

On the Optimal Reconfiguration of Radial AC Distribution Networks Using an MINLP Formulation: A GAMS-Based Approach

Sobre la reconfiguración óptima de redes radiales de distribución empleando un modelo de PNLEM: un enfoque basado en GAMS

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ABSTRACT

This paper addresses the problem of the optimal reconfiguration of medium-voltage distribution networks by proposing a mixed-integer nonlinear programming (MINLP) model. The objective function of this optimization model is the minimization of the total power losses in all the branches of the network, considering active and reactive power balance equations, voltage regulation bounds, and device capabilities, among others. The proposed MINLP formulation works with branch-to-node incidence that allows representing the active and reactive power flow in branches as a function of the real and imaginary components of the voltages and currents. The solution of the MINLP model is reached through the general algebraic modeling system widely known as the GAMS package while presenting it in the form of a tutorial. This software allows implementing the proposed model in a compact way, which is solved via branch and bound methods. Two test feeders comprising 5 and 14 nodes allow demonstrating the fidelity of the proposed MINLP model regarding power loss minimization when compared to that reported in the specialized literature.

Keywords: nonlinear optimization, general algebraic modeling system, distribution system reconfiguration, power loss minimization, mixed-integer nonlinear programming

RESUMEN

Este artículo aborda el problema de la reconfiguración óptima de redes de distribución de media tensión mediante la proposición de un modelo de programación no lineal entera mixta (PNLEM). La función objetivo de este modelo de optimización es la minimización de las pérdidas totales de potencia activa en todas las ramas del sistema, considerando las ecuaciones de balance de potencia activa y reactiva, los límites de regulación de voltaje y la capacidad de los diferentes dispositivos, entre otros. La formulación de PNLEM propuesto trabaja con la matriz de incidencia rama-nodo, la cual permite representar las ecuaciones de flujo de potencia en las ramas como una función de los componentes reales e imaginarios de los voltajes en los nodos y las corrientes en las ramas. La solución del modelo de PNLEM se obtiene a través del sistema de modelado algebraico general ampliamente conocido como el paquete GAMS, presentándolo en forma de tutorial. Este software permite implementar el modelo de optimización propuesto en forma compacta, el cual se resuelve mediante métodos de ramificación y corte. Dos alimentadores de prueba compuestos de 5 y 14 nodos permiten demostrar la fidelidad del modelo de PNLEM propuesto en relación con la minimización de pérdidas de potencia cuando se compara con reportes de la literatura especializada.

Palabras clave: optimización no lineal, sistema de modelado algebraico general, reconfiguración de sistemas de distribución, minimización de pérdidas de potencia, programación no lineal entera mixta

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Introduction

General context

Electrical distribution networks correspond to the largest part of the power system that is responsible for the commercialization and distribution of electricity services to end-users at medium voltage levels (Sánchez-Zuleta *et al.*, 2012). The extensive longitude of these electrical networks combined with medium voltages is susceptible to high power losses in comparison with transmission networks (Anders, 1994). In the Colombian context, electrical networks typically operate between 11,4 kV and 13,8 kV, with power losses between 6 and 15% of the total energy bought in the spot market (Zuleta *et al.*, 2017). These percentage differences are related to the practices implemented by utilities regarding distribution system operation, as well as to the geographical location

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of the distribution grid, given that Colombia is essentially a rural country. This implies that the distribution networks have hundreds of kilometers of extension increment power losses due to the natural configuration of the grid (Marneni *et al.*, 2015). An additional fact that furthers power losses in the distribution stage corresponds to the radial structure of this network, which is largely adopted by utilities since it simplifies the coordination of protective devices (reclosers, sectionalizers, and fuses) and also reduces investments in infrastructure such as conductors and supports (Celli *et al.*, 2004; Cruz *et al.*, 2018), among others.

Optimal reconfiguration in distribution networks is a strategy to improve the operating conditions of power systems. It is a real-time operational task performed to minimize losses, improve voltage profiles, improve reliability indicators, balance the load, and minimize operating costs (Celli *et al.*, 2004; Cruz *et al.*, 2018).

Network operation and design standards have changed in recent years due to factors such as the need for new monitoring and control systems, the rational use of resources, the demand for high-quality service, and the deregulation of the electric power market (Augugliaro *et al.*, 2004; Azghandi *et al.*, 2021). Each of these factors represents a set of challenges that require technological advances. The aim is to improve the current scenarios and adapt to the challenges of the future energy industry by providing clean, economic, reliable, and safe electrical energy. Optimization applied to distribution networks plays a relevant role in adapting to these new challenges (Jafar-Nowdeh *et al.*, 2020; Vargas-Robayo *et al.*, 2021; Zhengzhong *et al.*, 2021).

Future scenarios for distribution networks need to include strategies that allow operating under unconventional conditions such as dynamic and probabilistic loads, renewable energy sources at distribution points, small-scale generation, bidirectional power flow, among others (Haitham and Helmi, 2021; Jafar-Nowdeh *et al.*, 2020; Raju and Sandeep, 2021). Operation scenarios can be adequately and efficiently addressed by proposing an optimal reconfigurable network (Sambaiah and Jaybarathi, 2021).

Motivation

The amount of power losses of distribution networks is undoubtedly an essential issue for electrical distribution companies, since it is the most direct quality indicator in the electrical service (Celli *et al.*, 2004). In order to minimize power losses in distribution networks, multiple strategies can be implemented, such as the optimal placement of distributed generators (Grisales-Noreña *et al.*, 2017; Grisales-Noreña *et al.*, 2018), shunt-capacitors (Elsheikh *et al.*, 2014), batteries (Grisales-Noreña *et al.*, 2019; Montoya *et al.*, 2020b), or the optimal reconfiguration of the network (Verma and Singh, 2018). Nevertheless, in the case of the optimal reconfiguration, most studies focus on the solution technique, glossing over the importance of an adequate mathematical formulation. This gap in the literature is the main motivation of this research. Our interest is to provide a correct mathematical formulation of the reconfiguration problem in distribution networks using a mixed-integer nonlinear programming model that can be solved with any optimization package (Montoya *et*

al., 2020a). This is especially important since engineers need to be formed in mathematical analysis, *i.e.*, with the capabilities of current adequate mathematical models that represent real-life problems. Moreover, they need to have the ability to solve them efficiently.

State of the art

The problem of the optimal reconfiguration of AC distribution feeders is a classical optimization problem in power systems analysis (Civanlar *et al.*, 1988). In general terms, this problem can be described as determining the best subset of lines that generates a radial configuration network from an initial solution space conformed by connected (existing) and tie lines (opened), which allows reducing the total active power losses into the network, fulfilling the devices' capabilities (current in lines and power generation in sources) and guaranteeing power balance and voltages bounds in all the nodes. In mathematical terms, this problem can be formulated by using a mixed-integer nonlinear programming structure, *i.e.*, an MINLP model (Lavorato *et al.*, 2012). To solve this problem, the specialized literature has proposed multiple approaches, most of them based on metaheuristic optimization, namely genetic algorithms (Su *et al.*, 2005; Zhang *et al.*, 2014), ant colony optimization (Ahuja and Pahwa, 2005; Su *et al.*, 2005), chaotic stochastic fractal search algorithms (The *et al.*, 2020), tabu search algorithms (García-Martínez and Espinosa-Juárez, 2013), binary particle swarm optimization (Arya *et al.*, 2011; Tandon and Saxena, 2014; Xiaozhi *et al.*, 2010), culture search algorithms (Verma and Singh, 2018), ant lion optimizer (Shokouhi *et al.*, 2017), and bat algorithms (Quintero-Durán *et al.*, 2019), among others.

The main characteristic of the aforementioned metaheuristic optimization approaches is that all of them concentrate efforts on solving the reconfiguration problem in sequential steps by proposing codification and evolution strategies. This implies that they have decomposed the problem into a master-slave strategy, where the metaheuristic approach is the master layer, and the slave stage corresponds to a conventional power flow approach (Su *et al.*, 2005). Even if these strategies are efficient to solve complex optimization problems implying binary variables (Verma and Singh, 2018), they have a recurrent problem from a theoretical perspective, since these neglect the importance of a correct mathematical representation of the problem and only focus on designing an algorithm to solve it (Grisales-Noreña *et al.*, 2018). To address the problem of reconfiguration correctly, Lavorato *et al.* (2012) presented a complete formulation to solve the problem regarding the optimal planning of distribution network systems that can be solved in the AMPL software. Nevertheless, the problem in that formulation is the representation of the voltage profiles, since the authors follow the classical representation that uses trigonometric functions, which clearly includes strong nonlinearities in the optimization model, thus increasing the possibilities of staying stuck in a local solution (Montoya *et al.*, 2020; Sultana and Roy, 2015). Hence, we present an alternative mathematical formulation to address this problem, which allows representing the problem of the



optimal reconfiguration in AC distribution networks without involving trigonometric functions (which is presented as a tutorial). This approach will be particularly interesting to introduce beginners to optimization problems, especially for power systems engineers (Soroudi, 2017).

Contributions and scope

The main contributions of this research can be summarized as follows:

- ✓ The mathematical formulation of the optimal reconfiguration problem in AC distribution networks using a rectangular representation of the voltage and current variables added to the inclusion of binary variables, which allows determining the subset of conductors needed to minimize the total power losses in all the branches of the network.
- ✓ The implementation of the proposed MINLP formulation in a specialized software known as the general algebraic modeling system (GAMS) in the form of a tutorial that allows introducing engineering students to mathematical optimization.

It is worth mentioning that the proposed MINLP model for optimal reconfiguration of AC distribution feeders has not been previously reported in the specialized literature, which corresponds to a gap that this research aims to fill. In addition, we introduce the general algebraic modeling system as a powerful optimization tool that helps solve large-scale nonlinear programming problems by focusing on the mathematical formulation and not on the solution technique. This is important since, in power systems optimization, when metaheuristic optimization is employed, the mathematical model is neglected by tackling the sequential step to solve the optimization problem. This practice is not advised when engineering students are introduced to mathematical optimization; the main focus must be the correct formulation of the problem under study and not the solution method. Therefore, this research concentrates on presenting a comprehensive formulation of the optimization reconfiguration of AC distribution feeders using an MINLP model.

Organization of the document

This paper is organized as follows: the MINLP formulation section presents the mathematical formulation of the optimal reconfiguration problem of AC distribution feeders by using a rectangular representation of the voltage and current variables, which produces a mixed-integer nonlinear programming model. The next section introduces the solution methodology based on the general algebraic modeling system that allows implementing the MINLP model in a compact structure. The numerical validation section presents numerical simulations for a classical 13-node test feeder using the GAMS software, as well as their comparisons with literature reports. The conclusions and future Work section presents the principal outcomes derived from this work, as well as some possible future developments.

MINLP formulation

The problem of the optimal reconfiguration of electrical distribution networks is indeed a complex optimization problem due to the presence of the power balance equations containing multiple products between voltage and currents (nonlinear expressions). Additionally, the nature of this optimization problem is binary, given the necessity of selecting a subset of conductors that minimizes the power losses of the distribution system for a particular load condition. The complete mathematical model of the reconfiguration problem in distribution networks is described below.

Objective function

The objective function of the optimal reconfiguration problem corresponds to the minimization of the active power losses in all the branches of the network p_{loss} , as expressed by Equation (1).

$$\min z = p_{\text{loss}} = \sum_{l \in \mathcal{L}} R_l I_l^2, \quad (1)$$

where R_l is the resistance value of the conductor associated to branch l , and I_l is the magnitude of the current that flows in said branch. Note that $\mathcal{L}$ is the set containing all the branches (connected and non-connected).

Set of constraints

The set of constraints that defines the solution space of the optimal reconfiguration problem in AC distribution networks is defined as follows: first, the active and reactive power balance equations are presented using the real and imaginary parts of the voltage and current variables, as shown in Equations (2) and (3).

$$P_g^k - P_d^k = \sum_{l \in \mathcal{L}} \mathcal{A}_{kl} (V_k^r I_l^r + V_k^i I_l^i), \quad \forall k \in \mathcal{N}, \quad (2)$$

$$Q_g^k - Q_d^k = - \sum_{l \in \mathcal{L}} \mathcal{A}_{kl} (V_k^r I_l^i - V_k^i I_l^r), \quad \forall k \in \mathcal{N}, \quad (3)$$

where P_g^k and P_d^k are the active power generation and demands at node k , respectively; Q_g^k and Q_d^k represent the reactive power generation and consumption at node k , respectively; V_k^r and V_k^i are the real and imaginary parts of the voltage variable at node k ; and I_l^r and I_l^i correspond to the real and imaginary components of the current that flows in branch l . Note that $\mathcal{A}_{kl}$ is the incidence node-to-branch matrix, and its components are defined as follows:

- ✓ $\mathcal{A}_{kl} = +1$ if the branch l is connected at node k and the current I_l leaves this node.
- ✓ $\mathcal{A}_{kl} = -1$ if the branch l is connected at node k and the current I_l arrives to this node.
- ✓ $\mathcal{A}_{kl} = 0$ if the branch l is non connected at node k .

Second, the real and imaginary currents are defined as function of the voltage drops at the ends of each branch

(Equations (4) and (5)).

$$I_l^r = \frac{y_l}{R_l^2 + X_l^2} \sum_{k \in \mathcal{N}} \mathcal{A}_{kl} (R_l V_k^r + X_l V_k^i), \quad \forall l \in \mathcal{L}, \quad (4)$$

$$I_l^i = \frac{y_l}{R_l^2 + X_l^2} \sum_{k \in \mathcal{N}} \mathcal{A}_{kl} (R_l V_k^i - X_l V_k^r), \quad \forall l \in \mathcal{L}, \quad (5)$$

where y_l is a binary variable that determines whether the branch l is connected to the distribution network ($y_l = 1$) or not ($y_l = 0$) and X_l is the reactance effect in the conductor l . Note that $\mathcal{N}$ is the set that contains all the nodes of the network.

Third, the magnitudes of the voltages and currents are defined through Equations (6) and (7).

$$I_l = \sqrt{(I_l^r)^2 + (I_l^i)^2}, \quad \forall l \in \mathcal{L}, \quad (6)$$

$$V_k = \sqrt{(V_k^r)^2 + (V_k^i)^2}, \quad \forall k \in \mathcal{N}. \quad (7)$$

Fourth, the current capabilities and voltage regulation bounds are defined to ensure the useful life of the conductors and the regulatory policies regarding maximum voltage deviations (Equations (8) and (9)).

$$-I_l^{\max} \leq I_l \leq I_l^{\max}, \quad \forall l \in \mathcal{L}, \quad (8)$$

$$V_k^{\min} \leq V_k \leq V_k^{\max}, \quad \forall k \in \mathcal{N}, \quad (9)$$

where $I_l^{\max}$ represents the maximum thermal limit of the conductor associated with branch l , and $V_k^{\min}$ and $V_k^{\max}$ represent the minimum and maximum voltage bounds allowed in all the nodes of the network.

Fifth, to ensure that the resulting configuration of the distribution network is radial, a constraint is imposed in the number of conductors that can be connected to the distribution (Equation (10)).

$$\sum_{l \in \mathcal{L}} y_l = |\mathcal{N}| - 1, \quad (10)$$

where $|\mathcal{N}|$ represents the cardinality of the set of nodes, i.e., the number of elements in this set.

The interpretation of the mathematical model in Equations (1) to (10) that represents the problem of the optimal reconfiguration of AC distribution networks has the following description: Equation (1) corresponds to the objective function associated with the power losses minimization in all the branches of the network. Equations (2) and (3) determine the active and reactive power balance in all the nodes of the network. These Equations are widely-known in the specialized literature as power flow constraints. Equations (4) and (5) calculate the real and imaginary components of the currents that flow at each branch. Equations (6) and (7) determine the magnitude of the network variables, i.e., voltages in all the nodes and currents in all the branches. Equations (8) and (9) allow for solutions that fulfill the thermal capabilities of the calibers associated with each branch and the voltage regulation bounds permitted in all the nodes. Finally, Equation (10) defines that the number of branches that can be connected produces a radial configuration. Nevertheless, this radial structure is ensured by the presence of the active

and reactive power balance equations in the mathematical model, i.e., Equations (2) and (3) and the number of conductors available for operation, i.e., constraint (10).

Remark 1. The mathematical formulation presented in Equations (1) to (10) is not unique, since multiple representations can be reached by representing the real and imaginary parts of the currents as a combination of magnitudes and angles, i.e., trigonometric functions. However, these trigonometric functions introduce complex nonlinearities that can make the solution to the problem difficult.

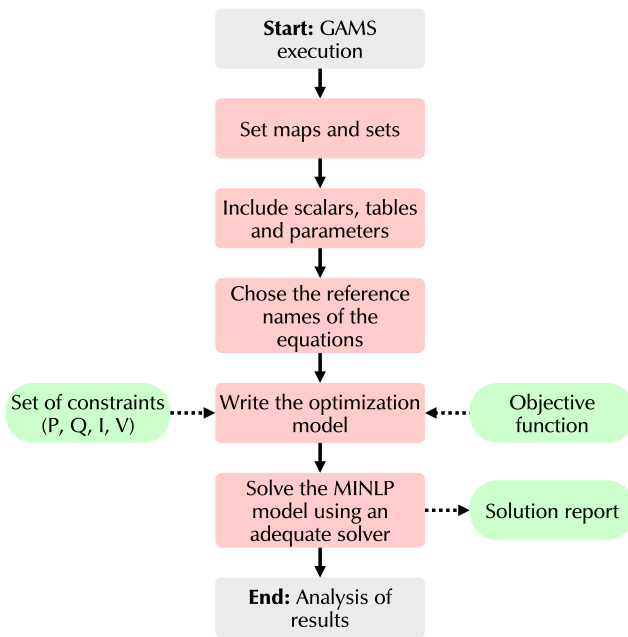
Solution methodology: GAMS software

This section presents the optimization strategy adopted to solve the problem of the optimal reconfiguration of AC networks with an MINLP model described in Equations (1) to (10). To this effect, the general algebraic modeling system is used as a solution technique. The GAMS software is a powerful tool that allows solving complex optimization models including linear and mixed-integer programming, quadratic programming and general nonlinear programming models with mixed variables (i.e., binary, integer) (Soroudi, 2017).

In the specialized literature, GAMS has been employed to solve complex optimization problems such as the optimal selection of conductors in distribution networks (Montoya et al., 2018), optimal planning of transmission networks (Aguado et al., 2017), optimal location of renewable generation in distribution networks (Babu and Singh, 2016; Gil-González et al., 2020; Montoya et al., 2020a), optimal operation of power systems with batteries (Soroudi, 2017; Montoya et al., 2020c), optimal design, and sizing of a pressure retarded osmosis power plant (Naghiloo et al., 2015), voltage stability analysis in direct current networks (Amin et al., 2019), multi-objective optimization of the stack of a thermoacoustic engine (Tartibu et al., 2015), multi-objective optimization of energy and water management in networked hubs (Pakdel et al., 2020), the optimal location of protective devices (Izadi et al., 2019; Gallego-Londoño et al., 2016), and so on.

The main advantages of using the GAMS software in mathematical optimization can be summarized as follows (Montoya et al., 2020c; Soroudi, 2017; Vargas-RObayo et al., 2021):

- ✓ It works with a compact structure, i.e., it employs sets that contain information regarding the number of variables as well as the dimension of the solution space.
- ✓ The information related to the system is introduced by using matrices, vectors, and scalars, and these can be assigned to the set's domain.
- ✓ It uses a symbolic representation of the variables to mathematically represent the optimization model under study, with the characteristic that the model has a pretty similar structure as presented in Equations (1) to (10).
- ✓ It is possible to differentiate the nature of the variables that intervene in the mathematical model, i.e., discrete



Source: Authors

Figure 1. Flowchart for optimal reconfiguration using GAMS

(integer), binary, continuous, and positive variables, among others.

- ✓ Multiple solution techniques based on interior point and branch and bounds methods can be selected to resolve the mathematical optimization model. Some of the classical natures of problems are linear programming (LP), nonlinear programming (NLP), mixed-integer programming (MIP), and mixed-integer nonlinear programming (MINLP).

Figure 1 presents the flowchart for the implementation of optimal reconfiguration in radial distribution networks using MINLP through GAMS. To illustrate an implementation of a mathematical model using the GAMS software, let us consider a small optimization example consisting of an AC distribution network operated at 13,2 kV with 5 nodes, 4 built lines, and 3 tie lines. The electrical configuration is depicted in Figure 2. The initial power losses in this system with the configuration depicted in said Figure are 222,842 kW, and the minimum voltage profile occurs in node 5 with a value of 0,952 pu.

The load information of this test feeder is reported in Table 1, and the branch data including connected and tie lines are presented in Table 2.

Table 1. Load information for the 5-node test feeder

Node	Active power [kW]	Reactive power [kVAr]
1	0	0
2	1 625	520
3	2 250	745
4	2 265	896
5	1 450	1 000

Source: Authors

It is worth mentioning that lines *e*, *f*, and *g* represent the subset of possible links to reconfigure the AC

Table 2. Branch information

Line	Resistance [Ω]	Reactance [Ω]
a	0,3414	0,4127
b	0,6467	0,6051
c	0,2540	0,5526
d	0,2469	0,8050
e	0,8245	0,9656
f	0,1525	0,4565
g	0,3548	0,6885

Source: Authors

distribution system by always guaranteeing a radial topology. In addition, the incidence node-to-branch matrix that represents this test feeder has the following structure:

$$\mathcal{A} = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 & 0 \\ -1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 & -1 & 0 & 1 \\ 0 & 0 & -1 & 0 & 0 & -1 & -1 \end{bmatrix}$$

where it was assumed that the currents flow from the smallest to the highest by rearranging the columns from lines *a* to *g* and the rows from node 1 to node 5.

The implementation of the mathematical model from Equations (1) to (10) to solve the reconfiguration problem in AC networks using GAMS is presented in Algorithm 1. Note that 13,2 kV and 1 000 kVA are used to obtain a per-unit (pu) representation of the system.

The information in Algorithm 1 can interpreted as follows:

- ✓ Lines 1 to 5 determine the sets in the optimization problems, i.e., nodes, lines, and generators, including the map that defines the location of the slack source.
- ✓ Lines 6 to 31 define all the constant information related to the test feeder, i.e., voltage ranges, and branch and load parameters.
- ✓ Lines 32 to 44 define the variables of the problem, i.e., voltages, currents, active and reactive power generations, and binary variables, as well as their constant bounds.
- ✓ Lines 45 to 61 are the necessary equations to solve the problem, starting by their names and followed by their mathematical structures.
- ✓ Lines 62 to 64 present the solution of the problem by defining its nature and selecting the minimization strategy. In addition, the variables of interest are extracted to analyze the final solution.

The solver used to reach the optimal solution of the AC reconfiguration problem in the 5-node test feeder corresponds to the DICOPT taking an average processing time of 1,40 s, which is fastest than any heuristic optimization approach. Figure 3 reports the final solution reached by GAMS, where lines *d* and *f* have been disconnected, and lines *c* and *e* are introduced in the final solution. The last power losses are 124,420 kW, which implies a reduction of about 44, 17% regarding the base case.

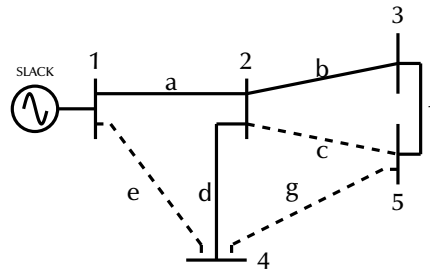
Algorithm 1 Implementation of the reconfiguration problem in the 5-node test feeder

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1 SETS
2 k Set of nodes /N1*N5/
3 l Set of braches /a,b,c,d,e,f,g/
4 g Set of conv. generators /G1/
5 map(g,k) Association nodes-gen /G1.N1/;
6 SCALARS
7 Vmin Minimum voltage [pu] /0.90/
8 Vmax Maximum voltage [pu] /1.10/
9 TABLE LOAD(k,*) Active and reactive power loads [kVA]
10 Pd Qd
11 N1 0 0
12 N2 1.625 0.520
13 N3 2.250 0.745
14 N4 2.265 0.896
15 N5 1.450 1.000;
16 TABLE A(k,l)
17 a b c d e f g
18 N1 1 0 0 0 1 0 0
19 N2 -1 1 1 1 0 0 0
20 N3 0 -1 0 0 0 1 0
21 N4 0 0 0 -1 -1 0 1
22 N5 0 0 -1 0 0 -1 -1;
23 TABLE LINES(l,*) [Ohm]
24 Rl Xl
25 a 0.001959366391185 0.002368572084481
26 b 0.003711547291093 0.003472796143251
27 c 0.001457759412305 0.003171487603306
28 d 0.001417011019284 0.004620064279155
29 e 0.004731978879706 0.005541781450872
30 f 0.000875229568411 0.002619949494949
31 g 0.002036271808999 0.003951446280992;
32 VARIABLES
33 z Objective function value
34 v(k) Voltage magnitude at node k.
35 vr(k) Real part of the voltage at node k.
36 vi(k) Imag. part of the voltage at node k.
37 l(l) Current maginitude in brach l.
38 lr(l) Real part of the current in brach l.
39 li(l) Imag. part of the current in brach l.
40 Pg(g) Active power generation in the Conv. Gen.
41 Qg(g) Reactive power generation in the Conv. Gen.
42 BINARY VARIABLES
43 y(l) Selection of the branch l.;
44 v.lo(k) = Vmin; v.up(k) = Vmax; vr.lo(k) = Vmin/2; vi.fx('N1') = 0; vr.fx('N1') = 1;
45 EQUATIONS
46 ObjFun Objective function
47 BalP(k) Active power balance per node.
48 BalQ(k) Active power balance per node.
49 Curr(l) Real current in branch l.
50 Curi(l) Imag. current in branch l.
51 Cur(l) Magnitude of the current in branch l.
52 Vol(k) Magnitude of the voltage.
53 NLines Number of lines;
54 ObjFun.. z =E= sum(l,LINES(l,'Rl')*sqr(l(l)));
55 BalP(k).. SUM(g$map(g,k),Pg(g))-LOAD(k,'Pd')=E= SUM(l,A(k,l)*(vr(k)*lr(l) + vi(k)*li(l)));
56 BalQ(k).. SUM(g$map(g,k),Qg(g))-LOAD(k,'Qd')=E= -SUM(l,A(k,l)*(vr(k)*li(l) - vi(k)*lr(l)));
57 Curr(l).. lr(l) =E= (y(l)/(sqr(LINES(l,'Rl')) + sqr(LINES(l,'Xl'))))*SUM(k,A(k,l)*(LINES(l,'Rl')*vr(k)
+ LINES(l,'Xl')*vi(k)));
58 Curi(l).. li(l) =E= (y(l)/(sqr(LINES(l,'Rl')) + sqr(LINES(l,'Xl'))))*SUM(k,A(k,l)*(LINES(l,'Rl')*vi(k)
- LINES(l,'Xl')*vr(k)));
59 Vol(k).. v(k) =E= sqrt(sqr(vr(k)) + sqr(vi(k)));
60 Cur(l).. l(l) =E= sqrt(sqr(lr(l)) + sqr(li(l)));
61 NLines.. SUM(l,y(l)) =E= card(k) - 1;
62 MODEL Reconfiguration /ALL/;
63 SOLVE Reconfiguration us MINLP min z;
64 DISPLAY z.l, pg.l, y.l, v.l, vr.l, vi.l, l.l;

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Source: Authors



Source: Authors

Figure 2. 5-node test system to illustrate the AC reconfiguration problem

Source: Authors

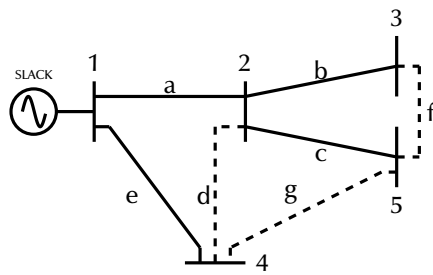


Figure 3. 5-node test system solution after optimal reconfiguration

Source: Authors

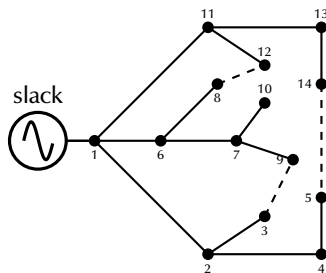


Figure 4. Electrical configuration of a radial distribution network

Source: Authors

It is important to mention that the implementation reported in Algorithm 1 can be applied to any AC distribution networks, regardless of the number of nodes and candidate lines, since it presents a compact structure for optimization, which is one of the most important and largely-known advantages of the GAMS software (Soroudi, 2017).

Numerical validation

In this section, in order to demonstrate the efficiency of the proposed approach for the optimal reconfiguration of AC distribution systems, the classical medium voltage distribution network composed by 14-nodes and 16 lines reported in (Tapia-Juárez and Espinosa-Juárez, 2013) is employed (Figure 4). This system is operated at 23 kV, and the based power is assumed to be 1 000 kVA. The initial active power losses for this test feeder are 512,165 kW. The information on the connected and candidate branches is reported in Table 3, and the load information is listed in Table 4.

Table 3. Branches information for the 14-node test feeder

Node i	Node j	Resistance [Ω]	Reactance [Ω]
Connected lines			
1	2	0,39675	0,5290
2	3	0,4232	0,5819
2	4	0,4761	0,9522
4	5	0,2116	0,2116
1	6	0,5819	0,5819
6	7	0,4232	0,5819
6	8	0,5819	0,5819
7	9	0,5819	0,5819
7	10	0,4232	0,5819
1	11	0,5819	0,5819
11	12	0,4761	0,6348
11	13	0,4232	0,5819
13	14	0,2116	0,2116
Tie lines			
3	9	0,2116	0,2116
8	12	0,2116	0,2116
5	14	0,4761	0,6348

Source: Authors

Table 4. Load information for the 14-node test feeder

Node	Active power [kW]	Reactive power [kVAr]
1	0,00	0,00
2	2 000	1 600
3	3 000	400
4	2 000	-400
5	1 500	1 200
6	4 000	2 700
7	5 000	1 800
8	1 000	900
9	600	-400
10	4 500	-1 700
11	1 000	900
12	1 000	-1 100
13	1 000	900
14	2 100	-800

Source: Authors

In this test system, we evaluate three simulation cases as follows:

- ✓ **Scenario 1 (S1):** The reconfiguration of this test feeder considering that all the tie lines are initially disconnected.

- ✓ **Scenario 2 (S2):** The reconfiguration of this test feeder considering the presence of a distributed generator at node 8 with a capacity of 10 MW operated with unity power factor.
- ✓ **Scenario 3 (S3):** The reconfiguration of this test feeder considering the presence of a large-scale capacitor compensation at node 6 with a size of 6 MVar.

Note that the first simulation scenario is the typical simulation case explored in the specialized literature for the optimal reconfiguration of the 14-node test feeder using metaheuristic techniques (Verma and Singh, 2018).

Table 5 presents the solution of the reconfiguration problem in the 14-node test feeder considering **S1**, where GA means genetic algorithm (Su et al., 2005), ACSA means ant colony search algorithm (Su et al., 2005), GAST means genetic algorithms based on spanning trees (Zhang et al., 2014), and MCA means modified culture algorithm (Verma and Singh, 2018). It is worth mentioning that Verma and Singh (2018) claim an optimal value of about 462 kW regarding power losses. However, this is not possible for this system, since, when we evaluated their solution, it turned out to be 466,47 kW.

From the results in Table 5, we can note the following. *i)* All the comparative methodologies, as well as the proposed MINLP model, solved in GAMS reach the same optimal solution (466,467 kW), which corresponds to a reduction of about 8,89% with respect to the base case. *ii)* Of the methods identified in the state of the art for the comparative analysis, none recorded the total calculation time. The state of the art was reviewed according to this work's contribution, objective, and motivation. It is relevant to highlight that the methods studied in this research are not the only strategies available for the optimal reconfiguration of radial networks. Therefore, it is likely that other solution methods do include runtime analysis. In the case of the proposed approach, this takes about 11,560 s, which is a short time for solving MINLP models. This is important since the utility can make multiple simulations before making a final decision regarding investment and grid intervention. *iii)* The solution reached by the GAMS package is obtained by using an interior-point optimization method combined with the branch and bound strategy, which makes it efficient in terms of quality response and computational effort (Kaur et al., 2014; Montoya et al., 2020c).

In the case of **S2**, the initial power losses considering the operation of the distributed generator with 10 MW with the initial topology of the system presented in Figure 4 are 364,057 kW. Once the mathematical formulation is solved by the GAMS package, the final power losses are 339,133 kW, which implies an improvement regarding power losses of about 24,924 kW. To reach this solution, the set of the disconnected lines are {4 – 5, 7 – 9, 11 – 12}, which is a solution found in approximately 15,50 s. This implies that the presence of the distributed generator does not significantly affect the complexity of the optimization problem under study in terms of the processing times.

As for **S3**, the initial power losses considering the initial topology depicted in Figure 4 and a capacitive compensation of 6 MVar at node 6 are 500,697. Once the proposed methodology for optimal reconfiguration in AC networks

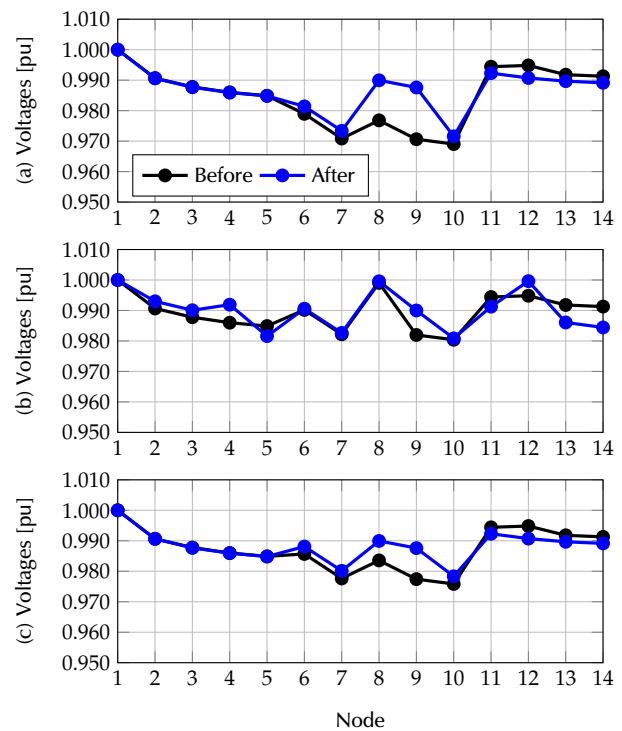


Figure 5. Voltage behavior in the nodes of the 14-node test feeder for each one of the simulation scenarios: (a) **S1**, (b) **S2**, and (c) **S3**

Source: Authors

is solved through GAMS, the resulting power losses are 463,039 kW, which means a reduction of 7,52% with respect to the initial case. Note that the disconnected lines are {6 – 8, 7 – 9, 5 – 14}, which agrees with the optimal solution for **S1**. In this problem, the GAMS package takes about 6 s to find the optimal solution, which confirms its effectiveness at analyzing complex MINLP models (Soroudi, 2017).

Remark 2. Note that the punctual injection of active and reactive power in specific nodes significantly influences the power loss behavior of the network, as it can be observed in the initial cases of **S2** and **S3**. However, the reconfiguration strategy applied to the test system considering these distributed energy resources can also help mitigate the negative effects produced by excessive injections of active and reactive power into the grid.

Figure 5 reports the voltage profiles for the 14-node test feeder in all the simulation scenarios including their base cases.

From Figure 5, we can observe that *i)* the reconfiguration of the AC distribution network allows improving the average voltages in all the nodes of the system, given that the reduction of power losses translates into lower voltage drops. Nevertheless, this does not imply that the worst voltage profile will improve, since the mathematical model presented in this paper is strongly nonlinear and non-convex, as seen in Figure 5b. *ii)* The presence of distributed generation and/or capacitor banks has a higher impact on the voltage profiles of the network (compare Figures 5b and 5c with 5a), which is expected in distribution networks since these largely modify the total power injection in the substation, whereas reconfiguration only redistributes those fluxes in a better way, regardless of the presence of shunt

Table 5. Solutions for **S1**

Method	Power losses [kW]	Disconnected lines	Proc. Time [s]
GA	466,470	{6 – 8, 7 – 9, 5 – 14}	–
ACSA	466,470	{6 – 8, 7 – 9, 5 – 14}	–
GAST	466,470	{6 – 8, 7 – 9, 5 – 14}	–
MCA	466,470	{6 – 8, 7 – 9, 5 – 14}	–
GAMS	466,467	{6 – 8, 7 – 9, 5 – 14}	11,560

Source: Authors

elements, *i.e.*, distributed generators and/or capacitor banks. *iii)* The reconfiguration of the network has positive impacts since it allows for further reduction in power losses, thus making it attractive for utilities regarding power quality and regulatory benefits via billing, as is the case of Colombian companies (Sánchez-Zuleta *et al.*, 2017).

Remark 3. *The effect of current constraints (6) and (8) can be considered for optimal reconfiguration in AC distribution networks if there is information available regarding the maximum thermal capabilities of the existing and tie lines, since the proposed rectangular representation of this problem allows evaluating it easily, due to the fact that our model is defined as a function of the branch currents, which implies that the information of the current magnitudes in all the branches is always available.*

In order to provide enough information to analyze the current flows in the 14-node test feeder, Table 6 presents the current magnitudes in this test system for each of the simulation scenarios.

From the results in Table 6, we can observe that each one of the reconfiguration planes provided by each simulation scenario effectively helps to redistribute the current flow in all the lines, which is directly connected to the power loss improvement. For example, in **S1**, if it is supposed that lines 1–6 have a current rate of 700 A, then, its loadability is about 98, 95% in the initial case. Nevertheless, after the application of the reconfiguration strategy, the final loadability is about 88, 03%, implying a liberation of capability of 10%, which can be used in the case of loads attended by this line that report increments in the near future. However, the discharge in this distribution line implies a loadability increment in some other lines to guarantee that the amount of power provided to the loads is satisfied. However, these increments in some lines are not a negative effect, since the global behavior of the network demonstrates that the power losses are reduced. This behavior is attributable to the nonlinear properties of the optimization problem analyzed in this research. Note that similar analyses can be made for **S2** and **S3** regarding their base cases.

Conclusions and future work

This paper proposes a new mathematical formulation to model the problem of the optimal reconfiguration of AC distribution feeders based on a rectangular representation of the voltage and current variables in nodes and branches, respectively. Due to the nature of the MINLP model's results, the GAMS package was selected as solution methodology since the main focus of this paper was indeed the mathematical formulation, not the solution technique. We presented the methodology in the style of a tutorial to

help engineering students understand the real complexity of the reconfiguration problem in AC distribution feeders.

The numerical results in the case under study (14-node test feeder) for all the simulation scenarios demonstrated that the reconfiguration of the system (modification of the topology) has positive impacts regarding power losses minimization, regardless of the presence of distributed energy resources in the grid, *i.e.*, distributed generators and/or capacitor banks. This implies that the proposed approach is suitable to be extended to electrical distribution networks with batteries and economic dispatch multi-period environments.

There is an alternative way to represent the reconfiguration problem in AC networks by using the magnitude of the nodal voltages and their angles. Nevertheless, that approach introduces complex characteristics in the model concerning trigonometric functions that relate voltages and currents in the power balance constraints. Said approach is less efficient than the rectangular representation proposed in this paper. It can multiply the possibilities of getting stuck in the local optimums, primarily when packages such as GAMS are used as solution methodology.

This work analyzes the problem of optimal reconfiguration in distribution networks using variables as electrical parameters, specifically power, voltage, and current. As future work, in the area of optimization for power systems, several variables can be implemented in the objective function and the constraints model. Likewise, criteria associated with social impacts can be included, thus allowing to analyze how the reconfiguration of networks, the inclusion of renewable energy sources, the implementation of storage systems, and others contribute to sustainable development.

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Table 6. Current behavior in the 14-node test system

Node		S1		S2		S3	
<i>i</i>	<i>j</i>	Before	After	Before	After	Before	After
1	2	394,1332	414,5480	394,1332	337,6734	394,1332	414,5480
2	3	133,2162	158,4840	133,2162	158,0997	133,2162	158,4840
2	4	158,3968	158,4072	158,3968	89,4029	158,3968	158,4072
4	5	84,8000	84,8056	84,8000	—	84,8000	84,8056
1	6	692,6546	616,1869	279,5282	277,4053	680,2022	613,2501
6	7	453,3914	425,2542	448,1370	421,2268	450,2295	422,3069
6	8	59,8829	—	393,6306	348,0422	59,4720	—
7	9	32,3017	—	31,9286	—	32,0772	—
7	10	215,8304	215,2670	213,3294	213,2291	214,3254	213,7757
1	11	223,5337	270,2963	223,5337	265,6106	223,5337	270,2963
11	12	64,9702	88,2380	64,9702	—	64,9702	88,2380
11	13	136,0605	136,3538	136,0605	211,2690	136,0605	136,3538
13	14	98,5651	98,7775	98,5651	160,1499	98,5651	98,7775
3	9	—	31,7464	—	31,6694	—	31,7464
8	12	—	59,0878	—	64,6598	—	59,0878
5	14	—	—	—	85,0858	—	—

Source: Authors

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**On the Optimal Reconfiguration of Radial AC Distribution
Networks Using an MINLP Formulation: A GAMS-Based
Approach**

**Sobre la reconfiguración óptima de redes radiales de
distribución empleando un modelo de PNLEM: un
enfoque basado en GAMS**

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