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Performance evaluation of GPS receiver under equatorial scintillation

Abstract: Equatorial scintillation is a phenomenon that occurs daily in the equatorial region after the sunset and affects radio signals that propagate through the ionosphere. Depending on the temporal and spatial situation, equatorial scintillation can represent a problem in the availability and precision of the Global Positioning System (GPS). This work is concerned with evaluating the impact of equatorial scintillation on the performance of GPS receivers. First, the morphology and statistical model of equatorial scintillation is briefly presented. A numerical model that generates synthetic scintillation data to simulate the effects of equatorial scintillation is presented. An overview of the main theoretical principles on GPS receivers is presented. The analytical models that describe the effects of scintillation at receiver level are presented and compared with numerical simulations using a radio software receiver and synthetic data. The results achieved by simulation agreed quite well with those predicted by the analytical models. The only exception is for links with extreme levels of scintillation and when weak signals are received.

Keywords: Component tracking performance, GPS receiver, Ionospheric scintillation, Communication system simulation.

INTRODUCTION

Several environmental factors may affect GPS (Global Positioning System) performance, such as electromagnetic interference, multipath, atmospheric delay and ionospheric scintillation. Ionospheric Scintillation is responsible for a significant decrease in GPS accuracy, which may lead to a complete system failure (Beach, 1998). Ionospheric scintillations result in rapid variations in phase and amplitude of the radio signal, which crosses the ionosphere. Such a phenomenon is more usual near equatorial regions approximately from -20° to 20° of the globe and auroral zone from 55° to 90° of latitude. Apart from that, the scintillation activity has a temporal dependence, according to the local season and the solar cycle that has an 11-year period (Beach, 1998; Kintner et al., 2004). The ionospheric scintillation phenomenon in equatorial regions is known as equatorial scintillation. This kind of scintillation impacts predominantly by causing fluctuations on the intensity of the signal (Beniguel et al., 2004). Equatorial scintillation usually takes place after sunset, affecting the GPS receiver performance, depending on its severity (Basu, 1981). The objective of this work is to evaluate the effects of equatorial scintillation on the code and carrier tracking loops of GPS receivers. Initially, an introduction to ionospheric behavior in equatorial zones is given;

Received: 06/08/09 Accepted: 29/09/09 followed by a statistical model presentation, which characterizes the amplitude scintillation. Following this, a receiver performance analysis is presented, as function of this effect. Based upon such an analysis, analytical models are used to represent the behavior and performance of GPS receivers. Finally, results of numerical simulations are presented and compared to analytical results.

FUNDAMENTALS OF IONOSPHERIC SCINTILLATION

Ionosphere

The ionosphere is the layer of the atmosphere where free electrons and ions are present in sufficient quantities to affect the radio waves traveling through it. The structure of the ionosphere varies due to season, daily variation, solar production and the process of recombination among electrons. The ionosphere is sub-classified in layers D, E, F1 and F2, according to the electrical density present. The D layer extends from 50km to 90km of altitude. It has a low electron density, vanishing during the night. The E layer extends from 90km to 140km in height and is basically produced by the solar X-rays, having a peak of electron density at 120km. The F1 layer extends from 140km to 200km and the main source of ionization is the solar extreme ultraviolet light (EUV). The F2 layer

extends from 200km to 1000km and presents a region of maximum electron density at 350km (Kelley, 1989). These layers are a result of photochemical processes and plasma transportation. A typical electron density profile of the ionospheric layers during the daytime and the ionization during the evening hours is shown in Fig. 1.

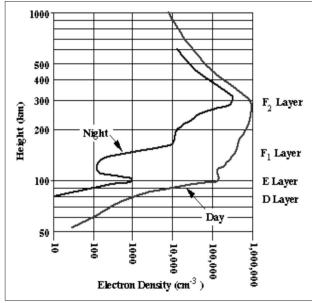


Figure 1. Electrical density profile of ionosphere during day and night.

It is important to observe how the layers decay at night in the absence of photo-ionization. The F1 layer almost disappears while F2 and E layers still remain due to recombination and transportation.

Equatorial Scintillation

Equatorial scintillation happens when small-scale irregularities in the F region of the ionosphere affect the RF signals. Influenced by the pressure gradients and gravity, the equatorial plasma present in the F2 layer is forced downward along the magnetic field lines. This process creates a belt of enhanced electron density from 15° to 20° on both sides of the geomagnetic equator. This particular region where the electron density in enhanced is referred to as the Equatorial Anomaly. The process by which they are created is known as the Fountain Effect. This process is illustrated in Fig. 2, where the Equatorial Fountain is indicated by the ExB drift, which drives the plasma upward. This plasma is then diffused along **B** field under the influence of gravity, g, and pressure gradients ∇_{P} . This process happens in the daylight hemisphere (Kelley, 1989).

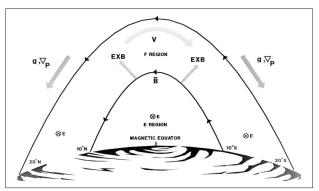


Figure 2. Equatorial fountain that gives rise to the equatorial anomaly. La Beaujardiere, O. et al. (2004).

At dusk, the electric field, **E**, increases as the neutral winds, **V**, increases, and the **ExB** drift raises the F layer. This process is known as Pre-Reversal Enhancement when the base of the F layer is forced against the gravity, creating the Rayleigh-Taylor Instability, in which a heavier fluid is held by a lighter one. When a perturbation happens, this equilibrium is broken and the lighter fluid rises through the denser fluid creating a bubble. In the region of the equatorial ionosphere these bubbles are called Equatorial Plasma Bubbles. The Equatorial Anomaly is responsible for the formation of the plasma density irregularities that result in the Equatorial Plasma Bubbles that lead to scintillation (Kintner et al., 2004).

STATISTICAL CHARACTERISTIC OF AMPLITUDE SCINTILLATION

The index that indicates the severity of amplitude scintillation is the S₄. It is defined as the normalized variance of intensity of the received signal, given by

$$\log(q_{s_0} - q_s) = \log(q_{s_0}) - \left(\frac{K_s}{2.303}\right)t. \tag{1}$$

where $I=A_{\rm S}^2$ is the intensity of the received signal. Based on studies of ionospheric scintillation data, it has been shown that amplitude scintillation might be modeled as a stochastic process that follows a Nakagami-m distribution, given by (Fremouw, Livingston and Miller, 1980)

$$\frac{t}{q} = \frac{1}{K_2 q_{xx}^2} + \frac{1}{q_{xx}} t \tag{2}$$

where $A_{\rm S}$ is the amplitude of the received signal, $\Gamma()$ is the gamma function, $_{q_{\rm q}}=\frac{q_{\rm mn}}{1+{\rm b}\,{\rm C}_{\rm m}}$ and $_{q_{\rm q}}=q({\rm C}_{\rm q})'$. The m parameter from Nakagami-m distribution and the ${\rm S}_4$ index are related by $m=1/{\rm S}_4^{-2}$.

SYNTHETIC AMPLITUDE SCINTILLATION DATA

Based on Humphreys et al. (2008), a scintillation model has been implemented with the objective of simulating the scintillation effects on equatorial transionospheric radio signals such as the GPS ones. This model assumes that amplitude scintillation follows a Rice distribution. This assumption has been made because of the implementation simplicity of the Rice model. The Rice distribution is given by

$$p(A_s) = \frac{2A_s(1+K)}{\Omega} I_0 \left(2A_s \sqrt{\frac{K+K^2}{\Omega}} \right) e^{-K-A_s^2(1+K)} / \Omega$$
 (3)

where, $A_s \ge 0$, $I_0()$ is the modified Bessel function of zeroth order and K is Rician parameter. Although the Nakamami-m distribution, (2), is the one that best fits the real scintillation data (Fremouw, Livingston and Miller, 1980). But in Humphreys et al. (2008), it is shown that Nakamami-m and Rice distribution are similar and they agree quite well with the empirical data for $S_4 < 1$, according to the chi-square tests. Thus, the Nakamagi-m distribution might be closely approximated by Rice distribution. This mapping is given by (Simon and Alouini, 2006),

$$K = \sqrt{m^2 - m} / m - \sqrt{m^2 - m} \tag{4}$$

Considering the expression

$$z(t) = z_K + \xi(t) \tag{5}$$

where z_K is a complex constant and $\xi(t)$ is a zero mean, gaussian process. From (5), the amplitude scintillation with a Rice distribution can be generated by

$$A_{s}(t) = |z(t)| \tag{6}$$

The block diagram showing the mechanization process of scintillation simulator is illustrated in Fig. 3.

According to this process, a zero-mean white Gaussian noise n(t) is applied to a 2^{nd} order Butterworth low pass filter, with the response:

$$|H(f)| = 1 / \sqrt{1 + \left(\frac{f}{Bd}\right)^4} \tag{7}$$

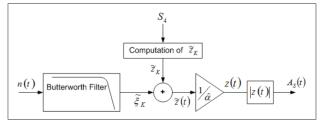


Figure 3. Mechanization process of scintillation simulator.

where $Bd = \beta/\sqrt{2\pi\tau_0}$ is the frequency bandwidth, $\beta=1.2396464$ is a constant and τ_0 is the decorrelation time of generated scintillation data. The filtered version of n(t) is denoted $\tilde{\xi}(t)$, with variance $\sigma_{\tilde{\xi}}^2$. The value of \tilde{z}_k in (5) is responsible for controlling the level of scintillation in the simulator.

$$\tilde{z}_{\kappa} = \sqrt{2\sigma_{\xi}^2 K} \tag{8}$$

Based on (4) and the relation $m=1/S_4^2$ it is possible to establish a relation between the scintillation index S_4 and the Rician parameter K, that is used to compute \tilde{z}_{κ} .

The constant \tilde{z}_{κ} is added to $\tilde{\xi}(t)$, resulting in $z(t) - \tilde{\xi}(t) + z_{\kappa}$. The signal z(t) is then normalized by $\tilde{\alpha} = E[|z(t)|]$, resulting in a synthetic scintillation data. An example of amplitude scintillation data generated by this model is shown in Fig. 4.

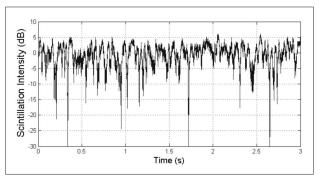


Figure 4. Example of scintillation for S_4 =0.68.

GPS RECEIVER

The GPS receiver is divided into three main parts, according to Fig. 5. The Front End (FE) is the set of devices where the electromagnetic waves from the GPS satellites are converted into electrical signal by the antenna. Through the front end, the input signal is filtered, amplified to a proper amplitude and converted to an Intermediate Frequency (IF) to be processed. The second section of the receiver is referred to as a Digital Signal Processing (DSP). This section performs the acquisition

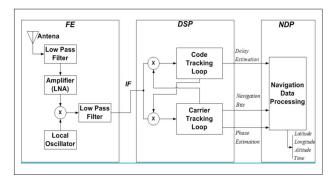


Figure 5. Architecture of GPS receiver (Ward, 1996).

and tracking of the received signal, providing the pseudo range and carrier phase information. The last section of the receiver is the Navigation Data Processing (NDP), this section has the task of calculating ephemeris data, GPS time, position and velocity (Ward, 1996).

Scintillations affect the performance of GPS receivers, in a notable way at the tracking loop level. Depending on the scintillation level, the receiver might increase the range measurement errors or can even lead to carrier loss of lock and code loops. In extreme cases, the scintillation can result in full disruption of the receiver.

The signal received from a generic GPS satellite, at the output of the FE that will be processed by the DSP section of the receiver is given as (Borre et al., 2007):

$$s(n) = A(n)C(n-\tau)D(n-\tau)\cos(2\pi f_{FI}t + \varphi) + N(n)$$
 (9)

where A(n) is the amplitude of the received signal, C(n) is the satellite pseudorandom noise code (PRN), D(n) is the navigation data sequence, τ is the code delay, f_{rr} is the intermediate frequency, Ψ is the phase of the GPS carrier. In addition to the received signal, there is the term N(n) that represents the band-limited, stationary, Gaussian noise, with zero mean and power spectrum density.

Carrier Tracking Loop

In order to demodulate the GPS navigation data successfully, it is necessary to generate an exact carrier wave replica. This task is usually executed in a GPS receiver by a phase locked loop (PLL). The model of PLL used on GPS receivers is based on a Costas suppressed carrier tracking loop, as illustrated in Fig. 6 (Ward, 1996).

In each arm of the Costas loop, the IF signal undergoes two multiplications. The first one has the objective of wiping off

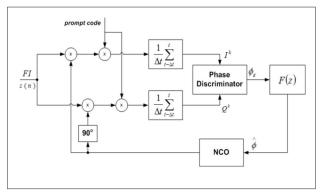


Figure 6. Block diagram of Costas carrier tracking loop.

the carrier of the received signal. The Costas tracking loop is insensitive to 180° phase shifts, which requires a second multiplication that wipes off the PRN code. The PRN code is generated by the code tracking loop. After the multiplications the signal in both arms is filtered by a pre-detection integrate and dump filter. These signals are then used by the phase discriminator to determine the carrier phase error between the local generated replica and the received signal. The phase error computed by the discriminator is filtered and applied as a feedback to the NCO.

An important parameter in the evaluation of receiver performance is the tracking threshold point, which is the value where the loop stops working stably and loses the lock. When it happens, the phase error measurements become meaningless and the number of cycle slips increases. The exact point of this transition is hard to determine. Reasonable values to be assumed as a threshold, and mean time between cycle slips are given respectively by Holmes (1982):

$$\sigma_{\varphi\varepsilon|\lim}^2 = (\pi/12)^2 \left[rad^2 \right] \tag{10}$$

$$\overline{T} = \pi^2 \rho_{\varepsilon} I_0^2 \left(\rho_{\varepsilon} \right) / 2B_n \tag{11}$$

where $\rho_{\epsilon} = 1/4\sigma_{\varphi\epsilon}^2$ is the signal-to-noise ratio of the loop.

Code Tracking LoopUnits

The objective of the code tracking loop is analogous to the carrier tracking loop. In this case, the code loop has the function of providing a PRN code sequence replica with the same code delay from the received signal. With this estimation of the code delay it is possible to obtain a pseudorange measurement. The code tracking loop in a GPS receiver is a delay locked loop (DLL), Fig. 7 illustrates a block diagram of the DLL.

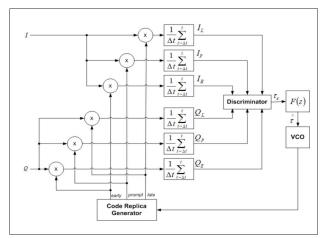


Figure 7. Block diagram of code tracking loop - DLL

First, the IF received signal is multiplied by a carrier wave replica, resulting in a base band signal. The code generator, provides the code replica and two other shifted versions of the code replica. Those three code replicas are called early, prompt and late. The early and late replicas are shifted from the original prompt replica by a factor d. The base band signal in I and Q arms are multiplied by the code replicas and filtered by a pre-detection integrate and dump filter. The I and Q filtered signals are then processed by the code loop discriminator to produce a code delay error that will be filtered to feedback the code generator.

As in the carrier tracking loop case, there is a tracking threshold that is used to evaluate the performance of the code loop. In this case, the DLL is considered to be in lock if the threshold is respected (Ward, 1996):

$$\sigma_{\tau\varepsilon|_{\text{lim}}}^2 \le \left(d/3\right)^2 \tag{12}$$

EFFECTS OF AMPLITUDE SCINTILLATION ON GPS RECEIVERS

According to [12], the tracking error variance at the output of the PLL is expressed as

$$\sigma_{\varphi e}^2 = \sigma_{\varphi S}^2 + \sigma_{\varphi Th}^2 + \sigma_{\varphi osc}^2 \tag{13}$$

where $\sigma_{\varphi S}^2$ corresponds to phase scintillation error component, $\sigma_{\varphi Th}^2$ is the thermal noise component and $\sigma_{\varphi osc}^2$ is the receiver oscillator noise. The receiver oscillator noise is assumed to have a standard deviation of 0.1 rad and it will be ignored in this work. For the equatorial region, the values of $\sigma_{\varphi S}^2$ are considerably low and well behaved.

When there is no scintillation, the component of tracking error due to thermal noise in a PLL is given by,

$$\sigma_{qTh}^2 = \frac{B_n}{C/N_0} \left[1 + \frac{1}{2\Delta t \left(C/N_0 \right)} \right] \tag{14}$$

where B_n is the PLL single-sided noise equivalent bandwidth, C/N_0 is the nominal carrier to noise density ratio and Δt is the pre-detection integration period.

The equatorial scintillation presents indicative fluctuation in the intensity of the received signal. This amplitude scintillation degrades the C/N_0 and, as a consequence, increases the tracking error due to thermal noise. In (Conker et al., 2003), the effects of amplitude scintillation have been modeled, considering that this kind of scintillation follows a Nakagami-m distribution. Thus the thermal noise tracking error can be characterized by S_4 , according to the expression

$$\sigma_{\varphi Th}^{2} = \frac{B_{n} \left(1 + \frac{1}{2\Delta t \left(C/N_{0} \right) \left(1 - 2S_{4}^{2} \right)} \right)}{\left(C/N_{0} \right) \left(1 - S_{4}^{2} \right)}$$
(15)

The term $\sigma_{\varphi Th}^2$ in (13) is the one that most contributes to the PLL tracking error variance. Indeed, the other terms in (12), compared with $\sigma_{\varphi Th}^2$ become negligible.

For the tracking error code delay at the output of DLL it is correct to affirm that $\sigma_{\tau\epsilon}^2 = \sigma_{\tau Th}^2$, where $\sigma_{\tau Th}^2$ is the thermal noise component. In this case, there is no phase scintillation component, because according to Davies, 1990, a non-coherent DLL is not affected by the phase scintillation. In the absence of scintillation, the DLL tracking error code loop in function of the thermal noise is given by

$$\sigma_{\tau Th}^{2} = \frac{B_{n}d}{2C/N_{0}} \left[1 + \frac{1}{\Delta t C/N_{0}} \right]$$
 (16)

In an analogous way to the PLL case, in (Conker et al., 2003), the effects of scintillation on the DLL is modeled using a Nakagami-m distribution to characterize tracking code error by function of amplitude scintillation index, S₄, that is expressed as

$$\sigma_{\tau Th}^{2} = \frac{B_{n} d \left(1 + \frac{1}{\Delta t \left(C/N_{o} \right) \left(1 - 2S_{4}^{2} \right)} \right)}{2 \left(C/N_{o} \right) \left(1 - S_{4}^{2} \right)}$$
(17)

Usually the results of DLL tracking error are presented in meters. In this case, $\sigma_{\text{te}(meters)} = W_{C/A}\sigma_{\text{te}}$, where $W_{C/A}$ is the chip length (293.0523m).

Numerical Results

This section describes the results obtained from the simulations conducted in this investigation, as depicted in the block diagram shown in Fig. 8 (Moraes, 2009).

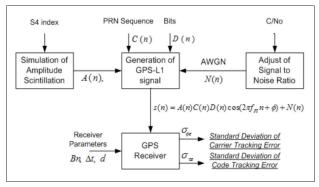


Figure 8. General block diagram of the simulation.

The model described in section III was implemented to generate synthetic amplitude scintillation data. With this model, it is possible to specify the scintillation severity by the S₄ index, generating an ionospheric channel response.

A GPS signal as expressed in (9) was generated. The navigation data bits D(n) were generated as a known sequence. This sequence was modulated by the PRN code and by carrier wave. This carrier wave was set to a $f_{\rm FI}$ frequency of 9.548MHz, with a sample frequency of 38.192MHz.

The amplitude of GPS generated signal varies with the synthetic amplitude scintillation data. Later a Gaussian noise was added to the GPS signal with amplitude scintillations. The level of noise is adjusted according to the desired C/N_0 of the simulated link.

This signal corrupted by the noise and affected by the amplitude scintillation is processed by the DSP section of the receiver. A software receiver based on (Borre et al., 2007) was modified in order to evaluate the effects of amplitude scintillation on carrier and tracking loops.

The tracking error output of this software receiver was compared with analytical models. In all simulations the GPS data lasted 30 seconds, the pre-detection integration period lasted 1ms and the correlation space was equal to 0.5 chip.

Figures 9 and 10 shows calibration test results for three different values of bandwidth for the carrier and code loops respectively. This test consists of simulating a situation where there is no scintillation. In this case, the received GPS signal is only corrupted by noise. The results of this simulation are compared with the analytical values based on (15) and (17).

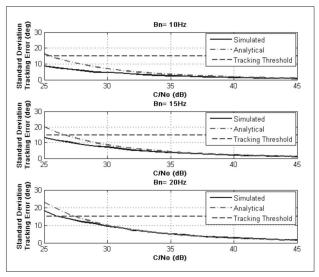


Figure 9. Calibration results for the Carrier tracking loop.

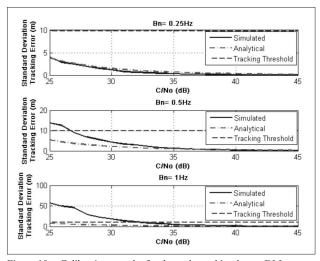


Figure 10. Calibrations results for the code tracking loop - DLL

It is observed that the results of simulation and analytical models do not diverge significantly until the level of the received signal is weak and the tracking error is above the tracking threshold (10) and (12) for the carrier and code loop. The next step in the simulation consists of affecting the GPS signal with amplitude scintillation. In this case, the amplitude scintillation was simulated from a low level

up to 0.7, that is considered a severe level of scintillation. For this simulation a GPS link was considered with C/N_0 =40dB and C/N_0 =32dB and B_n =20Hz. The results, shown in Fig. 11 for the carrier loop, appear to suggest that the analytical model fails to perform the scintillations effects in carrier loop for cases with weak signals. Thus GPS links with high C/N_0 are little affected by scintillation.

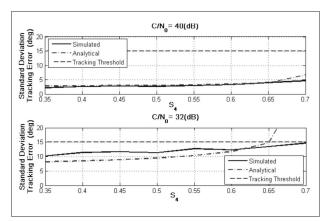


Figure 11. Carrier tracking loop performance under amplitude scintillation.

On the other hand, links with some limitation in C/N_0 present a carrier tracking error higher than expected.

To confirm this limitation of the receiver, a situation was considered where a GPS signal is affected by an amplitude scintillation of S_4 =0.63. These data were processed by the receiver, changing only the power of the received signals. Figure 12 presents the result of this simulation for the carrier loop. These results show that with low C/N_0 and severe scintillation, the analytical model does not describe the real tracking error.

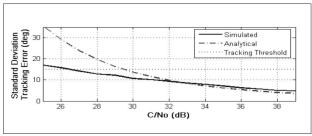


Figure 12. Costas carrier tracking loop performance for $S_a=0.63$.

Simulations show that thermal noise error associated with the amplitude scintillation is small for code loop. Even for extreme scintillation levels and weak signal, this loop presents robustness. Figure 13 shows the performance of the code loop under several levels of scintillation in a case where C/N_0 =36dB and B_n =1 Hz.

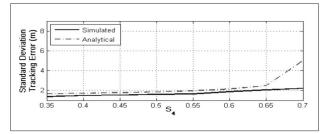


Figure 13. Code tracking loop under amplitude scintillation.

CONCLUSION

This work has presented a performance evaluation of a GPS receiver under equatorial scintillation. Analyzing the analytical models, it is possible to conclude that amplitude scintillation is a high source of error, especially in the carrier tracking loop. Using a synthetic amplitude scintillation model, it has been possible to simulate the amplitude scintillation in a software receiver. The results from numerical simulations showed that, except for the cases involving extreme scintillation, or radio link with low carrier to noise density ratio, C/N_0 , the numerical results agreed quite well with those predicted by the analytical models. In situations, involving weak signals and high scintillations, the analytical models fail to predict the real performance of the receiver (Moraes, 2009).

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