavior interpretation. Bottom, the O–C residuals calculated both linearly and quadratically. The plots use their own time span.

tant to mention that they report a change in rate of $7.1457 \times 10^{-13} \text{ day/cycle}$.

We have extended the time basis with the new values of T_{max} determined in January and February, 2020 for a total of 1606 times of maximum light and a time basis of twenty three years elapsed since the Zhou et al. (1999) study, increasing the accuracy of the ephemerides elements, T_0 and P given by Zhou et al. (1999). We followed the prescription provided by Zong et al. (2019) who calculated the number of elapsed cycles adjusting a linear fit to the times of maximum number of cycles presented in Figure 3 in the XY plane with X, the number of cycles and Y the times of maximum light. The newly determined values for T_0 and P are given in equation 3:

$$HJD = 2443125.7938(2) + 0.0390979132(9) \times E. \quad (3)$$

With these new determined values we calculated the new O–C values represented in Figure 4, analogous to those presented by Zong et al. (2019) in their Figure 5.

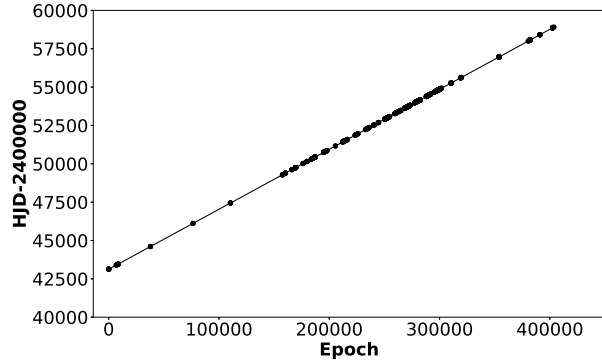


Fig. 3. Graphic representation of the linear equation 3 originally calculated by Zhou et al. (1999) that includes the new ephemerides elements with an extended time basis of 23 years. The new determined values are $T_0 = 2443125.7938(2)$ d and $P = 0.0390979132(9)$ d/cycle.

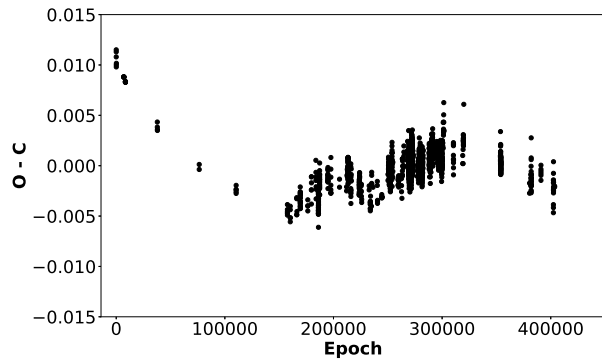


Fig. 4. O–C residuals of the 1606 data points with the new ephemerides equation deduced by a linear fit. This resembles equation 3 in Zong et al. (2019).

However, they arbitrarily discarded all O–C data points with E less than 150000 cycles because they showed an unexplained behaviour. Given the analogous results we obtained from Zong et al. (2019), we could have proceeded in the same fashion but, we preferred to consider all the O–C elements in the ephemerides procedure in Zhou et al. (1999).

Zong et al. (2019) carried out an exhaustive analysis of the O–C residuals. Their origin was based on the work of Fu et al. (2008) who suggested that the main period of BL Cam might have undergone an abrupt change. This change was studied by Fauvaud et al. (2010) and by Conidis & Delaney (2013) who suggested that the change of the main period

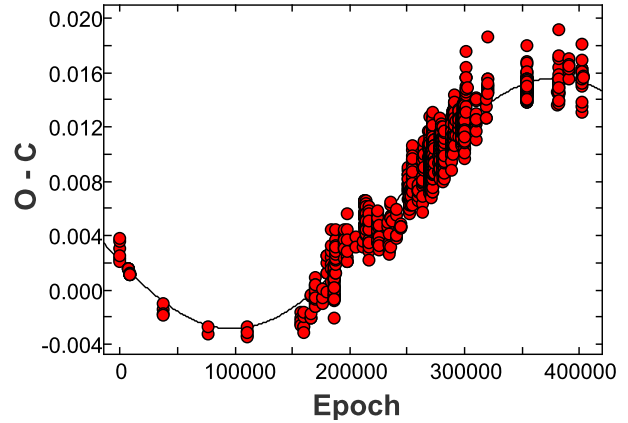


Fig. 5. Behavior of the O–C residuals for the whole sample of the 1606 data points with the ephemerides elements listed in equation 2 of Zhou et al. (1999) as a function of cycles. The color figure can be viewed online.

might be caused by a third body explained by a cubic curve adjustment shown in their Figure 5, which is presented here in Figure 4.

However, the model proposed by Zhou et al. (1999) shows that the main frequency derived in the O–C analysis is quite consistent with the fundamental frequency decomposed by Fourier transforms which explains all the times of maxima. Following this approach, we utilized Zhou et al.'s (1999) equation and considered the number of cycles and the O–C for the extended time basis all the elements, including those below an E of 150000 which Zong et al. (2019) had discarded. The smooth variation presented in Figure 5 was obtained if a sinusoid was assumed. If we only take the time span employed in Zhou et al (1999) into account, the logical deduction would be a parabolic behavior. This parabolic assumption was also assumed by Fauvaud et al. (2006) although their time basis was not long enough to reach a different conclusion, but when the elapsed time was extended, a sinusoidal variation can be seen.

Due to the fact that a sinusoid can be considered, in Figure 5 we calculated the variation parameters through a fit obtained with Period04, a canonical procedure utilized for short period variable stars (Lenz & Breger, 2005). Period04 is a computer program especially dedicated to the statistical analysis of large astronomical time series containing gaps. The program offers tools to extract the individual frequencies from the multiperiodic content of time series and provides a flexible interface to perform

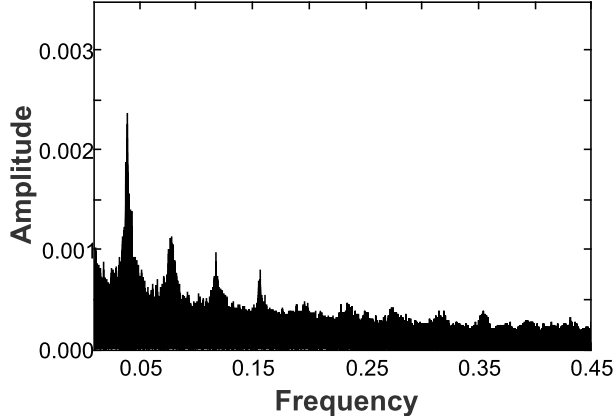


Fig. 6. Periodogram of the O–C residuals. The main peak is at 1.78×10^{-6} cycle/day.

TABLE 4

COEFFICIENTS DERIVED WITH PERIOD04

Parameter	Values	Uncertainty
Ω_1	178×10^{-8}	2×10^{-8}
B_1	923×10^{-5}	8×10^{-5}
α_1	576×10^{-3}	2×10^{-3}
Z	64×10^{-4}	1×10^{-4}

multiple-frequency fits. The Fourier analysis in Period04 is based on a discrete Fourier transform algorithm.

This fit to a sinusoid is shown in the Figure 5 by the continuous line, which explains those points discarded by Zong et al. (2019) and the newly observed points in 2020. The output of Period04 is presented by the following equation 4, with the numerical values presented in Table 4. It is shown schematically in Figure 6.

$$O - C = Z + \sum_{i=1}^n B_i \sin(2\pi(\Omega_i E + \alpha_i)). \quad (4)$$

With an extended time span it becomes evident that the conclusion reached previously was partial because it was obtained based on the limited time span at that time. Now, we postulate a sinusoidal behavior that could be explained by the presence of another unseen companion star and the light travel time effect (LTTE). Due to the above, we adjusted the equation:

$$(O - C) = a_0 + \sum_{i=1}^2 [a_i \cos(iwE) + b_i \sin(iwE)], \quad (5)$$

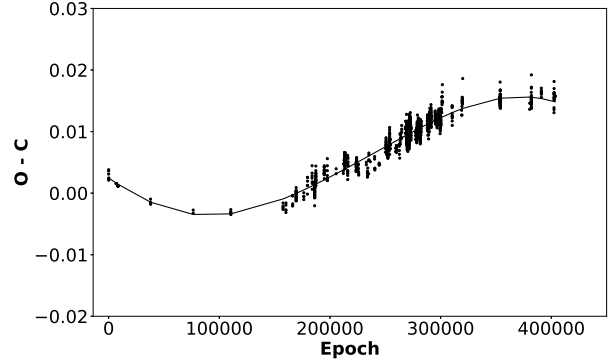


Fig. 7. New fit obtained utilizing Fourier series considering equation 5 and the Fourier coefficients listed in Table 5.

TABLE 5

FOURIER COEFFICIENTS

	[Values] $\times 10^{-4}$	[Uncertainty] $\times 10^{-4}$
a_0	59	1
a_1	-29	3
a_2	-5	1
b_1	-91	2
b_2	-5	2

to determine the optimized parameters for the equation to get the best fit to the data, we utilized the algorithm of Levenberg-Marquardt. As initial parameters we considered a_0 equal to $2Z$ and $w = 2\pi\Omega_1$. To the remaining coefficients we assigned zero values. The obtained optimized parameters and their standard deviations are presented in Table 5 for a frequency of $w = (122 \pm 2) \times 10^{-7}$ (1/d). This new analysis provides an orbital period of the star with a result of $P_{orb} = 55.2$ years. This postulation will be tested with continuous monitoring of this star over the next 12 years when the 55.2 years period that we predict will be completed. The results are shown in Figure 7.

Subtracting the calculated fit, we obtained the results presented in Figure 8. No clear evidence of another frequency exists as Fauvaud et al. (2010) and Conidis et al. (2013) proposed, but from our analysis it cannot be discarded due to the lack of observations in the cycle intervals between $[0, 142000]$ and $[330000, 382000]$ which makes the analysis difficult. Calculating the standard deviation of the residuals we get $\sigma = 0.0012$, less than that obtained by Zhou et al. (1999), Conidis et al. (2013) and Zong et al. (2019). This supports the sinusoidal behavior shown in the O–C diagram of Figure 7.

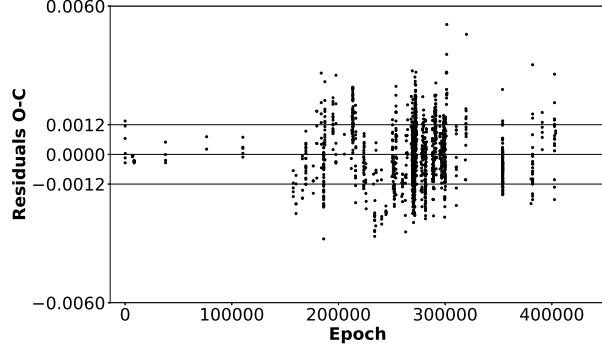


Fig. 8. Residuals after the Fourier series fit shown in Figure 7. The central horizontal line represents the mean value and the other extreme lines the standard deviation of the residuals.

TABLE 6
PARAMETERS OF THE COMPANION STAR
OF BL CAM

Orbital Parameter	Value
e'	0.15
w'	281.76
$A' \sin(i')$	1.65
P_{orb}	55.2

3.2. Determination of Orbital Parameters and Mass of the Companion Star

Carrying out an analysis of a binary system such as that developed by Zong et al. (2019), it is possible to determine the parameters of the companion star utilizing the formulae 6, 7 and 8 proposed by Borkovits et al. (1996), which are function of the Fourier coefficients.

$$e' = 2\sqrt{\frac{a_2^2 + b_2^2}{a_1^2 + b_1^2}}, \quad (6)$$

$$w' = \arctan \left(\frac{(b_1^2 - a_1^2)b_2 + 2a_1a_2b_1}{(a_1^2 - b_1^2)a_2 + 2a_1b_1b_2} \right), \quad (7)$$

$$A' \sin(i') = c\sqrt{a_1^2 + b_1^2}, \quad (8)$$

where a_0 is shown in equation 5; $a_{1,2}$; $b_{1,2}$ are the Fourier coefficients. These are listed in Table 5. A' denotes the semi-major axis. i' , e' y w' are the elements of the orbit of the companion, c is the speed of light in astronomical units per day.

TABLE 7
MASS OF THE COMPANION AS A FUNCTION
OF THE ANGLE

Angle	Semi-major axis	Mass
20	4.8	0.42
25	3.9	0.32
30	3.3	0.27
40	2.6	0.20
50	2.2	0.16
60	1.9	0.14
70	1.8	0.13
80	1.7	0.12

Then, we followed Borkovits & Hegedüs (1996) for the determination of the mass of the companion star.

Considering a three body system, Borkovits & Hegedüs (1996) present equation 11 in their paper as a solution which we used, adapting it to a binary system in which BL Cam orbits around another unseen star and the encountered variations in the O–C are provoked by the LTTE. This follows a prescription first employed by Fu et al. (2008). Combining them, equation 9 provides the mass function in terms of the orbital parameters.

Substituting the above-mentioned values listed in Table 6 calculated in this work in the mass function equation given in equation 9, it is possible to calculate the mass of the companion. Considering the mass of BL Cam as $m_1 = 0.99$ from McNamara (1997), we calculated the mass m_2 for different angles i' , shown in Table 7, determining the roots of the polynomial given in the equations:

$$f(m) = \frac{(A' \sin(i'))^3}{P_{orb}^2} = \frac{(m_2 \sin(i'))^3}{(m_1 + m_2)^2} = 0.00148, \quad (9)$$

$$\sin(i')^3 m_2^3 - f(m) m_2^2 - 2f(m) m_1 m_2 - f(m) m_1 = 0. \quad (10)$$

Being a cubic equation, it has three solutions. In each case we considered as a solution the real root. The other two are imaginary roots without physical interpretation. The mass of the companion star as a function of the inclination angle is shown in Table 7.

The behavior of mass as a function of angle is shown in Figure 9. Given the obtained values we can say that we are dealing with a M-type star.

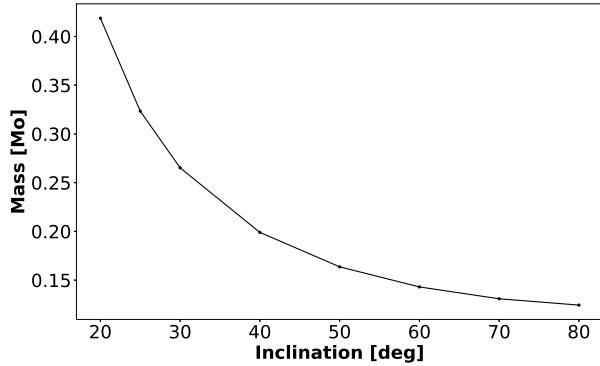


Fig. 9. Mass of the companion as a function of the angle.

3.3. Period Determination Conclusions

Despite having been determined to be a variable star many years ago, the variability of the SX Phe star BL Cam has been described with several interpretations as more information has been gathered. Considering the interpretation of this century only, we highlight the following studies.

Kim et al. (2003) found that the parabolic period variation had recently reversed. They also determined five frequencies for BL Cam using Fourier analysis. They stated that in order to confirm the periodic variation of the O–C values, BL Cam should be observed for at least 10 more years.

Rodriguez et al. (2007) reported that their results confirmed the existence of multi-periodicity in this star. In addition to the main frequency $f_0 = 25.5769$ c/d and its harmonics $2f_0$ and $3f_0$, with stable amplitude, a secondary frequency f_1 exists in the region 31–32 c/d with variable amplitude.

A more recent article, that of Fauvaud et al. (2010), states that the short-term O–C variation, if interpreted as a light travel-time effect, is indicative of a massive stellar component (0.46 to 1 $M_\odot$) with a short period orbit (144.2 d), within a distance of 0.7 AU from the primary and encourage more observations to confirm the long-term O–C variations. If they were also caused by a light travel-time effect, they could be interpreted in terms of a third component, in this case probably a brown dwarf star ($\geq 0.03M_\odot$), orbiting in 3400 d at a distance of 4.5 AU from the primary.

Conidis and Delaney (2013) found a more accurate period of 0.039097912(1) days, and presented an updated linear ephemeris. This newly presented linear ephemeris was used to calculate revised O–C values, which were fitted with a parabolic curve to measure the rate of change of the pulsation period.

Although the parabolic fit has a physical interpretation, it is noted that a cubic fit more appropriately describes the behavior of the O–C diagram, but they concluded that this assumes the O–C diagram is best represented by a quadratic fit. This has been shown to be a poor assumption, since a cubic polynomial is a better representation of the O–C diagram. This, according to them, is problematic since the physical meaning of the third order term cannot be explained physically.

The most recent paper, that of Zong et al. (2019) did not find evidence of a triple system as stated by Fu et al. (2008). Fauvaud et al. (2010) performed a triple system analysis of the O–C diagram. However, the determination of the second companion's parameters was not successful. The residuals of fitting the O–C curve implied that BL Cam might be a binary system in an eccentric orbit with a period of 14.01 (9) yr. The companion might be a brown dwarf.

In this study, with an extended time basis of 15779 days or 403578.6 cycles, we performed an O–C analysis and found that the residuals do not conform to the parabolic variation proposed by other authors but rather present a sinusoidal variation with a period of 60 years.

In our analysis we do not need to invoke multi-periodicity as was previously proposed, nor a parabolic behavior. Instead, with only one stable period, using Period04, we adjusted the 1606 times of maximum light shown in Figure 5. Our final fit is obtained using equation 5 and is presented in Figure 7; its residuals are shown in Figure 8.

Considering the obtained results of the present work, and taking into account the residuals in the σ interval presented in Figure 8, this paper has shed light on the nature of BL Cam. Before we consider that it might be a triple system, as Fauvaud1 (2010) proposed, continuous monitoring of the star is mandatory.

4. PHYSICAL PARAMETERS

In this section, we consider $uvby - \beta$ photometry to determine some physical parameters. With this photometric system it is possible to determine reddening and unreddened values via the procedure proposed by Nissen (1988). The accuracy of our photometry is evaluated by three methods. From these we determined the metallicity $[\text{Fe}/\text{H}]$ and by comparing the unreddened indexes c_0 and $(b - y)_0$ with the Castelli & Kurucz (2006) models effective temperature and surface gravity were estimated.

TABLE 8

MEAN PHOTOMETRIC VALUES AND STANDARD DEVIATIONS OF THE STANDARD STARS OF THE 2020 SEASON

ID	V	$(b - y)$	m_1	c_1	β	σV	$\sigma(b - y)$	σm_1	σc_1	$\sigma \beta$	N
HD114710	4.233	0.365	0.195	0.340	2.600	0.004	0.003	0.002	0.006	0.014	5
HD111812	4.944	0.429	0.204	0.406	2.589	0.044	0.003	0.004	0.005	0.016	5
HD28355	5.000	0.113	0.240	0.890	2.847	0.010	0.003	0.003	0.007	0.016	5
HD69897	5.117	0.314	0.148	0.383	2.630	0.010	0.002	0.002	0.005	0.013	8
HD115383	5.176	0.369	0.190	0.390	2.615	0.005	0.003	0.003	0.003	0.015	5
HD154029	5.255	0.002	0.174	1.098	2.871	0.021	0.002	0.004	0.008	0.012	5
HD157214	5.374	0.395	0.178	0.318	2.571	0.008	0.003	0.004	0.006	0.015	5
HD76398	5.427	0.085	0.208	0.971	2.852	0.007	0.003	0.003	0.006	0.010	8
HD178233	5.497	0.174	0.193	0.737	2.755	0.015	0.003	0.003	0.006	0.013	5
HD23324	5.638	-0.008	0.089	0.639	2.751	0.008	0.002	0.001	0.002	0.013	4
HD26462	5.695	0.234	0.170	0.590	2.723	0.014	0.003	0.003	0.009	0.016	5
HD24357	5.951	0.227	0.167	0.605	2.724	0.008	0.002	0.001	0.003	0.018	4
HD32147	6.218	0.614	0.639	0.248	2.552	0.022	0.001	0.004	0.008	0.018	5
HD122563	6.236	0.633	0.103	0.474	2.526	0.063	0.004	0.004	0.007	0.013	5
HD137778	7.573	0.538	0.453	0.292	2.567	0.017	0.004	0.006	0.011	0.012	5
HD125455	7.579	0.502	0.366	0.299	2.555	0.013	0.003	0.004	0.008	0.014	5
HD36003	7.636	0.641	0.663	0.200	2.521	0.021	0.002	0.002	0.011	0.016	5
HD154363	7.698	0.666	0.635	0.167	2.488	0.008	0.002	0.004	0.008	0.014	5
HD21197	7.846	0.667	0.731	0.152	2.537	0.011	0.002	0.006	0.011	0.012	4
HD117243	8.352	0.408	0.205	0.405	2.610	0.016	0.004	0.004	0.006	0.010	5
Mean						0.016	0.003	0.003	0.007	0.014	103
Std. Dev.						0.014	0.001	0.001	0.003	0.002	

The $uvby - \beta$ photometric system has the advantage that reddening and unreddened colors can be determined from the photometry and the proper calibrations. One of the pioneer works in this matter was that of Crawford and collaborators. Later, in 1988, Nissen (1988) extended the sample of clusters to thirteen and developed empirical calibrations which determined the intrinsic color index $(b - y)_0$ in terms of the other color indexes and β utilizing as reference the Hyades. Nissen's (1988) procedure is applicable for A and F type stars. For F type stars ($2.59 \leq \beta \leq 2.72$) the intrinsic color index $(b - y)_0$ is calculated by the expression:

$$(b - y)_0 = K + 1.11\Delta\beta + 2.7\Delta\beta - 0.05\delta c_0 - (0.1 + 3.6\Delta\beta)\delta m_0. \quad (11)$$

4.1. Data Acquisition and Reduction at SPM

At the SPM Observatory the observational, as well as the reduction procedures, have been employed since 1986 and have been described many times. A recent detailed description of the methodology can be found in Peña and Martinez (2014).

The star BL Cam was observed in $uvby - \beta$ photometry in February, 2020. The season covered five

nights during which BL Cam was observed on two. Over all the nights of observation the following procedure was used: each measurement consisted of five ten-second integrations of the star and three ten-second integrations of the sky simultaneously for the $uvby$ filters and almost simultaneous for the narrow and wide filters that define $H\beta$.

The accuracy of our observation was evaluated by three numerical procedures: (i) the accuracy of each point; (ii) a comparison of the observed standard stars with those values in the literature, and (iii) a comparison of the observed standard stars obtained in each night throughout the whole season.

In the first case, the accuracy is a direct result of the star counts. Although BL Cam is a faint star for our telescope-spectrophotometer system we obtained in the five ten-seconds integrations, enough counts to calculate the errors for the u , b , v , and y filters that define the $uvby - \beta$ photoelectric photometry, equal to (18491, 53040, 68053, 24413), respectively, which translated into uncertainties of (0.0074, 0.0043, 0.0038, 0.0064) magnitudes.

For the second criterion we reduced each night separately calculating the transformation coefficients and the difference in magnitude between the obtained values and the values reported in the literature for each night. To calculate the final photo-

TABLE 9
MEAN VALUES AND STANDARD DEVIATIONS

Season	B	D	F	J	H	I	L
2020 Feb	0.0743	0.9814	1.0758	0.0431	1.051	0.1893	-1.3529
$< \sigma >$	0.0303	0.0019	0.0037	0.0023	0.0054	0.0106	0.0139

Notes: Mean values and standard deviations $< \sigma >$ of the transformation coefficients obtained for the seasons.

metric values we averaged the nightly coefficients and the differences with the literature. With the obtained photometric values we reduced the data as described in Peña & Martínez (2014). What must be noted here are the transformation coefficients for the observed season (Table 9). This led to the obtainment of the final photometric values. The season errors were evaluated using the observed standard stars with those employed from the literature. These uncertainties were calculated through the differences in magnitude and colors for $(V, (b-y), m_1, c_1 \text{ and } H\beta)$ which are (0.035, 0.008, 0.011, 0.011, 0.012) for the 2020 season.

For the final numerical evaluation of the accuracy we considered all the standard stars on each night in the whole season, for a total of 118 points in $uvby$ and 106 points in $H\beta$, of the standard stars. For each star we calculated its mean value as well as the standard deviation. This provides a numerical evaluation of our uncertainties considering the whole season, as well as the goodness of the season. The obtained results are presented in Table 8 with the ID of the star in Column 1. Columns two to six present the magnitude and color indexes ($V, (b-y), m_1, c_1$ and $H\beta$) and Columns seven to eleven, their corresponding standard deviations; the last column lists N, the number of data points of each star in the season. The mean values of the season with the standard deviations are shown in the last two lines. With the exception of the star HD122563 the standard deviation of all the standard stars is on the order of thousandths in the V magnitude. For this reason, HD122563 may be a new variable star since it is similar to HD 115520, which was discovered to be a new δ Scuti variable by Peña et al. (2007).

4.2. Metallicity ($[\text{Fe}/\text{H}]$) Determination Through $uvby - \beta$ Observations

Nissen (1988) also proposed equations to determine metal abundance (for stars of F spectral type). The metal abundance $[\text{Fe}/\text{H}]$ is given by Nissen (1988) through the equation:

$$[\text{Fe}/\text{H}] = -(10.5 + 50(\beta - 2.626))\delta m_0 + 0.12. \quad (12)$$

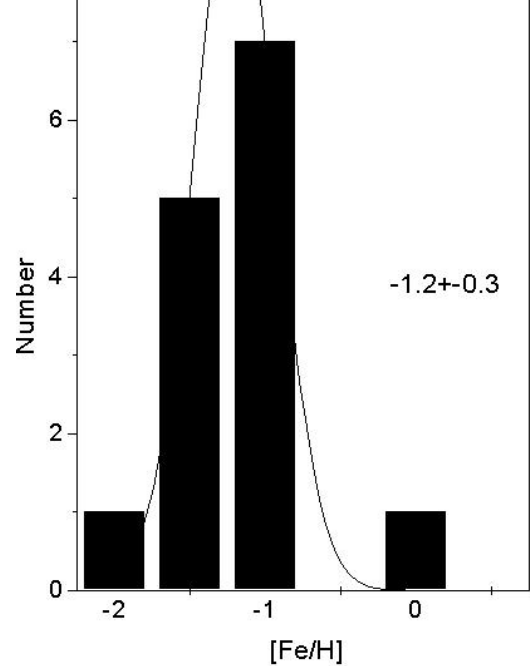


Fig. 10. Distribution of metallicity when the star goes through an F type stage.

We applied Nissen's (1988) prescription (described in detail in Peña & Martínez 2014) to the $uvby - \beta$ photometric values presented in Table 10 arranged by decreasing β , and we determined the reddening, the unreddened indexes $(b-y)_0, m_0, c_0$, as well as the metallicity when the star passes through an F type stage. The metallicity values distribution is presented in Figure 10 which shows the histogram of all the values. As can be seen the mean value is -1.2 ± 0.3 . The continuous line is a Gaussian fit.

A comparison between the unreddened indexes c_0 and $(b-y)_0$ was obtained for the star with the Castelli & Kurucz (2006) models which are based on ATLAS9 model atmospheres. This allowed us to determine the effective temperature T_e and the surface gravity $\log g$ (Figure 11). The effective temperature varies between 7250 K and 8000 K, whereas the surface gravity is around $\log g = 3.5$. Table 10 lists these values. Column 1 shows the HJD, Column 2 to 5 the unreddened indexes and β .

TABLE 10

TIME, MAGNITUDE, COLOR INDEXES AND β
OF BL CAM

HJD(-2458000)	V	$(b-y)$	m_1	c_1	β
904.6674	13.121	0.483	-0.075	0.973	2.824
904.6690	13.151	0.425	-0.005	0.801	2.784
904.6719	13.177	0.409	0.013	0.816	2.679
904.6735	13.196	0.433	-0.021	0.858	2.665
904.6767	13.230	0.404	-0.004	0.878	2.702
904.6785	13.216	0.394	0.016	0.798	2.785
904.6814	13.187	0.380	0.040	0.829	2.643
904.6828	13.153	0.375	0.038	0.795	2.863
904.6857	13.041	0.409	0.008	0.845	2.794
904.6872	13.004	0.374	0.023	0.912	2.838
904.6898	12.949	0.352	0.047	0.996	2.830
904.6914	12.947	0.326	0.077	0.957	2.643
904.6939	12.932	0.342	0.047	0.993	2.713
904.6956	12.978	0.306	0.103	0.933	2.834
904.6982	12.982	0.390	0.016	0.909	2.804
904.7001	13.269	0.331	0.004	0.913	2.888
904.7024	13.100	0.375	0.017	0.915	2.774
904.7039	13.121	0.361	0.087	0.897	2.809
904.7069	13.142	0.417	-0.022	0.904	2.788
904.7085	13.208	0.362	0.046	0.886	2.763
904.7130	13.203	0.440	-0.059	0.860	2.804
904.7145	13.195	0.410	0.057	0.745	2.781
904.7171	13.172	0.444	-0.023	0.775	2.934
904.7187	13.171	0.420	0.019	0.786	2.915
904.7202	13.179	0.374	0.058	0.835	2.782
904.7217	13.156	0.436	-0.060	0.828	2.881
904.7241	13.123	0.342	0.075	0.849	2.719
904.7257	13.046	0.363	0.054	0.844	2.901
904.7281	12.966	0.344	0.079	0.809	2.893
904.7295	12.974	0.312	0.080	0.887	2.824
904.7336	12.953	0.336	0.072	0.976	
904.7354	12.975	0.369	-0.022	1.013	2.805
904.7370	12.983	0.402	-0.026	0.976	2.716
904.7384	13.024	0.347	0.095	0.848	2.746
904.7408	13.060	0.373	0.065	0.857	2.778
904.7423	13.113	0.360	0.052	0.871	2.766
904.7439	13.123	0.409	-0.016	0.911	2.759
904.7453	13.141	0.393	0.012	0.888	2.635
904.7478	13.182	0.398	0.006	0.916	2.681
904.7493	13.159	0.438	0.011	0.820	2.623
906.6732	13.278	0.382	0.073	0.854	2.842
906.6754	13.247	0.357	0.125	0.856	2.835
906.6771	13.143	0.386	0.025	0.800	2.717
906.6908	12.968	0.314	0.087	0.894	2.819
906.6922	12.994	0.340	0.054	0.908	2.778
906.6937	13.059	0.334	0.089	1.015	2.817
906.7193	13.067	0.333	0.088	0.871	2.903
906.7208	12.999	0.320	0.076	0.953	2.777
906.7223	13.011	0.294	0.071	0.959	2.907
906.7315	12.985	0.356	0.003	1.037	2.865
906.7331	13.003	0.369	0.019	0.947	2.827

Table 10. Continued

HJD(-2458000)	V	$(b-y)$	m_1	c_1	β
906.7345	13.076	0.302	0.168	0.826	2.654
906.7438	13.176	0.365	0.078	0.830	2.782
906.7452	13.168	0.394	0.027	0.859	2.834
906.7467	13.208	0.380	0.050	0.832	2.771
906.7501	13.211	0.385	0.022	0.854	2.817
906.7516	13.195	0.388	0.030	0.824	2.834
906.7530	13.185	0.399	0.042	0.795	2.697
904.7478	13.182	0.398	0.006	0.916	2.681
904.6719	13.177	0.409	0.013	0.816	2.679
904.6735	13.196	0.433	-0.021	0.858	2.665
906.7345	13.076	0.302	0.168	0.826	2.654
904.6814	13.187	0.380	0.040	0.829	2.643
904.6914	12.947	0.326	0.077	0.957	2.643
904.7453	13.141	0.393	0.012	0.888	2.635
904.7493	13.159	0.438	0.011	0.820	2.623
904.7336	12.953	0.336	0.072	0.976	

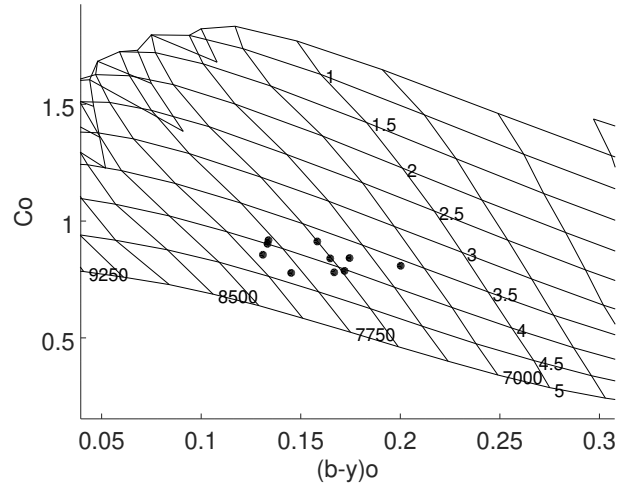


Fig. 11. Unreddened color indexes on the Castelli & Kurucz (2006) grids.

Subsequent columns present metallicity, effective temperature from the theoretical relation reported by Rodriguez (1989) based on a relation from Petersen & Jorgensen (1972, hereinafter P&J72) $Te = 6850 + 1250 \times (\beta - 2.684)/0.144$ for each value and averaged, and surface gravity. The averaged temperature along the phase interval of 0.3 to 0.8 is 7682 ± 503 K.

4.3. Physical Parameters Conclusions

Most of the papers devoted to BL Cam have emphasised its pulsational nature and few have tried to determine its physical parameters. In this paper, we were able to unreddden the color indexes and determine the reddening and the metallicity

TABLE 11
COLOR INDEXES & PHYSICAL PARAMETERS OF BL CAM AS A FUNCTION OF PHASE

HJD - 2458900.0	$(b - y)_0$	m_0	c_0	β	[Fe/H]	$T_e[K]$	$\log g$	Phase
6.7315	0.067	0.090	0.979	2.865		8421	3.9	0.54
4.6828	0.093	0.123	0.739	2.863		8403	4.7	0.14
6.6732	0.104	0.156	0.798	2.842		8221	4.3	0.05
4.6872	0.102	0.105	0.858	2.838		8186	4.1	0.26
6.6754	0.110	0.199	0.807	2.835		8160	4.3	0.11
4.6956	0.103	0.164	0.892	2.834		8152	4.0	0.47
6.7452	0.110	0.112	0.802	2.834		8152	4.3	0.89
6.7516	0.114	0.112	0.769	2.834		8152	4.4	0.06
4.6898	0.100	0.123	0.946	2.830		8117	3.8	0.32
6.7331	0.107	0.097	0.895	2.827		8091	3.9	0.58
4.6674	0.107	0.038	0.898	2.824		8065	3.8	0.75
4.7295	0.116	0.139	0.848	2.824		8065	4.1	0.34
6.6908	0.119	0.145	0.855	2.819		8021	4.1	0.50
6.6937	0.109	0.157	0.970	2.817		8004	3.6	0.58
6.7501	0.125	0.100	0.802	2.817		8004	4.2	0.02
4.7039	0.127	0.157	0.850	2.809		7935	4.0	0.68
4.7354	0.119	0.053	0.963	2.805		7900	3.6	0.49
4.6982	0.130	0.094	0.857	2.804		7891	3.9	0.54
4.7130	0.135	0.033	0.799	2.804		7891	4.1	0.91
4.6857	0.144	0.087	0.792	2.794		7804	4.1	0.22
4.7069	0.143	0.060	0.849	2.788		7752	3.8	0.76
4.6785	0.156	0.087	0.750	2.785		7726	4.2	0.03
4.6690	0.157	0.075	0.747	2.784		7718	4.1	0.79
4.7202	0.155	0.124	0.791	2.782		7700	4.0	0.10
6.7438	0.155	0.141	0.788	2.782		7700	4.0	0.86
4.7145	0.165	0.131	0.696	2.781		7692	4.3	0.95
4.7408	0.156	0.130	0.814	2.778		7665	3.9	0.63
6.6922	0.151	0.111	0.870	2.778		7665	3.7	0.54
6.7208	0.147	0.128	0.918	2.777		7657	3.6	0.27
4.7024	0.153	0.084	0.871	2.774		7631	3.7	0.64
6.7467	0.164	0.115	0.789	2.771		7605	3.9	0.93
4.7423	0.164	0.111	0.832	2.766		7561	3.8	0.67
4.7085	0.165	0.105	0.847	2.763		7535	3.7	0.80
4.7439	0.166	0.057	0.862	2.759		7501	3.6	0.70
4.7384	0.182	0.144	0.815	2.746		7388	3.7	0.56
4.7241	0.200	0.118	0.821	2.719	-0.775	7153	3.4	0.20
6.6771	0.200	0.081	0.763	2.717	-1.314	7136	3.6	0.15
4.7370	0.187	0.039	0.933	2.716	-1.939	7127	2.9	0.53
4.6939	0.194	0.091	0.963	2.713	-1.121	7101	2.8	0.43
4.6767	0.203	0.056	0.838	2.702	-1.539	7006	3.1	0.99
6.7530	0.217	0.096	0.759	2.697	-0.937	6962	3.4	0.09
4.7478	0.217	0.060	0.880	2.681	-1.334	6823	2.8	0.81
4.6719	0.225	0.068	0.779	2.679	-1.221	6806	3.1	0.86
4.6735	0.226	0.041	0.817	2.665	-1.518	6685	2.8	0.90
4.6814	0.257	0.077	0.804	2.643	-1.068	6494	2.7	0.11
4.6914	0.259	0.097	0.944	2.643	-0.837	6494	2.3	0.36
4.7453	0.252	0.054	0.860	2.635	-1.322	6424	2.5	0.74
4.7493	0.268	0.062	0.786	2.623	-1.244	6320	2.6	0.84
Average					-1.244	7598		
σ					0.315	555		

with $uvby - \beta$ photoelectric photometry and the well-calibrated equations of Nissen (1988). Locating these indexes on the grids of Castelli & Kurucz (2006) we determined the effective temperature and surface gravity of the star along its cycle of pulsation.

5. CONCLUSIONS

In the present study we have demonstrated that BL Cam is pulsating with one stable varying period whose O–C residuals show a sinusoidal pattern compatible with a light-travel time effect.

We have shown that the evolution of the ephemerides of the different authors were natural and correct given the shortness of the available data at their times. With a longer time basis we have shown that the long term variation is due to a binary system.

For the determination of the physical parameters some authors mentioned the need to acquire data in $uvby - \beta$, a need that we were able to satisfy. New observations in $uvby - \beta$ and CCD photometry were carried out at the San Pedro Mártir and Tonantzintla observatories, respectively, on the SX Phe star BL Cam.

The appropriate model of Castelli & Kurucz (2006) provided the physical characteristics of the star: effective temperature (T_e) and surface gravity ($\log g$), once the metallicity had been determined. The effective temperature was also calculated through the theoretical relation (P&J72). The numerical values obtained by both methods gave similar results within the error bars, and gave a good idea of the behavior of the star.

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