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# Predictive efficiency of distinct color image segmentation methods for measuring intramuscular fat in beef

Eficiência preditiva de distintos métodos de segmentação da cor de imagem para mensurar a gordura intramuscular na carne bovina

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#### ABSTRACT

Intramuscular fat (IMF) influences important quality characteristics of meat, such as flavor, juiciness, palatability, odor and tenderness. Thus, the objective of this study was to apply the following image processing techniques to quantify the IMF in beef: palette; sampling, interval of coordinates; black and white threshold; and discriminant function of colors. Thirty-five samples of beef, with a wide range of IMF, were used. Color images were taken of the meat samples from different muscles, with variability in the IMF content. The IMF of a thin cross-section meat was determined by chemical lipid extraction and was predicted by image analysis. The chemical method was compared with the image analysis. The segmentation procedures were validated by the adjustment of a linear regression equation to the series of values that were observed and predicted, as well as the regression parameters evaluated by the F-test. The predictive power of these approaches was also compared by residual analysis and by the decomposition of the mean square deviations. The results showed that the discriminant function was the best color segmentation method to measure intramuscular fat via digital images, but required adjustments in the prediction pattern.

**Key words**: tissue characterization, meat industry, marbling, image processing, meat quality.

## RESUMO

A gordura intramuscular (GIM) influencia importantes características qualitativas da carne, tais como: sabor, suculência, palatabilidade, odor e maciez. Assim, objetivouse aplicar diferentes técnicas de processamento de imagem para quantificar a GIM na carne bovina: paleta, amostragem, intervalo de coordenadas, limiar de preto e branco e função discriminante de cores. Foram utilizadas 35 amostras de bifes com uma ampla gama de GIM. Foram capturadas imagens coloridas das amostras

de carne de diferentes músculos com uma variabilidade no conteúdo de GIM. A gordura intramuscular da secção transversal e fina de carne foi determinada por extração química dos lipídios e predita por análise de imagem. O método químico foi comparado com a análise de imagem. Os procedimentos de segmentação foram validados pelo ajustamento de uma equação de regressão linear na série de valores observados e preditos e os parâmetros da regressão avaliados pelo teste F. O poder preditivo destas aproximações também foi comparado por meio de análise residual e pela decomposição do quadrado médio dos desvios. Os resultados mostraram que a função discriminante foi o melhor método de segmentação da cor para mensurar a gordura intramuscular via imagem digital, mas necessita de ajustes no padrão de predição.

Palavras-chave: caracterização tecidual, indústria cárnea, marmoreio, processamento de imagens, qualidade da carne.

#### INTRODUCTION

The content of intramuscular fat, also known as "marbling", influences important meat quality characteristics, such as flavor, juiciness, palatability, odor and tenderness. The effect of marbling on tenderness is related to a decrease in the density of meat, lower tension between the layers of connective tissue, increased lubrication of proteins by lipids, and by the capacity of fat to stimulate salivation, all of which result in a more prolonged perception of juiciness (LAWRIE, 2005). In addition, the visual appearance of fat, as

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well as its amount and distribution, also influence the overall acceptability of meat and therefore the choice of consumers prior to purchase.

Visual inspection is widely used in processes within the meat industry for the subjective assessment of quality, from initial classification until the time of purchase by consumers. However, the subjective methodologies of visual evaluation of beef are now being replaced by evaluation that is provided by images because the latter provide more reliability and better stratification of results (FERGUSON, 2004).

There are several techniques to quantify intramuscular fat (IMF) content, such as: chemical analysis (FOLCH et al., 1957; BLIGH & DYER, 1959; HARA & RADIN, 1978; AOAC, 2006); ultrasound (AASS et al., 2009); electrical impedance (ALTMANN & PLIQUETT, 2006); computed tomography (LAMBE et al., 2010); nuclear magnetic resonance (SANTOS et al., 2008) and hyperspectral imaging (LIU & NGADI, 2014). However, few of these methods are acceptable in terms of the quantification of fat in a cross-section of a slice of meat. In addition, few of these methods are satisfactory because they use large amounts of organic solvents, which are expensive, laborious, time consuming, tedious and invasive (destructive), all of which limit their industrial use.

There has been growing interest in the use of digital images in the agricultural and food industries. The processing and analysis of images has been the technology that has most recently been used for the quantification of IMF because it is a technique that is objective, fast, non-invasive (non-destructive), less costly and environmentally sustainable. Consequently, the objective of this study was to evaluate the predictive efficiency, in terms of IMF content, for different color segmentation procedures

applied in the digital image processing of beef as a substitution for chemical analysis.

## MATERIALS AND METHODS

Thirty-five samples of beef were acquired commercially; they were 2.54cm thick and the IMF content ranging from 0.80 to 7.85% (Table 1). The samples were collected from cross-sections of the following muscles: *Gluteus medius* (top sirloin cap, n=9); *Biceps femoris* (outside round, n=1); *Semimembranosus* (inside round, n=13); *Longissimus dorsi* (striploin, n=4); *Semitendinosus* (eye of round, n=4); and *Quadriceps femoris* (knuckle, n=4).

The images of the beef samples were taken using a FinePix S3200 (Fujifilm Corporation, Tokyo, Japan) digital camera with14 megapixels, 24x optical zoom and no flash. The meat samples were placed in a  $20 \times 20 \times 15 \, \mathrm{cm}$  cardboard box with a white background and without a cover; they were exposed to ambient lighting containing 16 fluorescent lamps (40W). The same exposure and focal length were used for all the images. The photographs were taken at a size of 4288  $\times$  2416 pixels with resolution of 72 dots per inch (Figure 1A) on both sides of the slice of meat and near a measurement scale.

The images were processed using the QUANT v.1.0.2 program (VALE et al., 2002). There were four stages in the processing: calibration (ruler); removal of cover of fat and connective tissue; background suppression (Figure 1B); and segmentation of muscle regions and IMF (Figure 1C). To separate the fat from the muscle, five color segmentation procedures were used, which were based on their characteristics in three-dimensional colorimetric space (RGB) and the intrinsic nature of these structures, which are: the color palette, color sampling, coordinate range, black and white

Table 1 - Descriptive statistics of intramuscular fat (%) content observed by chemical analysis and predicted by image analysis (n=35); bias
and mean percentage error (MPE) for the distinct color segmentation procedures.

Procedures	Descriptive statistics <sup>1</sup>						Bias	MPE, %
	Min.	Max.	Mean	SD	SEM	CV	Dias	WII E, 70
		Chem	ical analysis-					
Hara & Radin (1978)	0.81	7.85	3.12	1.76	0.30	56.5		
		Ima	ige analysis					
Palette	0.70	5.25	1.87	0.97	0.16	51.8	-1.25	19.6
Sampling	0.25	5.09	1.70	1.06	0.18	62.0	-1.42	31.8
Coordinates interval	0.44	5.12	1.66	0.93	0.16	55.8	-1.46	32.6
Threshold	0.19	5.15	1.65	0.99	0.17	60.4	-1.47	32.3
Discriminant function	1.52	8.15	3.27	1.45	0.25	44.3	0.15	-38.2

<sup>&</sup>lt;sup>1</sup>/Min. = minimum; Max. = maximum; SD = standard deviation; SEM = standard error of the mean; CV (%) = coefficient of variation.

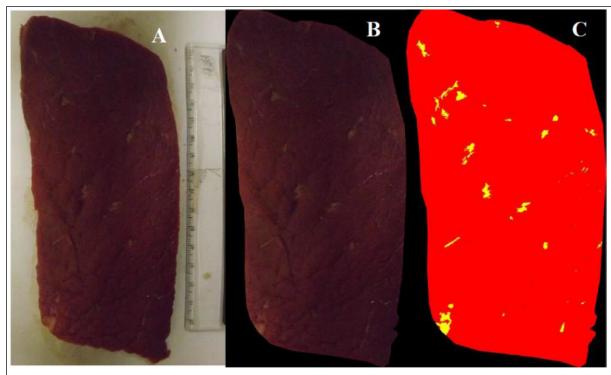


Figure 1 - Original (A), background suppressed (B) and segmented (C) image from Biceps femoris muscle representative of the beef samples

threshold, and discriminant function. During the procedure, the color black was assumed as the background, red as muscle, and yellow as fat (Figure 1C), except for the segmentation by black and white threshold, where the background was the color blue, the muscle was black and the fat was white. The quantification of IMF content was in the proportion (%) of the area occupied by these structures, without calculating the background.

After processing the images, the averages between the two sides of the piece were calculated and were compared using chemical analysis (HARA &RADIN, 1978).

The efficiency of prediction of the different procedures for image processing was evaluated by bias (difference between the mean of the predicted values and the mean of the observed values) and the mean percentage error

$$MPE = \frac{1}{n}\sum_{t=1}^{n}PE_{t}$$
 (MPE), given by , where 
$$PE_{t} = 100\left(\frac{y_{t}-\widehat{y}_{t}}{y_{t}}\right)$$

is the percentage error for the *i*-th observation, assigning the function of underestimated (+) or overestimated (-) to the

observed value.

In addition, the estimates generated by the different color segmentation procedures were validated by adjustment of simple linear regression equations in the range of the observed values (chemical analysis) and predicted values (image analysis) and the regression parameters evaluated by the F-test under the following simultaneous hypothesis test (MAYER et al., 1994):  $H_0$ :  $\beta_0$  = 0 and  $\beta_1$  = 1 where,  $H_0$ = null hypothesis;  $\beta_0$ = intercept of the linear regression between the observed and predicted IMF content; and  $\beta_1$  = slope of line. If  $H_0$  is not rejected, it can be concluded that the procedure predicts the observed values with similarity (a=0.05).

The predictive power of the procedures was also evaluated by residual analysis (DRAPER & SMITH, 1966; MONTGOMERY, 2005; MITCHELL & SHEEHY, 1997) and through decomposition of mean square deviation prediction, as suggested by KORAYASHL& SALAM (2000) as follows:

KOBAYASHI & SALAM (2000) as sollows:  

$$MSD = SB + SDSD + LCS = \frac{1}{n} \sum_{i=1}^{n} (x_i - y_i)^2$$

$$SB = (\bar{X} - \bar{Y})^2$$

$$SDSD = (S_x - S_y)^2$$

$$LCS = 2S_x S_y (1-r)$$

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In which: MSD = mean square deviation between predicted and observed values; SB = squared bias; SDSD= squared difference between standard deviations; LCS= lack of correlation weighted by standard deviations;  $x_i = i$ -th predicted value;  $y_i = i$  i i-th observed value;  $\overline{X}$  = mean of the predicted values;  $\overline{Y}$  = mean of the observed values;  $S_x$  and  $S_y$  = standard errors for the predicted and observed values, respectively; and r= Pearson correlation coefficients between predicted and observed values. It should be noted that for all the calculations of variances, the total of observations (n) was used as a divisor. The prediction model was considered effective when it presented low values for SB, SDSD, and LCS.

## RESULTS AND DISCUSSION

The observed values of IMF ranged from 0.8% to 7.8%, with an average of 3.1%, and there was wide variation around the mean (coefficient of variation > 50%; Table 1), which reflected the reality of beef cuts usually sold in Brazil (PINHO et al., 2011).

Discriminant function was the predictive method which obtained the mean that was closest to the observed mean and that resulted in a prediction with least bias (Table 1), i.e. with a systematic error that represented only 4.81% of the observed value. The low effect of bias in the prediction was due to the multidimensional representation of the adopted procedure, which made it possible to obtain data that fitted well to a simple level of description or the

organization of hierarchy in biology (THORNLEY & FRANCE, 2007). However, the other procedures predicted lower averages than were observed; there were negative biases and also those that systematically higher (Table 1), which indicated significant underestimates.

However, the discriminant function had a higher mean percentage error (MPE) and a negative value, while the color palette had a lower MPE and a positive value (Table 1), demonstrating that the former overestimated (-) with a higher degree, while the latter underestimated (+) with a lower degree of error the observations of the data set. The lower bias and the higher MPE obtained by the discriminant function (Table 1) can be confirmed, respectively, by the lower squared bias (SB) and the higher value for the lack of correlation weighted by standard deviations (LCS) of the discriminant function in relation to the others (Figure 2). This indicates that, on average, the procedure was accurate but that around the mean it was inaccurate. In addition, it should be emphasized that this procedure predicted the magnitude of variation that was closest to that which was observed (minimum and maximum, Table 1; <SDSD, Figure 2).

The F-test for the parameters of the regression equations of observed IMF values over the predicted values by color palette and discriminant function (Figure 3) confirmed non-rejection (P>0.05) of the established null hypothesis ( $H_0$ : $\beta_0$ =0 and  $\beta_1$ =1), which indicated that these procedures can be applied for the quantification of IMF. This fact can be confirmed by the closeness between the lines of least squares (dashed line) and equality (y=x) for these predictive methods

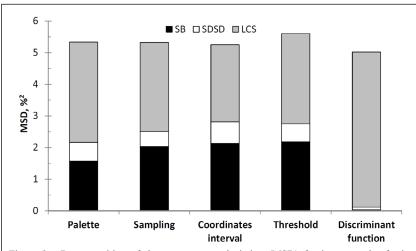


Figure 2 - Decomposition of the mean square deviation (MSD) for intramuscular fat in squared bias (SB), squared difference between standard deviations (SDSD) and lack of correlation weighted by the standard deviations (LCS) from distinct color segmentation procedures of digital images.

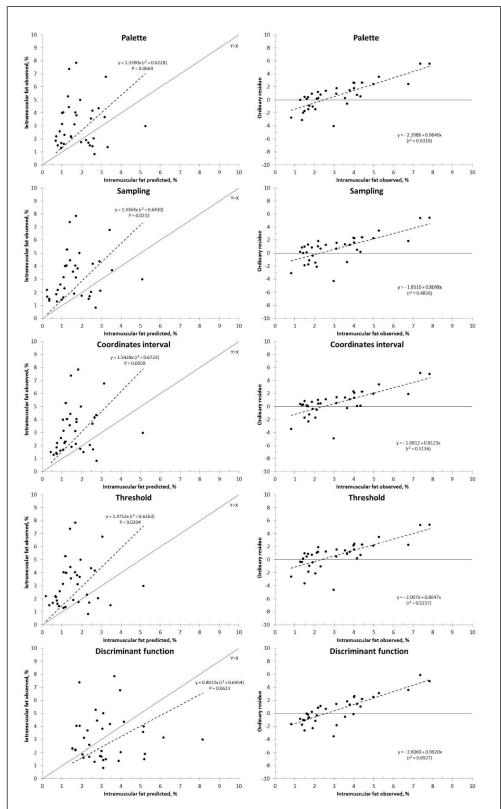


Figure 3 - Relationship between observed (chemical analysis) and predicted (image analysis) values of intramuscular fat from distinct color segmentation procedures, and dispersion of the ordinary residues according to the observed values. The dashed line corresponds to least squares straight line.

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(Figure 3). However, among the procedures tested, the only one that allowed for complete automation in image processing was the discriminant function, which makes it suitable application for industrial usage.

The coefficient of determination ( $r^2$ ) ranged from 0.62 to 0.67 (Figure 3). It is known that the  $r^2$  indicates the accuracy of model, varying from 0 to 1, and that when it has a value of  $\geq$  0.70 it indicates that the model is well adjusted. All the  $r^2$  values generated by the different predictive methods were below expectations (<0.70), although the values were close, especially in the range of coordinates ( $r^2 = 0.67$ ). The models did not fit well, i.e. they had a certain degree of inaccuracy and this can be confirmed by the behavior observed in the mean square variation: MSV = SDSD + LCS (Figure 2).

The validation of the predictive models from the linear regression is an important method. However it is empirical because when there is a lot of dispersion of the points around the mean the rejection of the null hypothesis may be fail and the y=x axial tilt is different from 1 (MITCHELL, 1997); this is not recommended when there is uncertainty about the predicted values (TEDESCHI, 2006).

The dispersion of the ordinary residuals in relation to the observed values (Figure 3) was random around the axis corresponding to zero, but it made it possible to systematically identify the occurrence of overestimation in the levels lower than 2% and underestimation in the levels above 3% of IMF for all the studied procedures; i.e. there was a tendency to decline from 0.80 (sample) to 0.99 (discriminant function) in relation to IMF content. These results may indicate that such procedures are inadequate to predict levels of IMF; however, some adjustments are necessary due to wide and systematic dispersion of residues. As well as the fact that such behavior demonstrated a lack of adjustment of the procedures to the data and their inadequacy in describing the studied phenomenon, the absence of a parameter associated with curvilinear and non-linear relationships can be identified as the main negative factor in relation to prediction of the methods that were studied.

All the procedures had similar predictive power (MSD), with values ranging from 5.02 for the discriminant function to 5.61 for the black and white threshold (Figure 2). However, the discriminant function had a lower squared bias (<SB) and higher mean square variation (>MSV= SDSD + LCS) than the others (Figure 2). The latter was due to the greater lack of correlation weighted by the standard deviations (>LCS), given that it had lower square difference between the standard deviations

(<SDSD). Although the difference in the SB and SDSD between the discriminant function and the other predictive methods was very high, this was not enough to reduce the prediction error (MSD) due to the poor performance of the LCS (> value), which counterbalanced such differences.

When comparing the observed and predicted values, the MSD value will be lower the closer it is to the simulation of measurement (> accuracy and precision). A higher MSV (SDSD + LCS) indicates that the procedure fails to simulate the measurement variability around the mean (precision). A higher SDSD indicates that the procedure fails to simulate the magnitude of oscillation between n measurements. A higher LCS means that the procedure fails to simulate the variation pattern of n measurements (KOBAYASHI & SALAM 2000). Therefore, the discriminant function requires adjustments in the prediction pattern of deviation of an observation based on the arithmetic mean of all the observations in the evaluated data set (>LCS, Figure 2). In other words, in the wide dispersion of data around the y=x equality line (Figure 3) to decrease the LCS and consequently reduce the mean square deviations (<MSD), allowing its use in the prediction of IMF by utilizing digital images. These adjustments can be obtained with greater control over the factors that affect the final quality of the images to be segmented, such as greater control over the brightness (luminosity) and opaqueness (opacity) by changing the lighting (UV light) and the use of polarizing filters when capturing images. This allows for better identification and removal of connective tissue in the stage prior to the segmentation of images, resulting in greater accuracy in the prediction of IMF content than other procedures, considering that the discriminant function has already demonstrated less systematic error (<SB) and simulated the same range (<SDSD).

## CONCLUSION

The discriminant function can be successfully used in digital image analysis to quickly predict the intramuscular fat content in beef with required accuracy for use in industrial conditions; it had a higher prediction efficiency compared to the other tested procedures for color segmentation.

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