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Influence of mass transfer on bubble plume hydrodynamics

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ABSTRACT

This paper presents an integral model to evaluate the impact of gas transfer on the hydrodynamics of bubble plumes. The model is based on the Gaussian type self-similarity and functional relationships for the entrainment coefficient and factor of momentum amplification due to turbulence. The impact of mass transfer on bubble plume hydrodynamics is investigated considering different bubble sizes, gas flow rates and water depths. The results revealed a relevant impact when fine bubbles are considered, even for moderate water depths. Additionally, model simulations indicate that for weak bubble plumes (i.e., with relatively low flow rates and large depths and slip velocities), both dissolution and turbulence can affect plume hydrodynamics, which demonstrates the importance of taking the momentum amplification factor relationship into account. For deeper water conditions, simulations of bubble dissolution/decompression using the present model and classical models available in the literature resulted in a very good agreement for both aeration and oxygenation processes. Sensitivity analysis showed that the water depth, followed by the bubble size and the flow rate are the most important parameters that affect plume hydrodynamics. Lastly, dimensionless correlations are proposed to assess the impact of mass transfer on plume hydrodynamics, including both the aeration and oxygenation modes.

Key words: aeration, bubbles, hydrodynamics, mass transfer, modeling, oxygenation.

INTRODUCTION

Bubble plumes are produced when gases are injected in liquids, as shown schematically in Figure 1. These systems occur in several engineering applications including artificial aeration, oxygenation and mixing in tanks and water bodies, reservoir destratification, contaminant containment, underwater blowouts, CO₂ sequestration, among others (Wüest et al. 1992, Johansen 2003, Yapa and Chen 2004, Singleton and Little 2006, Lima Neto et al. 2008a, c, Socolofsky et al. 2008, Einarsrud and Brevik 2009, Lima Neto 2012a, b, Zhang and Zhu 2013).

The integral approach proposed by Cederwall and Ditmars (1970) and then revisited by Milgram (1983), Socolofsky et al. (2002), and Lima Neto (2012a) has long been used to model the hydrodynamics of round bubble plumes in stagnant water. These models consider Gaussian distributions of water velocity

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and void fraction (see Figure 1), as observed experimentally (Milgram 1983, Lima Neto et al. 2008b). Key model parameters are the entrainment coefficient and the factor of momentum amplification due to turbulence, which can be estimated using functional relationships given by Milgram (1983) and Lima Neto (2012a). For relatively weak bubble plumes (i.e., with relatively low gas flow rates and high water depths and slip velocities). Lima Neto (2012a) showed that a relationship for the momentum amplification factor is indeed needed, as the importance of turbulent momentum flux increases with decreasing air flow rate (Leitch and Baines 1989). On the other hand, for stronger bubble plumes, this effect becomes negligible. Wüest et al. (1992) investigated the effect of mass transfer using such integral approach but considering top hat distributions of plume properties and neglecting the effect of turbulence. Buscaglia et al. (2002) compared an integral approach based on the model of Wüest et al. (1992) to computational fluid dynamic (CFD) simulations and obtained similar results. McGinnis et al. (2004) and Socolofsky et al. (2008) also validated and improved the method of Wüest et al. (1992). More recently, Einarsrud and Brevik (2009) presented an alternative bubble plume model accounting for bubble dissolution that makes use of a turbulent correlation parameter analogous to the entrainment coefficient. Differently from previous studies on mass transfer, Einarsrud and Brevik (2009) assumed Gaussian profiles for plume parameters. Other investigations on the effects of crossflow, stratification or hydrate formation have also been conducted (Johansen 2003, Socolofsky et al. 2008, Zhang and Zhu 2013), but are not the focus of the present study.

In this paper, we proposed a simple integral model to predict gas transfer from round bubble plumes in stagnant water. The model is based on Gaussian profiles of plume properties, conservation equations of liquid volume, momentum and buoyancy, and functional relationships, modified from Lima Neto (2012a), to describe the hydrodynamics of weak/strong bubble plumes. The effect of mass transfer as initially suggested by Wüest et al. (1992) was incorporated into the model. It is important to note that the model developed herein differs from that of Wüest et al. (1992) because the former uses Gaussian distributions of water velocity and void fraction while the latter uses top hat distributions. In addition, different functional relationships for the initial conditions of the plume, entrainment coefficient and momentum amplification factor were used in our model. Also, the present model considers a simple numerical integration of the bubble plume equations, making it simpler than the other currently available models.

MODEL FORMULATION

The axial variation of mass of gaseous species transferred per bubble is given by Eq. (1), which has been modified from Wüest et al. (1992) to account for a Gaussian distribution of water velocity in the radial direction (see Figure 1):

$$\frac{dm_i}{dz} = -K_L \left(HP_i - C_i\right) \frac{\pi d_b^2}{\left(\frac{u_c}{1 + \lambda^2} + u_s\right)} \tag{1}$$

in which m_i is the mass of each gaseous specie i (oxygen or nitrogen), K_L the liquid-side mass-transfer coefficient, H the Henry's constant, P_i the partial pressure of the gas at a given depth, C_i the bulk aqueous-phase concentration, d_b the bubble diameter, λ the spreading ratio of the bubble core radius relative to the entrained liquid radius, u_c the centerline liquid velocity, and u_s the bubble slip velocity. Relationships for K_L , H, P_i , and u_s , as well as a constant value of $\lambda = 0.8$ were obtained from Wüest et al. (1992).

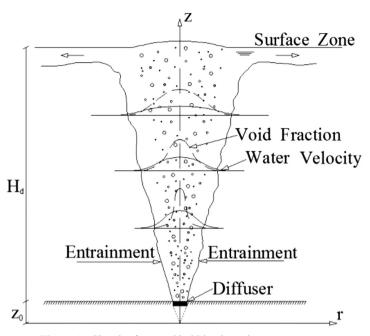


Figure 1 - Sketch of a round bubble plume in stagnant water.

At a distance z from the source, mass transfer from one bubble to the water [given by Eq. (1)] will promote a reduction in the bubble volume V_b . On the other hand, as the bubble rises towards the free water surface, it will also suffer decompression which in turn will promote an increase in V_b , as a counterbalance effect. The following expression obtained by considering the ideal gas law, together with isothermal expansion, is used to evaluate the impact of decompression on bubble diameter:

$$V_{b,z} = \frac{m_{b,z}}{\rho_{g,d}} \left(\frac{H_a + H_d}{H_a + H_d - z} \right)$$
 (2)

where $m_{b,z}$ is the total mass of gaseous species of a bubble at a distance z from the source, $\rho_{g,d}$ is gas density at the diffuser, H_a the atmospheric pressure head, and H_d the water head above the diffuser. Thus, assuming a spherical bubble, the diameter d_b can be calculated by:

$$d_b = \sqrt[3]{\frac{6V_{b,z}}{\pi}} \tag{3}$$

A volumetric gas flow rate $Q_{g,z}$ for all the bubbles at a given height z was calculated to introduce the effect of mass transfer on plume hydrodynamics:

$$Q_{g,z} = V_{b,z}N \tag{4}$$

in which N is the number flux of bubbles, assumed constant along the axial direction and equal to the number flux at the diffuser. This means that bubble coalescence and breakup are considered negligible. Equation (4) also assumes monodisperse bubble sizes.

Lastly, bubble plume hydrodynamics can be described by two equations derived from conservation of liquid volume, momentum, and buoyancy, which have been modified from Cederwall and Ditmars (1970) to account for mass transfer and momentum amplification due to turbulence:

$$\frac{du_c}{dz} = \frac{2gQ_{g,z}}{\gamma\pi u_c b^2 \left(\frac{u_c}{1+\lambda^2} + u_s\right)} - \frac{2\alpha u_c}{b}$$
(5)

$$\frac{db}{dz} = 2\alpha - \frac{gQ_{g,z}}{\gamma \pi u_c^2 b \left(\frac{u_c}{1 + \lambda^2} + u_s\right)} \tag{6}$$

in which b is the plume radius where $u=0.37u_c$, g the gravity acceleration, α the entrainment coefficient, and γ the momentum amplification factor, defined as the ratio of total momentum flux to the momentum flux carried by the mean flow. The following functional relationships for the parameters α and γ were adjusted herein to a wide range of laboratory and field-scale data, provided by Milgram (1983), resulting in correlation coefficients higher than 0.95:

$$\alpha = 0.0148 \ln(\beta) + 0.0824 \tag{7}$$

$$\gamma = 1.405 (\beta)^{-0.18} \tag{8}$$

in which β is a dimensionless parameter given by:

$$\beta = \frac{g'Q_{g,a}}{H_d u_s^3} \tag{9}$$

where g' is the reduced gravity defined as $g' = g (\rho_w - \rho_g)/\rho_w$, in which ρ_w and ρ_g are the water and gas density, respectively, and $Q_{g,a}$ is the air volumetric flow rate at atmospheric pressure. Note that Eqs. (8) and (9) have the same form as those presented by Lima Neto (2012a), but here a constant slip velocity of $u_s = 0.23$ m/s (instead of $u_s = 0.35$ m/s, as suggested by Milgram 1983) was used to calculate β . This value of u_s covers bubble diameters d_b ranging from about 5 to 10 mm (see Wüest et al. 1992), which were probably the mean sizes of the bubbles present in the coarse-bubble aeration tests reported by Milgram (1983), where bubble dissolution was assumed negligible.

Eq. (7) indicates that, for a given value of g', the higher the value of β (i.e., the higher the gas flow rates $Q_{g,a}$ as compared to the water depths H_d and slip velocities u_s), the higher will be the centerline (and entrained) liquid velocity. Note that lower slip velocities means smaller bubbles and a higher number flux N (for the same value of $Q_{g,a}$), which results indeed in higher entrainment into the plume (Lima Neto et al. 2008a). On the other hand, Eq. (8) shows that higher values of β will result in a smaller effect of turbulence, as the turbulent momentum flux is expected to decrease with decreasing the bubble slip velocity (and size) and increasing the air flow rate (Leitch and Baines 1989). Therefore, low values of β represent weak bubble plumes, while high values of β represent strong bubble plumes.

In addition, relationships for the virtual origin of the flow z_o as well as the initial conditions of u_c and b are obtained from Lima Neto (2012a). Thus, Eqs. (5) and (6) can be solved together with Eqs. (1) - (4) by using a simple explicit Euler type finite difference scheme. Observe that previous numerical studies on bubble plumes normally use Runge-Kutta methods (Wüest et al. 1992, Socolofsky et al. 2008, Lima Neto 2012a, b) or more sophisticated approaches (Buscaglia et al. 2002, Yapa and Chen 2004).

RESULTS AND DISCUSSION

In this section, model simulations were performed for a wide range of gas volumetric flow rates $Q_{g,a}$ and water depths H_d . The tests included initial bubble diameters ranging from fine to coarse bubbles ($d_b = 2\text{-}10$ mm). Furthermore, both weak bubble plumes, where the effect of turbulence was considered important ($\gamma > 1$), and strong bubble plumes, where turbulence was considered negligible ($\gamma = 1$), were investigated. Note that all simulations considered constant concentrations of oxygen and nitrogen in the ambient water. The reader may refer to Singleton and Little (2006) for studies considering the coupling of bubble plume and ambient water models.

First we analyzed the impact of mass transfer and turbulence on air-bubble plume hydrodynamics by comparing model simulations with laboratory and field-scale data available in the literature.

Figure 2 shows present model predictions of the axial variation of centerline liquid velocity (u_n) , plume radius (b) and experimental data of Milgram (1983) for $Q_{\sigma a} = 0.118 \text{ m}^3/\text{s}$ and $H_d = 50 \text{ m}$. The simulations were performed for $\beta = 1.91$, $\alpha = 0.097$, and $\gamma = 1.25$, and considered three conditions: no bubble dissolution, as a reference, and the effect of mass transfer for initial bubble diameters d_{b} of 2 (normally used in finebubble aeration) and 8 mm (assumed herein as a mean bubble diameter in the coarse-bubble experiments of Milgram 1983). For the case of no dissolution, a good agreement can be seen between model predictions and experimental data. For $d_b = 8$ mm, the values of u_c shown in Figure 2(a) were consistently lower than the reference case (no dissolution), with deviations of up to 13%, while the values of b shown in Figure 2(b) were consistently higher, with deviations of up to about 5%. These relatively small differences suggest that for coarse air bubbles, the impact of dissolution was not significant at the present flow conditions. Additional simulations were also conducted for lower values of $Q_{g,q}$, but the effects of dissolution were still small. Nevertheless, simulations for higher values of H_d were also performed, and the deviations were more pronounced. On the other hand, for $d_b = 2$ mm, the values of u_c shown in Figure 2(a) were up to about 50% lower than the reference case, while the values of b shown in Figure 2(b) were up to about 20% higher. This means that for fine air bubbles, dissolution will be important and, as a consequence, the volumetric flow rate Q_{gz} will increase slower with z, which will result in a faster increase in b and faster decay of u_{gz} [see Eqs. (5) and (6)]. Note that for the tests above, the bubble slip velocity u_s was approximately constant and equal to 0.23 m/s, as bubble diameter ranged from about 2 to 10 mm (see Wüest et al. 1992). Another important point is the effect of turbulence. The above-mentioned value for the momentum amplification factor ($\gamma = 1.25$) means that 25% of the total momentum flux is carried out by turbulence. As a comparison, if a constant value of $\gamma = 1.0$ (as assumed by Wüest et al. 1992) were used in the simulations, the deviations from the values shown in Figure 2 would reach up to about 10%. Therefore, for such flow conditions, in which the bubble plumes can be considered strong ($\gamma \cong 1$), the effect of turbulence was relatively small as compared to the mean flow.

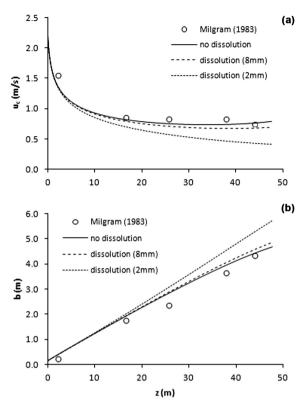


Figure 2 - Comparison between model predictions and experimental data of Milgram (1983) for $Q_{g,a} = 0.118 \text{ m}^3/\text{s}$ and $H_d = 50 \text{ m}$: (a) centerline liquid velocity, and (b) plume radius. Simulations are performed for $\beta = 1.91$, $\alpha = 0.097$ and $\gamma = 1.25$, and under three conditions: no dissolution, and dissolution of air bubbles with diameters d_s of 2 and 8 mm.

Figure 3 shows model predictions of the axial variation of u_c and b and experimental data of Fannelöp and Sjöen (1980) for $Q_{g,a}=0.01~\text{m}^3/\text{s}$ and $H_d=10~\text{m}$. Again, three conditions were considered: no bubble dissolution, and the effect of mass transfer for initial bubble diameters d_b of 2 mm (fine-bubble aeration) and 8 mm (assumed herein as a mean bubble diameter in the coarse-bubble experiments of Fannelöp and Sjöen 1980). The simulations were performed for $\beta=0.81$, $\alpha=0.077$, and $\gamma=1.46$. A good agreement between model predictions and experimental data is obtained for the reference case of no dissolution. For $d_b=8~\text{mm}$, the values of u_c and b almost overlap with the reference case. This confirms that for coarse bubbles, dissolution is negligible at the present flow conditions. However, for $d_b=2~\text{mm}$, the values of u_c shown in Figure 3(a) were up to about 10% lower than the reference case, while the values of b shown in Figure 3(b) were up to about 3% higher. This suggests that even for relatively small water depths as in the present case, dissolution can have an impact on bubble plume hydrodynamics. Regarding the effect of the momentum amplification factor, if a value of $\gamma=1.0~\text{m}$ were used (instead of $\gamma=1.46$), the deviations from the values shown in Figure 3 would reach up to about 17%. For such case ($\gamma=1.46$), the bubble plume can be considered weaker than in the previous condition shown in Figure 2 ($\gamma=1.25$), which means that the momentum carried by the mean flow is small as compared to that carried by turbulence.

Figure 4 shows model predictions of the axial variation of u_c and b and experimental data of Milgram and Van Houten (1982) for $Q_{g,a}=0.0005~\text{m}^3/\text{s}$ and $H_d=3.66~\text{m}$. The same conditions as those in the preceding analyses (see Figures 2 and 3) were considered: no bubble dissolution, and the effect of mass transfer for initial bubble diameters d_b of 2 and 8 mm. The simulations were performed for $\beta=0.11$, $\alpha=0.050$, and $\gamma=2.09$. Model predictions and experimental data agree well with the reference case of no dissolution. For $d_b=8$ mm, the values of u_c and b totally overlap with the reference case. This clearly shows that for coarse bubbles, dissolution is negligible at the present flow conditions. For $d_b=2$ mm, the values of u_c shown in Figure 4(a) were up to about 4% lower than the reference case, while the values of b shown in Figure 4(b) were up to about 1% higher. These results indicate that for the present case, dissolution has a negligible impact on bubble plume hydrodynamics. Regarding the impact of turbulence, if a value of y=1.0 were used (instead of y=2.09), the deviations from the values shown in Figure 4 would be up to about 33%. For this case (y=2.09), the bubble plumes can be considered weaker than in the previous conditions shown in Figures 2 and 3 (y=1.25-1.46).

We also investigated the axial variation of bubble diameter by comparing present model simulations with those from classical bubble plume models accounting for mass transfer, including applications for both aeration and oxygenation under deeper water conditions.

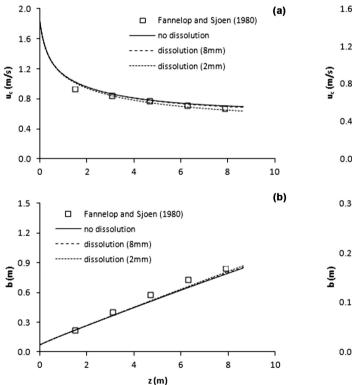


Figure 3 - Comparison between model predictions and experimental data of Fannelop and Sjoen (1980) for $Q_{g,a} = 0.01 \text{ m}^3/\text{s}$ and $H_d = 10 \text{ m}$: (a) centerline liquid velocity, and (b) plume radius. Simulations are performed for $\beta = 0.81$, $\alpha = 0.077$ and $\gamma = 1.46$, and under three conditions: no dissolution, and dissolution of air bubbles with diameters d_b of 2 and 8 mm.

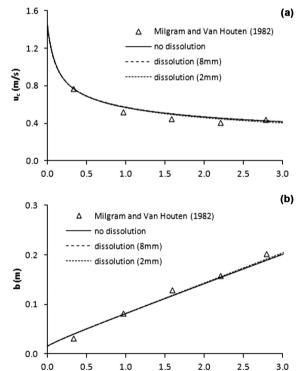


Figure 4 - Comparison between model predictions and experimental data of Milgram and Van Houten (1982) for $Q_{g,a} = 0.0005 \text{ m}^3/\text{s}$ and $H_d = 3.66 \text{ m}$: (a) centerline liquid velocity, and (b) plume radius. Simulations for no dissolution and dissolution of air bubbles with $d_b = 8 \text{ mm}$ are performed for $\beta = 0.11$, $\alpha = 0.050 \text{ and } \gamma = 2.09$, and under three conditions: no dissolution, and dissolution of air bubbles with diameters d_b of 2 and 8 mm.

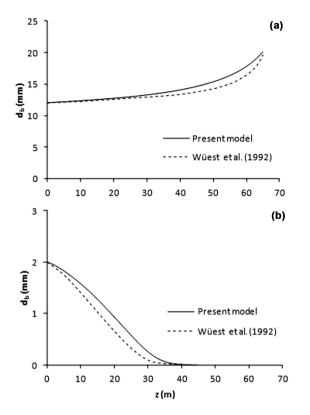
z (m)

In Figure 5 we compare predictions of bubbles' diameter d_b variations with z using the present model and that of Wüest et al. (1992), which was applied to a lake with a diffuser depth $H_d = 65$ m, including two modes of operation: aeration, using an initial bubble diameter $d_b = 12$ mm and an air volumetric flow rate $Q_{g,a} = 0.014$ m³/s; and oxygenation, using an initial bubble diameter $d_b = 2$ mm and an oxygen volumetric flow rate $Q_{g,a} = 0.0062$ m³/s. Figure 5(a) shows that the models agree very well with the case of aeration, with deviations of less than 10%. A gradual increase in bubble diameter from 12 to about 20 mm is clearly seen, which demonstrates that bubble expansion dominates bubble dissolution, as expected for such aeration systems. Figure 5(b) shows a reasonably good agreement between the present model simulation and that of Wüest et al. (1992) for the case of oxygenation, with deviations of up to about 40%. Nonetheless, both models provided a complete dissolution of the bubbles at about z = 40 m. This is expected in fine-bubble systems, which are commonly used for hypolimnetic oxygenation. Overall, the simulations shown in Figures 5(a) and 5(b) suggest that the present model is appropriate to describe both the aeration and oxygenation process.

In Figure 6 we compare predictions of bubbles' diameter d_b variations with z using the present model and 1D integral and computational fluid dynamics (CFD) models used by Buscaglia et al. (2002) to evaluate the effects of aeration plumes in a large combined sewage/stormwater reservoir, including the following conditions: initial bubble diameter $d_b = 5$ mm, water depth $H_d = 77$ m, and two air volumetric flow rates of $Q_{g,a} = 0.00254$ and 0.0254 m³/s. The present model shows a very similar behavior as those obtained from 1D and CFD models, with deviations of less than 10% for both flow conditions. It is interesting to observe that the model proposed herein reproduced well a zone dominated by bubble dissolution, in which d_b decreases with z [up to about z = 60 m in Figure 6(a) and z = 50 m in Figure 6(b)], followed by a zone dominated by bubble expansion, in which d_b increases with z. Furthermore, it can be seen that an increase in the air flow rate $Q_{g,a}$ from 0.00254 to 0.0254 m³/s resulted in final simulated values of d_b (at z = 77 m) increasing from about 4.5 mm [see Figure 6(a)] to 5.5 mm [see Figure 6(b)], respectively. This clearly shows the impact of reduced bubble contact time on d_b for the higher air flow rate, which resulted in larger bubbles reaching the water surface.

A sensitivity analysis was conducted to investigate the effect of each relevant parameter $(H_d, d_b, Q_{g,a})$ and λ) on bubble plume hydrodynamics, for both modes of operation: aeration and oxygenation. Observe that the other relevant parameters $(\alpha, \gamma, u_s, \lambda_s)$ were not included because they are already calculated as a function of H_d , d_b and/or $Q_{g,a}$. Tables I and II show that the impact of H_d , d_b and $Q_{g,a}$ on the variations of u_c and u_c and u_c be significant (from about 10 to 150%). Contrastingly, the impact of u_c (using the typical ranges reported by Lima Neto 2012a, b) was negligible (< 3%). It is also interesting to point out that, as expected, the impact of the parameters was higher for the oxygenation mode than for the aeration mode (except for the effect of u_c , on the variation of u_c , in which the results were of the same order of magnitude).

Figures 7(a) and 7(b) present dimensionless correlations given by Eqs. (10) and (11) which are useful to quickly predict the impact of mass transfer on bubble plume hydrodynamics for the aeration and oxygenation modes, respectively. Note that L is a length scale given by $L = (Q_{g,a}^2/g)^{1/5}$ and R^2 is the coefficient of determination (i.e., the square of the Pearson product-moment correlation coefficient, which is a measure of the linear dependence between two variables). These correlations were obtained by running the present model for different values of d_b/H_d and L/H_d that resulted in a maximum deviation of u_c of 10%, as compared to the reference case of no bubble dissolution. Thus, as the deviations of u_c were consistently larger than the deviations of b (see Figures 2, 3 and 4), this deviation of 10% was taken herein as a threshold



(a) 5 **(mm)** 3 Present model 2 -- Buscaglia et al. (2002) 1D 1 ----- Buscaglia et al. (2002) CFD 0 0 20 40 60 80 7 (b) 6 5 **(mm)** ⁴ ³ Present model 2 ---- Buscaglia et al. (2002) 1D 1 ------ Buscaglia et al. (2002) CFD 0 20 40 0 60 80 z (m)

Figure 5 - Comparison between present model simulations and those from the integral model of Wüest et al. (1992): $H_d = 65$ m and (a) initial bubble diameter $d_b = 12$ mm and $Q_{\rm g,a} = 0.014$ m³/s (aeration); and (b) initial bubble diameter $d_b = 2$ mm and $Q_{\rm g,a} = 0.0062$ m³/s (oxygenation).

Figure 6 - Comparison between present model simulations and those of Buscaglia et al. (2002) considering both 1D integral and computational fluid dynamics (CFD) models: initial bubble diameter $d_b = 5$ mm, $H_d = 77$ m and (a) $Q_{g,a} = 0.00254$ m³/s; and (b) $Q_{g,a} = 0.0254$ m³/s (both aeration).

TABLE I Sensitivity analysis of the present model: aeration mode.

Parameter	Standard value	Range	Variation of u _c (%)	Variation of b (%)
$H_d(m)$	50	25 – 100	+33.151.4	-47.8 - +126.4
d _b (mm)	4	2 -8	-34.0 -+16.4	+14.94.5
$Q_{g,a}(m^3/s)$	0.10	0.05 - 0.20	-23.5 - +30.8	-10.7 - +10.8
λ (-)	0.8	0.6 - 1.0	-1.3 - +0.8	-1.2 - +1.4

TABLE II Sensitivity analysis of the present model: oxygenation mode.

Parameter	Standard value	Range	Variation of $u_c(\%)$	Variation of b (%)
$H_d(m)$	50	25 – 100	+56.667.3	-50.6 - +157.4
d _b (mm)	4	2 -8	-49.8 -+35.5	+25.69.4
$Q_{g,a}(m^3/s)$	0.10	0.05 - 0.20	-27.7 - +36.9	-9.1 - +9.0
λ (-)	0.8	0.6 - 1.0	-1.9 - +2.8	-2.3 - +2.7

to indicate whether the flow conditions were susceptible or not to the effect of mass transfer. Therefore, the regions in Figures 7(a) and 7(b) located above the adjusted curves represent the flow conditions slightly affected by mass transfer (i.e., the regions with relatively large values of $Q_{g,a}$ and d_b where the deviations of u_c are smaller than 10%). In this case, bubble plume hydrodynamics can be predicted disregarding mass transfer. On the other hand, the regions located below the curves represent the flow conditions strongly affected by mass transfer (i.e., the regions with relatively small values of $Q_{g,a}$ and d_b where the deviations of u_c are higher than 10%). For such cases, a model that includes the effect of mass transfer (such as the present model or the CFD model of Buscaglia et al. 2002) must be used in order to accurately predict bubble plume hydrodynamics.

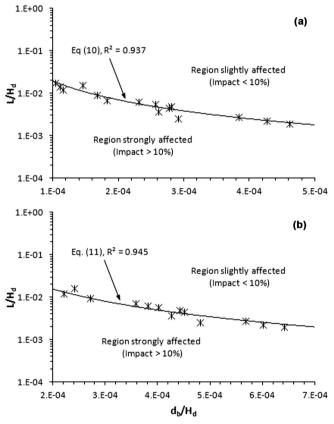


Figure 7 - Dimensionless correlations to predict the impact of mass transfer on bubble plume hydrodynamics for (a) aeration and (b) oxygenation systems. Stars represent model simulations for different values of d_b/H_d and L/H_d that resulted in a maximum deviation of u_c of 10%, as compared to the reference case of no bubble dissolution. The parameter L is a length scale given by $L = \left(Q_{g,a}^2/g\right)^{1/5}$ and R^2 is the coefficient of determination.

Aeration:
$$\frac{L}{H_d} = 2.28 \cdot 10^{-8} \left(\frac{d_b}{H_d}\right)^{-1.483}$$
 (R2 = 0.937)

Oxygenation:
$$\frac{L}{H_d} = 1.24 \cdot 10^{-8} \left(\frac{d_b}{H_d} \right)^{-1.649}$$
 (R2 = 0.945)

CONCLUSIONS

In this study, we incorporated a gas-liquid mass transfer submodel into an integral model for unstratified bubble plumes based on the Gaussian type self-similarity and new functional relationships for the entrainment coefficient and momentum amplification factor. The impact of mass transfer on bubble plume hydrodynamics was investigated for different bubble sizes, gas flow rates and water depths. The results were compared to a wide range of laboratory and field-scale data available in the literature, including both weak bubble plumes (i.e., with relatively low gas flow rates and high water depths and slip velocities), where the effect of turbulence was important, and strong bubble plumes, where turbulence was negligible. It was clearly seen that coarse bubbles have a slight effect on bubble plume hydrodynamics, even for deeper water conditions. On the other hand, for moderate water depths, dissolution can impact bubble plume hydrodynamics if fine bubbles are used. It was also shown that the momentum amplification factor had an important effect on bubble plume hydrodynamics, specially for weak bubble plumes. In many cases analyzed here, both dissolution and turbulence affected bubble plume hydrodynamics, which demonstrates the importance of taking the momentum amplification factor relationship into account.

Simulations of bubble dissolution using the present model and classical models available in the literature resulted in a very good agreement, including both aeration and oxygenation modes of operation under deeper water conditions. Sensitivity analysis of model parameters also showed that the water head above the diffuser, initial bubble diameter and gas flow rate are the most important parameters that affect bubble plume hydrodynamics. Lastly, dimensionless correlations were proposed to verify the impact of mass transfer on bubble plume hydrodynamics, including both aeration and oxygenation systems. These correlations are important to help researchers/practitioners decide whether considering or not mass transfer to model the flow circulation induced by bubble plumes for applications including surface aeration, algal displacement, sediment suspension, and so on. Note that neglecting mass transfer would make the analysis much simpler, provided no interaction with the ambient water quality would be required for the simulations.

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RESUMO

Este artigo apresenta um modelo integral para avaliar o impacto da transferência de gás na hidrodinâmica de plumas de bolhas. O modelo é baseado no princípio de similaridade do tipo Gaussiana e em relações funcionais para o coeficiente de entrada turbulenta e o fator de amplificação da quantidade de movimento devido à turbulência. O efeito da transferência de massa na hidrodinâmica de plumas de bolhas é investigado considerando diferentes tamanhos de bolhas, vazões gasosas e profundidades de água. Os resultados revelaram um impacto relevante quando bolhas finas

são consideradas, mesmo para moderadas profundidades da água. Além disso, as simulações do modelo indicaram que para plumas de bolhas fracas (ou seja, com vazões gasosas relativamente baixas e profundidades de água e velocidades relativas elevadas), tanto a dissolução como a turbulência podem afetar a hidrodinâmica das plumas, o que demonstra a importância de se levar em conta o fator de amplificação da quantidade de movimento. Para condições de águas mais profundas, simulações dos processos de dissolução e descompressão das bolhas utilizando o modelo atual e modelos clássicos disponíveis na literatura forneceram resultados semelhantes tanto para sistemas de aeração como de oxigenação. Análise de sensibilidade mostrou que a profundidade da água, seguida do tamanho das bolhas e da vazão gasosa são os parâmetros que mais afetam a hidrodinâmica das plumas. Finalmente, correlações adimensionais são propostas para avaliar o impacto da transferência de massa na hidrodinâmica das plumas, incluindo tanto sistemas de aeração como de oxigenação.

Palavras-chave: aeração, bolhas, hidrodinâmica, transferência de massa, modelagem, oxigenação.

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