



Revista de la Construcción

ISSN: 0717-7925

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Pontificia Universidad Católica de Chile
Chile

i Ginovart, Josep Lluís; Coll-Pla, Sergio; Costa-Jover, Agustí; López Piquer, Mónica
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Revista de la Construcción, vol. 16, núm. 3, 2017, pp. 468-478
Pontificia Universidad Católica de Chile
Santiago, Chile

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Evaluation of large deformations on Romanesque masonry pillars: The case of Santa María de Arties (XII-XIII) at Valle de Arán, Spain

Análisis de grandes deformaciones en pilares de obra de fábrica románicos: el caso de Santa María de Arties (XII-XIII) en el Valle de Arán, España

Josep Lluís i Ginovart (Main and Corresponding Author)

Universitat Internacional de Catalunya (UIC)
C/ Immaculada 22, 08017 Barcelona (Spain)
jlluisg@uic.es

Sergio Coll-Pla

Universitat Rovira i Virgili (URV)
Av/ Universitat 1, 43204 Reus (Spain)
sergio.coll@urv.cat

Agustí Costa-Jover

Universitat Rovira i Virgili (URV)
Av/ Universitat 1, 43204 Reus (Spain)
agusti.costa@urv.cat

Mónica López Piquer

Universitat Internacional de Catalunya (UIC)
C/ Immaculada 22, 08017 Barcelona (Spain)
mlopezp@uic.es

Manuscript Code: 810

Date of Acceptance/Reception: 12.11.2017/09.09.2016

DOI: 10.7764/RDLC.16.3.468

Abstract

There is a set of Romanesque churches at Valle de Aran that were built between the eleventh and thirteenth centuries; these churches have suffered large deformations and geometrical displacements. These deformations have provoked, in some cases, convex shapes to appear, in relation to the generatrix of the vaults, which have the inverted shape of an arch. Geometrical assessment of the least rigid elements, the pillars, makes it possible to analyse the displacements, which have been the cause of funicular shapes on some vaults. It is possible to deduce the regression plane of the displacements of the pillars of the central nave and to define the deformation vectors over it. Thus, these data reveal the directions of the deformations of vaults and pillars to be determined. The deformations of the pillars are not perpendicular to the directrix of the central vault, so the methodology and results can be very useful to understand the nature of the displacements and to maintain these masonry structures.

Key words: Romanesque, masonry, barrel vault, pillar, great deformations, Valle de Arán.

Resumen

En el Valle de Arán existe un conjunto de iglesias románicas que fueron construidas entre los siglos XI y XIII; estas iglesias han sufrido grandes deformaciones y desplazamientos geométricos. Estas deformaciones han provocado que, en algunos casos, que aparezcan formas convexas, en relación con la generatriz de las bóvedas, que tienen la forma invertida de un arco. La evaluación geométrica de los elementos menos rígidos, los pilares, permite analizar los desplazamientos, que han sido la causa de las formas funiculares en algunas bóvedas. Es posible deducir el plano de regresión de los desplazamientos de los pilares de la nave central y definir los vectores de deformación sobre ella. Así, esta información permite determinar la dirección de las deformaciones de bóvedas y pilares. Las deformaciones de los pilares no son perpendiculares a la directriz de la bóveda central, por lo que la metodología y los resultados pueden ser muy útiles para comprender la naturaleza de los desplazamientos y para mantener estas estructuras de mampostería.

Palabras clave: Románico, obra de fábrica, bóveda de cañón, pilar, grandes deformaciones, Valle de Arán.

Introduction and Description of the problem

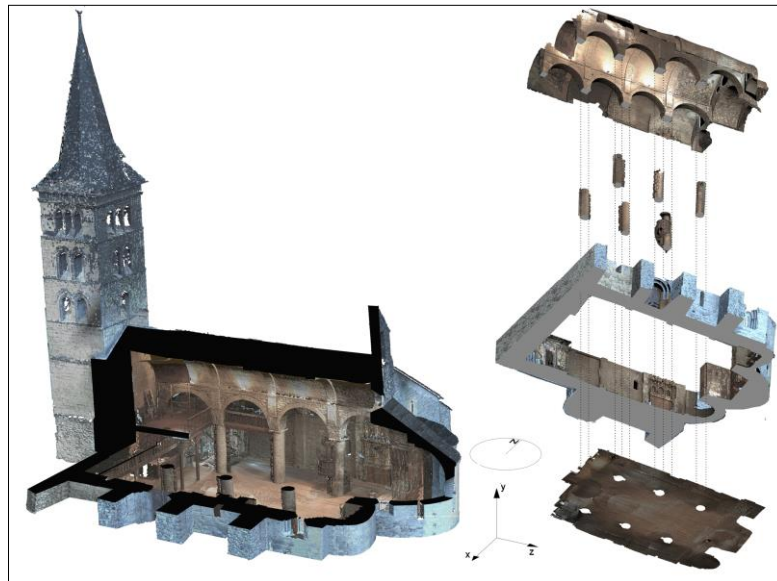
The great deformations of the Valle de Aran Romanesque

The churches of Valle de Aran are located at the Spanish Pyrenees and were built between twelfth and thirteenth centuries. One of the main features of these buildings is the large deformations of the masonry structure. One of the most deformed buildings is the church of Santa Maria de Arties (XII) (Figure 1), which is a basilica floor plan with a central

nave and two collaterals, each with four bays. The central pillars support the formerets under the barrel vault and the lateral half-vaults that supports over perimeter walls. The heading is currently finished with a semicircular apse, reconstructed during last years, and the two original apsidioles. All of them are covered with hemispherical domes.

The structure presents a typical deformation pattern: leaning of vertical elements towards the outside because of vaults thrust, and settlement of vaults, which have caused the apparition of funicular shapes, which is the inverse of the natural shape of an arch since it is convex in relation to its generatrix. One of the causes of these deformations is the displacement of the pillars since these are the least rigid elements of the structure. The investigation focuses on the geometrical parametrization and evaluation of these movements. Previous investigations focused on the assessment of the overall structure, in order to understand the stability conditions (Costa-Jover, Lluís i Ginovart, Fortuny-Anguera, & Coll-Pla, 2014; Costa Jover & Coll Pla, 2017), which revealed that masonry is working to the limit due to the deformations suffered, while the origin of the movements can be explained by rigidity issues.

Figure 1. Santa María of Arties (2015). Source: authors.



State of the Art

Due to the large deformations, these Romanesque constructions were assessed by several authors, such as Emmanuel Viollet-le-Duc (1814-1879), who visited Bossost (1883) (Español, 2011), and later by Lluís Domènech i Montaner (1850-1923), who was Dean of the Escuela de Arquitectura de Barcelona (1905) (Granell & Ramon, 2006). Subsequently, the *Institut d'Estudis Catalans* organized an expedition with the combined historical and archaeological purpose of visiting the Valle de Aran and La Ribagorça (1907). Two of the participants were the architects Josep Puig i Cadafalch (1867-1956) and Josep Goday i Casals (1881-1936) (Alcolea Blanch, 2008), who suggested that these churches were initially covered with timber structures, which were later replaced by masonry barrel vaults (Puig i Cadafalch, 1908).

Juan Bassegoda i Nonell (1930-2012) stated that formal anomalies are a defining characteristic of the Catalan Romanesque architecture (Bassegoda, 1974). The case study presented in this paper focuses on the church of Santa Maria d'Arties, which is the most assessed building of this group. Its great deformations were identified during the restoration work of the 70s (Bassegoda, 1972; Saez, 1976). Afterwards, José Luis Villanueva i noted the existence of the funicular shapes (Villanueva, 1974), and in 2009, the structure was assessed by means of finite elements (FEM) by the team of Joan Polo i Berroy (Polo, 2009).

Otherwise, the architectural heritage topographic documentation is a key tool for its preservation. Current techniques of Massive Data Capture (MDC), such as digital photogrammetry and terrestrial laser scanner, have become widespread in the assessment of built heritage (Kadobayashi, Kochi, Otani, & Furukawa, 2004; Yilmaz, Yakar, Gulec, & Dulgerler, 2007). Numerous investigations have tested the technique's reliability (Grussenmeyer, Landes, Voegtli, & Ringle, 2008), (Vendrell, Giráldez, González, Cavallé, & Roca, 2008), and has proven their effectiveness to survey the building's geometry with high precision. The point clouds make it possible to detect and monitor degradation processes and formal anomalies. Other applications goes from heritage documentation (Dhonju, Xiao, Shakya, Mills, & Sarhosis, 2017; H. K. Dhonju, W. Xiao, V. Sarhosis, J. P. Mills, S. Wilkinson, Z. Wang, L. Thapa, 2017) to deepen in the history and buildings constructions (Benito, 2011; Sternberg, 2006) between many others.

The specific issue of deformation assessment is essential for architectural heritage conservation, and many studies have developed simple procedures to address that issue from the 3D topographical information of the point clouds, i.e. the Cathedral of St. Johannis in Meldorf (Quagliarini, Clini, & Ripanti, 2016), the churches of Santa Maria in Portonovo (Bonali, Pesci, Casula, & Boschi, 2014) and Cantalovo (Pesci, Bonali, Galli, & Boschi, 2012) or the Palazzo d'Accursio (Costa-Jover, Lluís i Ginovart, Fortuny-Anguera, & Coll-Pla, 2014; Costa Jover & Coll Pla, 2017), all in Italy. Those investigation focuses on the assessment of vertical elements deformations, except the Portonovo's case, where a simple assessment of the cylindrical barrel vaults is performed from standard primitives.

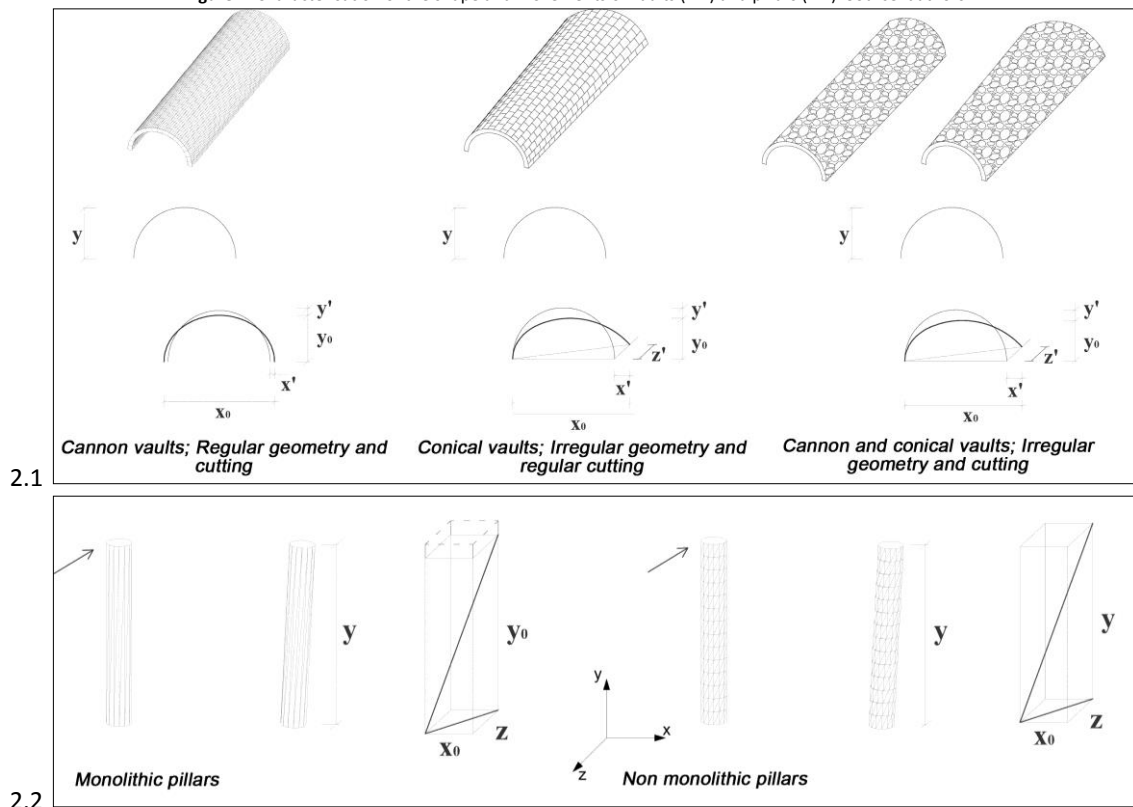
Methodology

Theoretical framework: systematization of the deformations on vaults and pillars

In order to establish the general theoretical framework, the assessment of the shapes can only be understood in three dimensions. From the point of view of historiography, Emmanuel Viollet-le-Duc (1814-1879) assessed the barrel vaults and the abutment with timber beams with precision (Viollet-le-Duc, 1868). Afterwards, August Choisy (1841-1909) did not explain the Romanesque vaults, but did explain the origin of barrel vaults from Roman construction with brick and concrete (Auguste Choisy, 1873). He referred to the byzantine influence on construction with or without centering (A Choisy, 1883). Otherwise, in the work *Historia General del Arte* (1901), Josep Puig i Cadafalch described the great difference between the Romanesque vaults, where stability is the main concept inherited from roman vaults, which were significantly more monolithic (Puig i Cadafalch, 1901).

When the geometry of these vaults is regular and the construction is monolithic due to the masonry configuration, the thrust is perpendicular to the central guideline of the vault. Conversely, barrel vaults of Valle de Aran churches have specific features. These are conical vaults, as was theorised by Joan Bassegoda (1974), and the stone-cutting is not regular, as stated by Josep Puig i Cadafalch (1901). Finally, the supports of the vaults, external walls and arches, have different stiffness, as noted by Luis Villanueva (1974). Those three conditions are far from the general theory of the thrust of homogeneous vaults with cylindrical guideline. In addition, the assessment of the pillar deformations and their stiffness is influenced by the contributions of Josep Puig i Cadafalch (1908).

Figure 2. Characterisation of the shape and movements of vaults (2.1) and pillars (2.2). Source: authors.



In any or in a combination of the precedent hypotheses, thrusts have two directions (x, z) as long as the supports stand still. Thus, the resultant thrust is not perpendicular to the guideline of the vault (Figure 2.1), and deformations can

appear on two directions. Vaults thrusts are transmitted to vertical structural elements. The vaults of the central nave are supported by the walls over formerets, which at the same time are supported by the pillars of the central nave. Thus, the vertical elements can deform over the three planes.

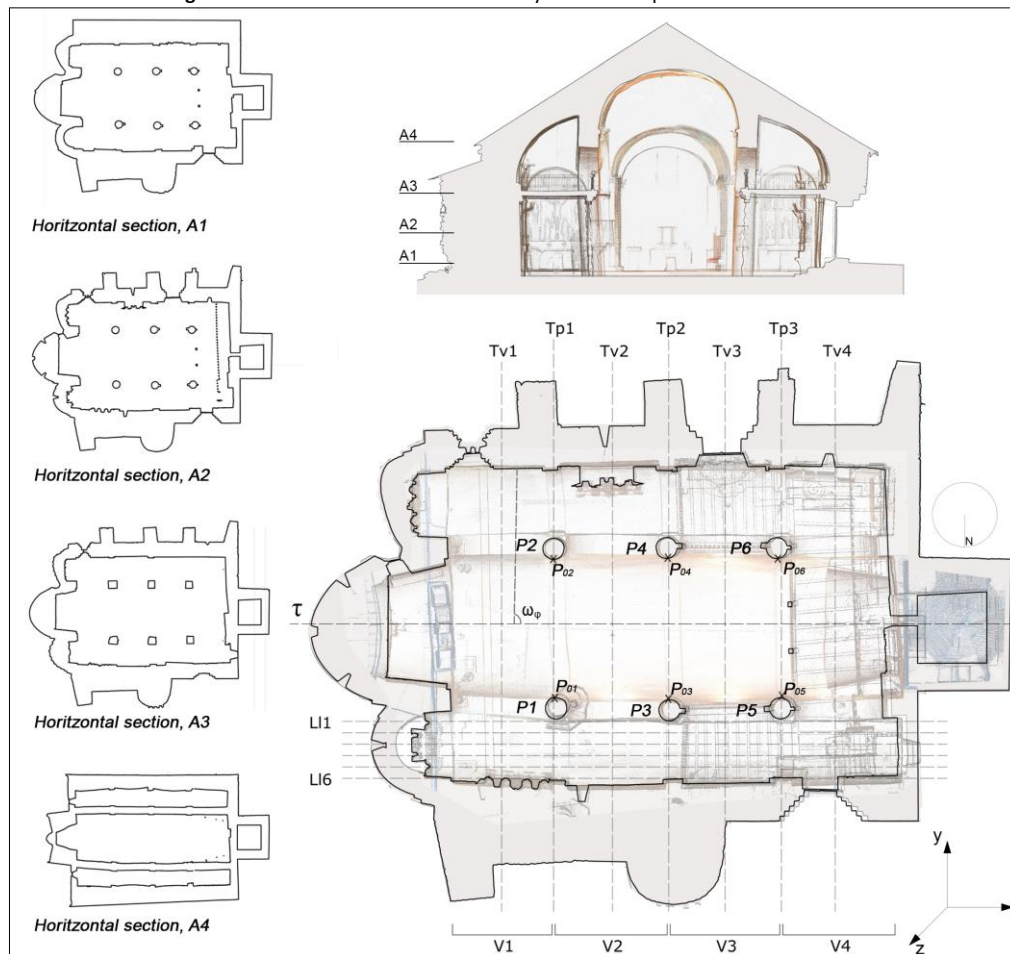
The deformations of the pillars are directly related to the stone cutting and mortar of the pillar, and the thrusts received from the irregular shape of the vault. A monolithic, infinitely rigid pillar tends to rotate on its base. The upper part moves over the axis (x) towards the exterior due to the main horizontal thrust with the consequence that there is also movement in the axis (y) since their extreme upper part declines. Finally, there is also movement over axis (z) (Figure 2.2).

If pillars are not monolithic and are built with numerous joints, they tend to deform in the upper part. If we suppose that the extremes of the vaults have not suffered differential settlements and that the movement of these extremes is thus ($\Delta y=0$), then the deformations are $df_p(df_{px}, 0, df_{pz})$, which is the hypothesis of the present case study. There can be a combination of rotations and translations

The geometrical assessment of the pillars

The assessment is based on a three-dimensional model of the church os Santa María de Arties (Figure 3) obtained with a terrestrial laser scanner (TLS). It is a contactless, non-invasive surveying technique that makes it possible the massive capture of geometric and radiometric data of a given surface (Pesci, Bonali, Galli, & Boschi, 2012). Thus, it allows a quick and easy capture of the geometry of objects. The main limitations lie in the management of dense point clouds, the texturization of surfaces and the need to place the device in a stable position. In addition, cost is a very important limiting factor (Lluís i Ginovart, Costa-Jover, Coll-Pla S., & Puche Fontanilles, 2016).

Figure 3. Santa María de Arties. Planimetry and section planes. Source: authors.



The scanner used is a Leica ScanStation P20, with a bandwidth of 808/658, class 1. The scanning ratio is 1,000,000 points, and the noise at 100 is 9.0 mm for black surfaces, 4.30 mm for grey surfaces, and 1.5 mm for white surfaces. The field

of view is 360° horizontal and 270° vertical. The point cloud is processed with the specific software Cyclone, and after the program 3DReshaper is used to obtain the three-dimensional mesh with an average distance of points of 5 cm, as well as a measure of the triangle for detecting 10 cm holes. The model of the interior of the building has 80.582 points and 156.449 triangles, and the exterior has 314.650 points and 609.472 triangles.

The investigation methodology focuses on the assessment of the geometrical characteristics of the 6 pillars $[P_1...P_6]$ with the objective of studying the displacements that they have suffered (Lluis i Ginovart, Costa, & Coll, 2016). The pillars of the central nave have deformed in a specific way, namely, through the masonry joints (n_s). These joints are perfectly visible on pillars P_3 , P_4 , P_5 and P_6 , while they are more difficult to see on P_1 and P_2 since these pillars are partially covered by mural paintings. The measurement of the displacements suffered by the masonry has to deal with the non-monolithic behaviour of the pillars, so the displacements are not linear along their entire length.

The procedure is based on slicing the pillars on (n_s) rows. Thus, the displacement of each pillar can be deduced according to the coordinates of the centroid of each row (x_{ci} , y_{ci} , z_{ci}), which is calculated from the corresponding polylines through CAD (Computer Aided Design) software.

The centroid of reference (x_{c0} , y_{c0} , z_{c0}) to quantify the displacements of each row is set in the section of the floor plan since it is considered that it would have not suffered any displacements on (x), and ultimately it defines a common criteria to evaluate pillars displacements. The final section is located at the impost of the pillar (x_{cs} , y_{cs} , z_{cs}). The procedure assumes that the original pillars were vertical.

The obtained points makes it possible to deduce the regression plane P_{ri} for each pillar. It is calculated as a function of the (n_i) centroid points of each row. The plane is defined by means of the command "Extract Form" of the program 3DReshaper (www.3dreshaper.com). Thus, the plane that best fits the (n_i) points on each pillar is found. Points are projected perpendicularly over that plane, so it can be defined as a function over plane P_{ri} .

Moreover, it is possible to define a displacement vector contained on each plane $[P_{r1}...P_{r6}]$, so the results can be expressed by a vector with coordinates (x_i , z_i). This vector expresses the direction and magnitude of the deformation, so it has a coordinate (0, 0) in the base of the pillar and another (x_d , z_d) that indicates the displacement of the element. Thus, (x_d) represents horizontal displacement, while (z_d) shows the rotation of the plane in relation to the directrix of the vault. The resultant vector between (0, 0) (which is the centroid in the base of the pillar) and (x_d , z_d) (which is the centroid of the last row of the pillar) represents the total leaning of the element.

The assessment of this displacement vector determines the clearance angle (ω) of the regression plane P_{ri} of the plane over the directrix of the vault (τ) (Figure 2). Thus, this angle can be understood as:

- a) (ω_ϕ) = 90°, perpendicular to the directrix ϕ_1 ,
- b) (ω_ϕ) < 90°, displacement towards the apse,
- c) (ω_ϕ) > 90°, displacement towards the façade.

The data obtained characterizes the general tendency of the deformation of the vaults supported by the pillars. The reparation and containment of these deformations are the cause of the reinforcement of the perimeter walls by means of the construction of buttresses or strategical placement of bell towers, which are usually built in the façade opposite to the apse.

Results

Assessment of the pillars of Santa María de Arties

The assessment of the morphological characteristics of the pillars (Figure 4) is made through the visible elements, such as the masonry joints. Non-visible elements are not considered. Thus, data are obtained according to the centroids of each visible row. Thus, pillars has following rows: ($P_1=26$), ($P_2=26$), ($P_3=27$), ($P_4=25$), ($P_5=23$) and ($P_6=23$). Rows are numbered from bottom to top.

The values of the area, perimeter and height do not show important differences between pillars (Table 1) and (Table 2). The arithmetic mean of the areas (Table 1) is 0.693 m², with a range between $[P_1, P_4]$ of [0.731, 0.678] and a coefficient of variation (from here on C.V.) of 2.77%, so the area of the pillars can be considered to be homogeneous in general terms. The arithmetic mean of the perimeter is 2,981 m, with a range between $[P_1, P_6]$ of [3.060, 2.950] and a C.V. of

1.45%. In conclusion, the sections of pillars P_1 and P_2 , located in the heading of the church, are slightly larger than the rest.

In respect to height (Table 2), the arithmetic mean is 3.840 m, as measured over the current wood floor, and the values have a range of [4.170, 3.587]. There is a slight inclination of the floor towards the presbytery, so pillars by pair are comparably of the same height. Thus, the arithmetic mean of [P_1 , P_2] is 4.055 m, with a C.V. of 4.01%, for pillars [P_3 , P_4], the arithmetic mean is 3.829 m, with a C.V. of 2.18%, and finally, for pillars [P_5 , P_6], the arithmetic mean is 3.636 m, with a C.V. of 1.89%.

Table 1. Morphologic characteristics of the pillars P_i . Area and perimeter. Source: authors.

Pillars	Pillar 1		Pillar 2		Pillar 3		Pillar 4		Pillar 5		Pillar 6	
	Area (m ²)	Perim. (m)	Area (m ²)	Perim. (m)	Area (m ²)	Perim. (m)	Area (m ²)	Perim. (m)	Area (m ²)	Perim. (m)	Area (m ²)	Perim. (m)
Rows												
28	-	-	-	-	-	-	-	-	-	-	-	-
27	-	-	-	-	0.695	2.992	-	-	-	-	-	-
26	0.989	3.932	0.708	3.059	0.697	2.977	-	-	-	-	-	-
25	0.745	3.086	0.700	2.974	0.707	2.994	0.670	2.907	-	-	-	-
24	0.735	3.050	0.690	2.953	0.696	2.968	0.677	2.955	-	-	-	-
23	0.735	3.057	0.697	2.971	0.693	2.966	0.677	2.939	0.678	2.938	0.678	2.947
22	0.737	3.053	0.696	2.972	0.698	2.975	0.674	2.952	0.682	2.937	0.676	3.002
21	0.738	3.057	0.693	2.961	0.693	2.958	0.675	2.951	0.691	2.981	0.674	3.073
20	0.731	3.045	0.692	3.039	0.687	2.952	0.682	2.979	0.683	3.011	0.675	2.924
19	0.733	3.070	0.690	3.053	0.688	2.954	0.669	2.948	0.693	2.978	0.675	2.923
18	0.732	3.054	0.691	3.026	0.686	2.950	0.673	2.918	0.690	2.962	0.678	2.932
17	0.725	3.045	0.693	3.047	0.688	2.952	0.678	2.963	0.689	2.957	0.678	2.996
16	0.718	3.007	0.691	2.955	0.681	2.939	0.681	2.955	0.696	2.971	0.678	2.930
15	0.739	3.059	0.708	2.992	0.680	2.938	0.681	2.969	0.694	2.965	0.679	2.931
14	0.715	3.018	0.714	3.005	0.682	2.942	0.681	2.962	0.700	2.983	0.678	2.930
13	0.711	3.008	0.712	2.999	0.681	2.938	0.684	2.958	0.701	2.992	0.680	2.936
12	0.718	3.014	0.709	3.087	0.687	2.946	0.683	2.961	0.692	2.959	0.679	2.933
11	0.728	3.038	0.702	3.048	0.683	2.940	0.680	2.953	0.685	2.947	0.677	2.927
10	0.728	3.041	0.700	3.006	0.687	2.949	0.679	2.968	0.685	2.947	0.684	2.944
9	0.715	3.011	0.687	3.022	0.685	2.959	0.675	2.947	0.677	2.937	0.683	2.938
8	0.720	3.031	0.694	3.033	0.686	2.945	0.672	2.981	0.683	2.964	0.683	2.940
7	0.715	3.022	0.696	3.057	0.685	2.945	0.674	2.953	0.685	2.944	0.680	2.973
6	0.702	2.995	0.690	3.018	0.686	2.955	0.672	2.937	0.684	2.937	0.682	2.936
5	0.707	3.001	0.681	2.932	0.684	2.942	0.678	2.963	0.681	2.943	0.680	2.938
4	0.702	2.980	0.686	2.944	0.685	2.956	0.680	2.970	0.685	2.948	0.691	2.961
3	0.699	2.978	0.686	2.995	0.684	2.944	0.682	2.961	0.691	2.972	0.676	2.927
2	0.690	2.958	0.686	3.010	0.689	2.958	0.686	2.971	0.696	2.974	0.687	2.953
1	0.689	2.958	0.669	2.919	0.688	2.952	0.685	2.969	0.711	3.002	0.692	2.964
Max.	0.989	3.932	0.714	3.087	0.707	2.994	0.686	2.981	0.711	3.011	0.692	3.073
Min.	0.689	2.958	0.669	2.919	0.680	2.938	0.669	2.907	0.677	2.937	0.674	2.923
Aver.	0.731	3.060	0.695	3.003	0.688	2.955	0.678	2.956	0.689	2.963	0.680	2.950

In terms of the stereotomy of the Stone (Table 2), it is possible to identify the entire stone cutting by means of the mortar joints of pillars P_3 , P_4 , P_5 and P_6 , while in P_1 and P_2 , this is not possible since these pillars are partially covered by a stucco with mural paintings. Points P_{0i} are defined as the reference for setting the height of the rows. These are located in the line perpendicular to plane (τ), which defines the axis of the central nave (Figure 3).

Horizontal joints, which define the rows, are generally visible in all pillars P_i . Only visible rows were taken into account for statistical treatment, and the first joint over the wood flooring, which is not original, were not considered. Thus, the assessment, identified a total number of 147 joints.

The pillars of the first structural line [P_1 , P_2] have 26 rows; the second [P_3 , P_4] have 25 and 27 rows, respectively; and those of line [P_5 , P_6] have 22 and 23 rows. The height of the rows ranges from [0.311, 0.071] in pillars P_5 and P_3 ,

respectively. The mean of the range is (0.191 m), so there are 20 pieces that have a measurement that is only larger than 13.60% of all the rows. There are 39 rows between [0.119-0.141 m], which amounts to 20.47%, and 51.02% are between [0.119-0.161 m].

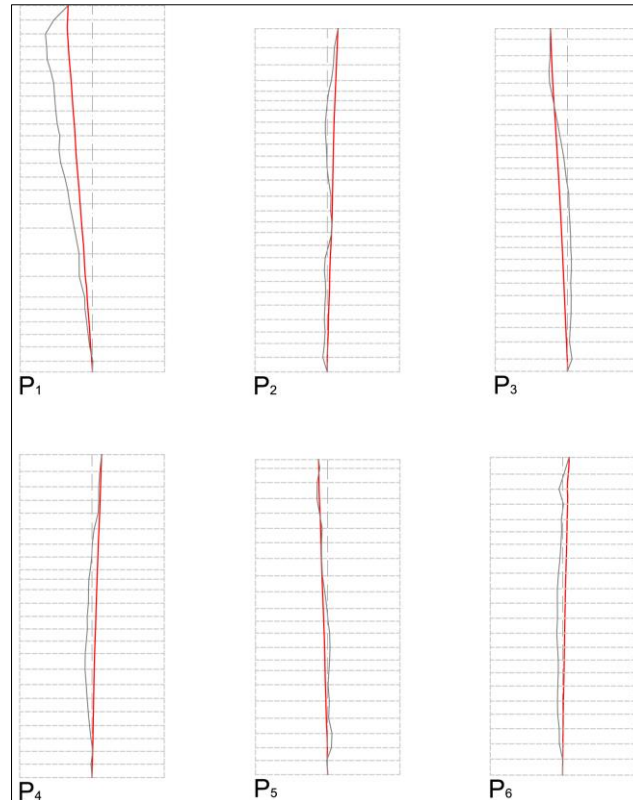
Table 2. Height of each row and the number of pieces per row. *We cannot measure the number of pieces per row because these pillars are stuccoed. However, given the results from the previous pillars, we can calculate an average of 7.97 pieces/row. Source: authors.

Pillars	Pillar 1		Pillar 2		Pillar 3		Pillar 4		Pillar 5		Pillar 6	
	Height	Pieces / Row	Height	Pieces / Row	Height	Pieces / Row	Height	Pieces / Row	Height	Pieces / Row	Height	Pieces / Row
Rows	(m)		(m)		(m)		(m)		(m)		(m)	
28	-	-	-	-	-	-	-	-	-	-	-	-
27	-	-	-	-	0.102	8	-	-	-	-	-	-
26	0.135		0.479		0.123	7	-	-	-	-	-	-
25	0.197		0.140		0.231	8	0.182	7	-	-	-	-
24	0.109		0.100		0.132	9	0.193	9	-	-	-	-
23	0.163		0.100		0.114	8	0.148	7	0.063	9	0.176	7
22	0.102		0.130		0.170	8	0.154	6	0.111	9	0.196	7
21	0.141		0.120		0.156	9	0.129	9	0.214	8	0.139	9
20	0.118		0.120		0.153	8	0.219	7	0.131	8	0.196	7
19	0.172		0.130		0.095	7	0.122	9	0.187	8	0.147	7
18	0.162		0.140		0.109	9	0.161	8	0.164	10	0.122	8
17	0.131		0.110		0.177	8	0.122	9	0.147	9	0.155	8
16	0.129		0.160		0.071	9	0.090	9	0.221	9	0.154	7
15	0.181		0.200		0.164	9	0.141	8	0.157	8	0.180	9
14	0.130		0.130		0.174	9	0.161	9	0.203	8	0.163	8
13	0.155		0.130		0.150	8	0.130	9	0.159	8	0.159	8
12	0.153	*	0.110	*	0.170	9	0.148	8	0.124	7	0.175	7
11	0.159		0.160		0.125	8	0.122	7	0.148	8	0.160	7
10	0.182		0.150		0.125	8	0.154	8	0.163	8	0.151	8
9	0.191		0.100		0.122	7	0.193	7	0.109	7	0.130	9
8	0.309		0.140		0.139	11	0.148	8	0.140	9	0.151	9
7	0.148		0.100		0.137	8	0.161	7	0.171	7	0.147	8
6	0.121		0.190		0.140	9	0.135	7	0.192	6	0.187	7
5	0.159		0.130		0.226	8	0.174	8	0.173	7	0.102	6
4	0.124		0.155		0.125	9	0.116	7	0.182	8	0.220	9
3	0.144		0.090		0.192	8	0.167	9	0.119	7	0.118	8
2	0.153		0.232		0.185	6	0.116	8	0.165	7	0.220	9
1	0.066		0.071		0.081	8	0.181	8	0.146	6	0.137	8
Max.	0.309	-	0.479	-	0.231	11.00	0.219	9.00	0.221	10.00	0.220	9.00
Min.	0.066	-	0.071	-	0.071	6.00	0.090	6.00	0.063	6.00	0.102	6.00
Average	0.151	7.97	0.147	7.97	0.144	8.26	0.151	7.92	0.156	7.87	0.160	7.83

A total number of 98 pieces were identified on pillars P₃, P₄, P₅ and P₆ based on the vertical masonry joints, which are very diffuse. The range of pieces per row is [6-11] pieces, and these extreme numbers make up only 7.14% of the overall stone cutting. The rows with six pieces are P₃.2, P₄.22, P₅.1, P₅.6 and P₆.5, and the only row with eleven pieces is P₃.8. The average number of pieces per row is 8, which amounts to 38.78% of the total number. There are 9 pieces in 28.57% of the rows and 7 pieces in 25.51% of the rows. Thus, rows tend to be built with a number of pieces between 7 and 9, which collectively amount to 92.86%.

These values cause the pillars to have a low stiffness and, therefore, they have a great capacity to deform under the active thrust (E_{ba}) of the vaults through the transverse and former arches. These are also sensitive to the reaction of the walls and the buttressing system.

Figure 4. Representation of displacements on the regression planes P_{ri} over (z_i) . Source: authors.



About the assessment of the regression planes P_{ri} of each pillar, vector (x_i, y_i) contained in the regression plane P_{ri} shows the displacement of the elements, where (x_i) represents horizontal displacement. The red line (Figure 4) represents the leaning of each pillar over its corresponding regression plane on the direction (z_d) of maximum displacement. A second line was defined for to visualize the displacements in (x_d) , applying a multiplier of 10 (Figure 4), which makes it possible to identify the nuances of such displacements. Thus, three modes are identified:

- Maximum displacement in the upper part towards the exterior of the building (P_1).
- Maximum displacement in the central part of the pillar (P_4, P_6).
- Variable displacement between the upper part and lower part of the pillar (P_2, P_3, P_5).

Thus, the projection of the displacements of the centroids over the regression planes is not uniform in relation to the vector of the leaning. The vector can be decomposed to on two vectors, one in the lower part of the pillar, which tends to the central vault, and another, which tends to the exterior of the building. The change occurs at a height that ranges from [1.587, 2.946] in [P_2, P_4].

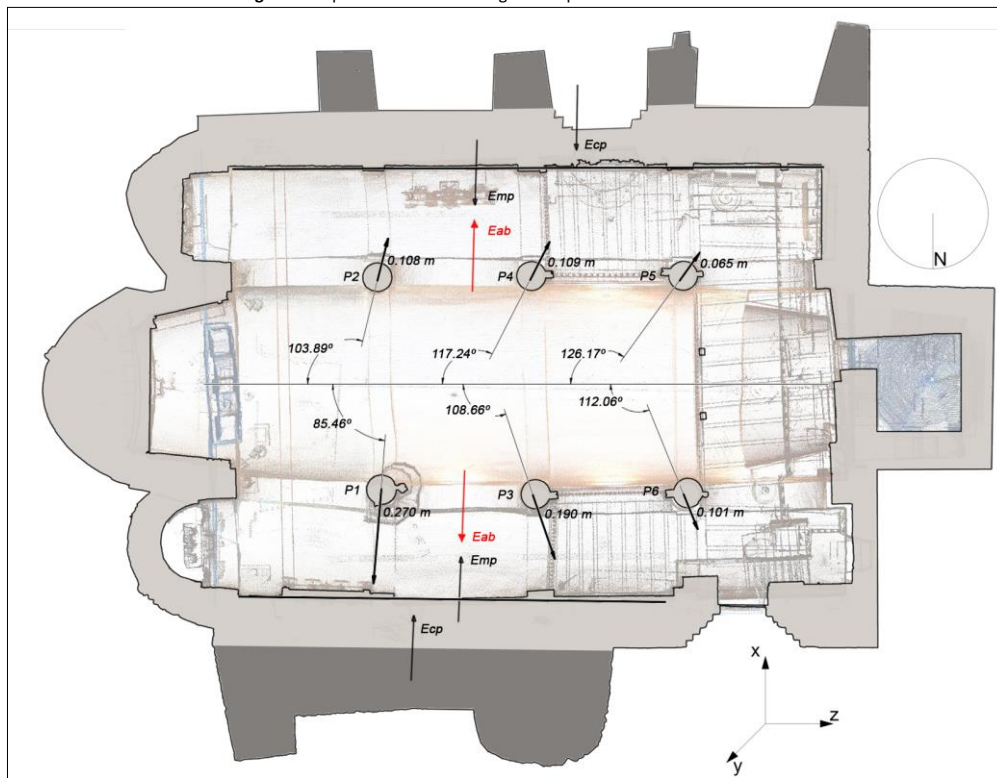
The greatest displacement is found in pillar P_1 (Table 3), with a range of displacement on each row of [0.270, 0.001]. That displacement is followed by that in pillar P_3 , with a range of [0.190, 0.001]. The range of displacements of the rest of the pillars is as follows: P_2 [0.108, 0.002], P_4 [0.109, 0.002], P_5 [0.101, 0.001], and finally, the least deformed pillar, P_6 [0.065, 0.001]. Thus, pillars P_1, P_3 and P_5 have greater deformations than the others. These are located in the North face, where a massive buttress of 131.04 m³ was built, which stiffens the structure. The wall at the south face has a volume of 179.91 m³, which was later reinforced with four buttresses of 44.96 m³.

About (z_i) , it shows the rotation of the plane in relation to the directrix of the vault, and it is represented in the floor plant of (Figure 5). None of the regression planes P_{ri} is perpendicular to the directrix of the central vault. Each one is gently sloped. The angle in P_1 is 85.466°, so $(\omega_\phi) < 90^\circ$ (Figure 5). It is also the most inclined pillar (0.270 m) and is the highest (4.170 m). The rest of the pillars have angles $(\omega_\phi) > 90^\circ$, with a range [103.893°, 126.169°]: [P_2 ; 103,893°], [P_3 ; 108,665°], [P_4 ; 117,245°], [P_5 ; 112,066°] and [P_6 ; 126,169°].

Table 3. Characteristics of the displacement vector (the angles refer to the inclination of the vector in respect to the vertical). Source: authors.

	Max. Disp. X	Min. Disp. X	Angle	Pillar length	Pillar height	Angular deviation
Pillars	(m)	(m)	(°)	(m)	(m)	(°)
P1	0.270	0.001	3.78	4.183	4.170	1.11
P2	0.108	0.002	1.78	4.842	3.940	2.72
P3	0.190	0.001	2.85	3.890	3.888	1.37
P4	0.109	0.002	1.71	3.774	3.770	2.21
P5	0.101	0.001	1.67	3.590	3.587	2.15
P6	0.065	0.001	1.17	3.687	3.684	3.15
Max.	0.270	0.002	3.78	4.842	4.170	3.15
Min.	0.065	0.001	1.17	3.590	3.587	1.11
Average	0.141	0.001	2.16	3.994	3.84	2.12

Figure 5. Representation of the regression planes P_{ri} . Source: authors.



Discussion and Conclusions

The obtained regression planes P_{ri} , which contain the deformations for each pillar, tend to have the direction of the thrust over the pillar P_i . These displacements are the result of the active thrusts of vaults and the reactions of the buttressing system, walls and buttresses.

This study revealed that the direction of the displacements of the six pillars P_i is not perpendicular to the central axis of the church ϕ_1 since $(\omega_\phi) \neq 90^\circ$. These results prove the hypothesis that the thrusts of the vaults are not perpendicular to the axis of the church, as was the case in Roman vaults, which Choisy (1873) defined with regular geometry and stone cutting. The direction of displacements is caused by the irregular geometry of the vaults of Santa Maria de Arties as well as the masonry stone cutting and the above mentioned effect of the walls and buttresses. The last ones were added to maintain equilibrium during the last millennium.

The displacement of the five pillars ($P_2 \dots P_5$), where $(\omega_\phi) > 90^\circ$, tends to the opposite façade of the apse. In addition, pillars P_5 and P_6 , built during twelfth century on that façade, are the least deformed pillars because of two subsequent

transformations: the construction of the bell tower over the centre of the façade (XIII-XIV) and the wood choir (XVIII). These elements have a stiffening function.

Pillar P_1 is the most deformed pillar of Santa Maria de Arties and has $(\omega_\phi) < 90^\circ$ over the main axis. The displacement tends to the apse. This pillar, together with pillar P_3 , where $(\omega_\phi) > 90^\circ$, is located where a great balancing was achieved through the buttressing system. In respect to a specific weight of more than 24 kN/m^3 , the buttressing system weighs 3144.96 kN . This is where funicular shapes have appeared, which are inverted arches. Despite the hanging shape, vaults are thick enough to work under compression strength.

It can be considered that pillar displacements tend to have the same direction of the thrust over pillar P_i . Thus, the regression planes identified P_{ri} , which contain these displacements, are essential to defining any intervention over these masonry buildings because they show the direction of possible preventive actions. The issue is complex and exceeds the initial aims of that investigation, and opens the door to further research on that sense.

Otherwise, the vectorization of the displacements of each row, deduced from the regression plane, makes it possible to parametrize the leaning of each pillar. Three deformation modes were identified, so the displacements of the pillars are not uniform. Moreover, on pillars (P_2 , P_3 , P_5), the displacements are variable and appear to be negative displacements on (x) in relation to the vertical. The range of heights has been identified where this change occurs, which is [1.587, 2.946] on [P_2 , P_4], respectively. Although the values are low, this point is of great importance for determining the appropriate actions that need to be taken for intervention on such buildings. Otherwise, no relevant differences have been identified between the pillars displacements of each side that can be related to the two buttressing systems.

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