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Estimation of Discount Rates in Latin America: Empirical Evidence and Challenges*

Estimación de los ratios de descuento en Latinoamérica: Evidencia empírica y retos

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Samuel Mongrut²

Abstract

This paper compares the main proposals that have been made in order to estimate discount rates in emerging markets. Seven methods are used to estimate the cost of equity capital in the case of global well-diversified investors; two methods are used to estimate it in the case of imperfectly diversified local institutional investors; and one method is used to estimate the required return in the case of non-diversified entrepreneurs. Using the first nine methods, one estimates the costs of equity for all economic sectors in six Latin American emerging markets. Consistently with studies applied to other regions, a great deal of disparity is observed between the discount rates obtained across the different models, which implies that no model is better than the others. Likewise, the paper shows that Latin American markets are in a process of becoming more integrated with the world market because discount rates have decreased consistently during the first five-year period of the XXI Century. Finally, one identifies several challenges that have to be tackled to estimate discount rates and value investment opportunities in emerging markets.

Keywords: Discount rates, cost of equity, emerging markets

Resumen

Este estudio compara las principales propuestas que se han dado para estimar las tasas de descuento en los mercados emergentes. Se han usado siete métodos para estimar el costo de capital propio en el caso de inversionistas globales bien diversificados; se aplicaron dos métodos para estimar dicho costo en caso de inversionistas corporativos locales imperfectamente diversificados; y se utilizó un método para estimar el retorno requerido en el caso de empresarios no diversificados. Aplicando los nueve primeros métodos, uno puede estimar los costos del capital propio para todos los sectores económicos en seis mercados emergentes latinoamericanos. Consistentes con estudios aplicados en otras regiones, se observó una gran disparidad entre las tasas de retorno obtenidas en los diferentes modelos, lo que implica que ningún modelo es mejor que el otro. De igual modo, el artículo demuestra que los mercados de Latinoamérica están en proceso de integración con el mercado mundial debido a que las tasas de descuento han decrecido sistemáticamente durante el primer lustro del siglo XXI. Finalmente, se identifican varios retos que deberán ser abordados para estimar las tasas de descuento y valorar las oportunidades de inversión en los mercados emergentes.

Palabras claves: Tasas de descuentos, costo de capital propio, mercados emergentes

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INTRODUCTION

When we wish to assess the value of a company or an investment project, it is not only necessary to have an estimation of the future cash flows, but also to have an estimation of the discount rate that represents the required return of the stockholders that are putting their money in the company or project. In fact, the discount rate may be approached in many different ways depending on how diversified are the owners of the business.

As a rule, in the literature of corporate finance it is normally assumed that these owners are none others than shareholders with a well diversified investment portfolio and, therefore, the discount rate could be understood as a cost of equity capital, which only depends on the market risk that is addressed by means of the well-known parameter 'beta'. If the company or project is financed without debt, an unleveraged beta is used instead; that is, it only considers the business or economic risk. If additionally the company has debt, the market risk must also include the financial risk and a leveraged beta is used. Alternatively, it could also be possible to consider the required return by creditors too, in which case the discount rate is a 'weighted-average cost of capital'.

The final objective is to estimate the value of the company or investment project as if were traded in the capitals market; in other words, we are looking for a market value. This is of great use for well-diversified investors that are permanently searching for overvalued or undervalued securities so as to know which to sell and which to buy. This arbitrage process allows prices to come close to their fair value¹. However, in Latin American emerging markets, as well as in developed markets, there are local institutional investors (pension funds, insurance companies, mutual funds, among others) which do not hold a well-diversified investment portfolio for legal reasons or due to herding behavior².

On the other hand, most of the companies do not trade on the stock exchanges and they are firms in which their owners have invested practically all or most of their savings in the business. Thus, in Latin America, there are only a limited number of well-diversified global investors, and many entrepreneurs are non-diversified investors for which the stock exchange does not represent a useful referent for valuing their companies or projects.

Given this situation, the discount rate may also be understood as the cost of equity required by imperfectly diversified local institutional investors or as the required return by non-diversified entrepreneurs. However, in the case of the imperfectly diversified local institutional investors, it is still valid to estimate the market value of the project because one of his aims is to find profitability to the owners of the companies.

In the case of the non-diversified entrepreneur, there is no need to estimate the value of the project as if it were traded on the stock exchange unless there is a desire to sell the business to well-diversified global investors or to institutional investors. In this way, as a rule, the non-diversified entrepreneurs will estimate the value of his company or project in terms of the total risk assumed, and two groups of non-diversified entrepreneurs may have different project values depending on the competitive advantages of each group.

Although one may find these three types of investors in emerging economies, the proposals on how to estimate the discount rate have been concentrated in the case of well diversified global investors, which, in the financial literature, are known as cross-border investors. The proposals have been few, and not theoretically sound, in the case of imperfectly diversified institutional investors, and almost non-existent in the case of non-diversified entrepreneurs (Mongrut & Ramirez, 2006).

In this paper, the aim is to compare the performance of the main models that have been proposed in the finan-

¹ To obtain a 'fair' value, the equilibrium model is generally used.

² In several Latin American countries pension funds are legally limited to invest abroad. For example, the investment

limit for foreign investments of Peruvian Pension Funds is 12.5% (Mongrut, Palacios, Rosales, & Fuenzalida, 2010).

cial literature to estimate the discount rate in the case of well diversified global investors, imperfectly diversified investors and non-diversified entrepreneurs in six Latin American stock exchange markets that are considered as emerging by the International Finance Corporation (IFC)³: Argentina, Brazil, Colombia, Chile, Mexico and Peru. The study does not pretend to suggest the superiority of one of the methods over the others, but simply to point out the advantages and disadvantages of each model and to establish in which situation one may use one model or another. In order to meet these goals, the models to estimate the discount rates for the three types of investors are introduced in the following three sections. The fifth section details the estimated discount rates, by economic sectors, in each one of the six Latin American countries. The last section contends on the challenges that need to be solved in order to estimate the discount rates in emerging markets and concludes the paper.

MODELS TO ESTIMATE THE COST OF CAPITAL IN THE CASE OF WELL DIVERSIFIED INVESTORS

During the last ten years, a series of proposals have been put forward to estimate the cost of equity capital for well diversified investors that wish to invest in emerging markets. A compilation of these models may be found in Pereiro and Galli (2000), Pereiro (2001), Harvey (2001) and Fornero (2002). The proposals could be divided into three groups according to the degree of financial integration of the emerging market with the world: complete segmentation, total integration and partial integration. Two markets are fully integrated when the expected return of two assets with similar risks is the same; if there is a difference, this is due to differences in transaction costs. This also implies that local investors are free to invest abroad and foreign investors are free to invest in the domestic market (Harvey, 2001).

According to this definition, the Capital Asset Pricing Model (CAPM), as originally developed by Sharpe (1964), Lintner (1965) and Mossin (1966), is a domestic model that assumes complete segmentation. In the other extreme case, the global or world CAPM is found, a model that assumes complete integration. Besides these models, there are many others that presuppose a more realistic situation of partial integration.

Among the models of partial integration, the following ones have been chosen because they are either theoretically sound (given their assumptions) or popular among practitioners: the Mariscal and Lee's or Goldman Sachs' model, the Lessard's model, the D-CAPM model, the Hybrid model and the Damodaran's model. The differences among these models of partial integration lie on where one could include a critical variable named "country risk", which is defined as the risk that private and public companies or agencies default upon their obligations (Fuenzalida, Mongrut & Nash, 2005). In this sense, the Goldman Sachs' model assumes that the country risk could be included in the risk-free rate; the Lessard's model and the D-CAPM assumes that it can be included in the market systematic risk (beta); the hybrid model and the Damodaran's model assume that it can be included in the market risk premium. Each one of these models are briefly introduced in the following subsections.

The local CAPM

The local CAPM states that in conditions of equilibrium, the expected cost of equity is equal to (Sharpe, 1964):

$$E(R_i) = R_i^L + \beta_i^L (R_M^L - R_f^L) \quad (1)$$

where:

R_i^L	: Local risk-free rate
β_i^L	: Local market systematic risk
$R_M^L - R_f^L$: Local market risk premium using the MSCI Index

The application of this model is comprehensible providing that the capitals markets are completely

³ In the year 2000, the IFC sold the rights of this database to Standard & Poor's.

segmented or isolated from each other. However, this assumption does not hold. Furthermore, as Mongrut (2007) points out, the critical parameter to be estimated in equation (1) is the market risk premium. Unfortunately, the market risk premium is usually negative in emerging markets due to the market's high volatility with negative skewness, as well as the short time span for historical financial series. Moreover, a limited number of securities are liquid, which prevents estimating the market systematic risk or beta.

Global CAPM

The global or world CAPM was originally proposed by Solnik (1974). Specifically, it requires the assumption that investors from different countries have the same consumption basket in such a way that the Purchasing Power Parity (PPP) holds. Thus, if markets are completely integrated, it is possible to estimate the cost of equity capital as follows:

$$E(R_i) = R_B^G + \beta_i^G (R_M^G - R_B^G) \quad (2a)$$

where:

- R_B^G : Global risk-free rate
- β_i^G : Global market systematic risk relative to the global market
- $R_M^G - R_B^G$: Global market risk premium using the MSCI global index⁴

The global risk-free rate usually is approximated using the ten years' return series the United States of America (US) Treasury Bonds.

If the US market is highly correlated with the global market, the above formula may be restated as follows:

$$E(R_i) = R_B^{US} + \beta_i^{US} (R_M^{US} - R_B^{US}) \quad (2b)$$

where:

$$R_B^G = R_B^{US} \quad R_M^G - R_B^G = \frac{R_M^{US} - R_B^{US}}{\beta_{US}^G}$$

- R_B^{US} : US risk-free rate
- β_i^{US} : Market systematic risk relative to the US market
- $R_M^{US} - R_B^{US}$: US market risk premium using the MSCI Index

However, there usually are deviations relative to the PPP, either due to differences in the consumption tastes between the groups of individuals in different countries or to differences in prices of the goods to what they have access (Adler & Dumas, 1983). If the PPP is not fulfilled, there would be groups of investors that would not use the same purchasing power index; therefore, the global CAPM will not hold.

The Goldman Sachs' model

One of the first models found in the literature of partial integration to estimate the cost of equity capital in emerging markets was the one suggested by Mariscal and Lee (1993). This model is also named the Goldman Sachs' model because both authors proposed this model while they were working for that company. They suggested that the cost of equity capital could be estimated in the following way:

$$E(R_i) = R_B^{US} + \beta_i^{S\&P} (R_M^{S\&P} - R_B^{US}) + (R_B^{ME} - R_B^{US}) \quad (3)$$

where:

- $\beta_i^{S\&P}$: Market systematic risk relative to the Standard & Poor's index
- $R_M^{S\&P} - R_B^{US}$: Market risk premium relative to Standard & Poor's index
- $R_B^{ME} - R_B^{US}$: Sovereign risk differential (they called it 'country risk')

⁴ MSCI stands for Morgan Stanley Capital International, a large provider of data.

Note that in this specification the CAPM is estimated relative to the US Standard & Poor's index and that to the sovereign risk is added to the risk-free rate. As a measure of sovereign risk, the difference between the yield to maturity offered by domestic bonds denominated in US dollars and the yield to maturity offered by US Treasury bonds, with the same maturity time⁵, is used. Despite its simplicity and popularity among practitioners, this model has a number of problems (Harvey, 2001):

- A sovereign yield spread (debt) is being added to an equity risk premium. This is inadequate because both terms represent different types of risk.
- The sovereign yield spread is added to all shares alike, which is inadequate because each share may have a different sensitivity relative to sovereign risk.
- The separation property of the CAPM does not hold because the risk-free rate is no longer risk-free⁶.

Lessard's hierarchical model

In 1996, Lessard suggested that the adjustment for country risk could be made on the stock beta and not in the risk-free rate as in the previous approach. In order to gain more insight into this proposal, it assumes that it is possible to state a linear relationship between the stock returns of the US and those of the emerging market (EM) through their respective indexes:

$$R_M^{EM} = a + bR_M^{US} + e_{EM/US} \Rightarrow \sigma^2(R_M^{EM}) = b^2 \sigma^2(R_M^{US}) + \sigma^2 e_{EM/US} \quad (4a)$$

where: $b = \beta_M^{US}$

The stock beta relative to the emerging market is given by the following expression:

$$\beta_M = \frac{\text{Cov}(R_i, R_M^{EM})}{\sigma^2(R_M^{EM})} = \frac{\text{Cov}(R_i, a + bR_M^{US} + e_{EM/US})}{b^2 \sigma^2(R_M^{US})} = \frac{1}{b} \beta_i^{US} \quad (4b)$$

The latter expression may be written as:

$$\beta_i^{EM} \beta_{EM}^{US} = \beta_i^{US}$$

If, and only if, the following conditions are met:

$$\text{Cov}(R_i, e_{EM/US}) = 0$$

$$\sigma^2 e_{EM/US} = 0$$

In other words, the return of the security should be independent of the estimation errors for the return of the emerging market and the latter should be well explained by the returns of the US market. With these assumptions in mind, the equation (2b) could be written in the following way (Lessard, 1996):

$$E(R_i) = R_B^{US} + \beta_i^{EM} \beta_{EM}^{US} (R_M^{US} - R_B^{US}) \quad (4c)$$

However, nothing warrants that both assumptions could hold, hence the following relationships between betas will not be fulfilled⁷:

$$\beta_i^{EM} \beta_{EM}^{US} \neq \beta_i^{US}$$

Though this would be a serious limitation, Lessard's model enjoys some popularity among investment analysts because it increases the beta of the security with respect to that of the emerging market adjusting it by the beta of the emerging market relative to the US. As in the case of the Local CAPM and the Global CAPM, they usually resort to Morgan Stanley Capital International (MSCI) indexes to make the calculations comparable.

⁵ Fuenzalida, Mongrut and Nash (2005) discuss alternative ways to estimate the sovereign risk.

⁶ The separation property states that a combination of a risk-free portfolio with an efficient risky portfolio yields another efficient portfolio.

⁷ Bodnar, Dumas and Marston (2003) use a similar argument to arrive to the same conclusion.

The D-CAPM model

Estrada (2002) takes up the observation made by Markowitz (1959) three decades before: the investors in emerging markets pay more attention to the risk of loss than to the potential gain which they may obtain. In this sense, using a measure of total systematic risk as the stock beta is not adequate because it does not capture the real concern of the investors in these markets.

In this sense, Estrada (2002) suggested a variant of the CAPM, which he called D-CAPM (Downside Risk - CAPM). The D-CAPM uses the Global CAPM model and only substitutes the estimation of the security's beta for the estimation of its D-Beta (Downside Beta) using the concepts of semi-standard deviation and cosemivariance. The Downside Beta is estimated as follows:

$$\beta_i^D = \frac{S_{i,G}^\mu}{S_i^\mu \cdot S_G^\mu} = \frac{E\{\text{Min}[(R_i - \mu_i)0] \cdot \text{Min}[(R_G - \mu_G)0]\}}{\sqrt{E\{\text{Min}[(R_i - \mu_i)0]\} \cdot E[\text{Min}[(R_G - \mu_G)0]]}} \quad (5a)$$

where:

- S_i^μ : Semi-standard deviation of the security
- S_G^μ : Semi-standard deviation of the global market (i.e. global index of MSCI)
- $S_{i,G}^\mu$: Cosemivariance of the security's returns with those of the global market

Hence, the cost of equity is established as a version of equation (2a):

$$E(R_i) = R_B^G + \beta_i^D (R_M^G - R_B^G) \quad (5b)$$

Even though the D-CAPM yields estimates of the cost of equity that are higher than those obtained with the Global CAPM, these still have a low magnitude for emerging markets. Despite this, the model is theoretically sound and represents a good alternative to the Local CAPM and Global CAPM. Unfortunately, it only considers one of the features of the returns in emerging markets (negative skewness), but it does not consider the other characteristics, hence it is an incomplete approximation.

The hybrid model

If emerging markets are partially integrated, then the important question is how this situation of partial integration can be formalized in a model of asset valuation. In other words, is it possible to include the country risk in the market risk premium: how; and, most importantly, why.

Bodnar, Dumas and Marston (2003) contend that a situation of partial integration may be stated in an additive way, meaning that local and global factors are important to pricing securities in emerging markets:

$$E(R_i) = R_f^L + \beta_i^G (R_M^G - R_f^G) + \beta_i^{EM} (R_M^{EM} - R_f^{EM}) \quad (6a)$$

where:

- β_i^G : Beta of the security with respect to the global market
- β_i^{EM} : Beta of the security with respect to the local emerging market

Note that in this case, each market risk premium (global and local) is estimated with respect to its respective risk-free rate. The world MSCI index is used to calculate the world premium and the local emerging market MSCI is used to estimate the local premium for market risk.

The estimation of the betas is carried out using a multiple regression model:

$$R_i - R_f^G = \alpha_i + \beta_i^G (R_M^G - R_f^G) + \beta_i^{EM} (R_M^{EM} - R_f^L) + e_i \quad (6b)$$

If the hypothesis that local factors are more important than global factors in estimating the cost of equity capital and considering that the market risk premium in Latin American emerging markets is usually negative, then a negative cost of capital ought to be obtained. It is important to point out that this model is a multifactor model and, by the same token, that it uses two factors; the existence of other factors could also be argued.

According to Estrada and Serra (2005), there is hardly any evidence that a set of three families of variables can explain the differences between the returns of the portfolios composed by securities from emerging markets. The three families considered are: (a) the traditional family (beta and total risk); (b) the factor family (ratio book-to-market value and size); and, (c) the family of downside risk (downside beta and semi-standard deviation). Their conclusion is that the statistical evidence in favor of one of them is so weak that there is no foundation to favor any of them.

Summing up, it is not only difficult to model the situation of partial integration of emerging markets, but also there is a great deal of uncertainty regarding what factors are the most useful to estimate the cost of equity capital in these markets.

Damodaran's model

If the emerging markets are partially integrated and if the specification given by the equation (6a) is possible, one of the great problems to be faced is that the market risk premium in emerging markets is usually negative; so, the cost of equity instead of increasing will decrease. Damodaran (2002a) has suggested adding up the country risk premium to the market risk premium of a mature market, like the US. In order to understand his argument, let us assume that, under conditions of financial stability, the expected reward-to-variability ratio (RTV) in the local bond emerging market is equal to the RTV ratio in the local equity emerging market, so there are substitutes:

$$\frac{R_M^{EM} - R_B^{US}}{\sigma^{EM}} = \frac{R_B^{EM} - R_B^{US}}{\sigma^{EM}} \Rightarrow R_M^{EM} - R_B^{US} = (R_B^{EM} - R_B^{US}) \left(\frac{\sigma_M^{EM}}{\sigma_B^{EM}} \right) \quad (7a)$$

Note that one is working with US dollars returns and financial stability at a certain level of country risk for local bond and equity markets, hence: $R_B^{US} = R_f^L$

If one approximates the global market by the US market, and if equation (7a) and the previous condition are introduced in equation (6a), one obtains the general model proposed by Damodaran (2002a) to estimate the cost of equity capital:

$$E(R_i) = R_B^{US} + \beta_i^{US} (R_M^{US} - R_B^{US}) + \lambda_i (R_B^{EM} - R_B^{US}) \left(\frac{\sigma_M^{EM}}{\sigma_B^{EM}} \right) \quad (7b)$$

where:

$$\begin{aligned} \lambda_i &: \text{Firm exposure to country risk (lambda)} \\ R_B^{EM} - R_B^{US} &: \text{Country default risk} \\ \frac{\sigma_M^{EM}}{\sigma_B^{EM}} &: \text{Relative volatility ratio (RVR)} \\ (R_B^{EM} - R_B^{US}) \frac{\sigma_M^{EM}}{\sigma_B^{EM}} &: \text{Country risk premium} \end{aligned}$$

Note that the second slope (β) of the equation (6a) has been changed to a new slope denominated *lambda* (λ) in equation (7b). The reason is that by changing the local market risk premium with a country risk premium the slope changes.

This specification is useful because it directly avoids estimating the local market risk premium — the most important parameter in the estimation —, which displays the greatest estimation error (Ferson & Locke, 1998). Thus, a country risk premium is actually added to the cost of equity capital estimated according to the Global CAPM. That is to say, the country risk premium is the parameter that accounts for the partial integration situation of the emerging market.

Damodaran (2003) suggests two ways to estimate the security exposure to country risk (λ): (1) the resulting slope in the regression between the returns of the security with respect to the returns of bonds issued by the emerging country that are not guarantee; and, (2) the ratio between the percentage of revenues (I) that the company (j) obtains from the local market (L) divided

by the percentage of income that companies obtain on average from the local market (P):

$$\lambda = \left(\frac{\%I_j^L}{\%I_P^L} \right)$$

Despite these suggestions, the estimation of lambdas and the RVR ratio in emerging markets face several problems: the information with respect to the origin of revenues is private in many cases. Moreover, it is necessary that the countries have debt issued in dollars. Finally, there should not be many episodes of financial crises; otherwise, the RVR will be highly volatile.

In fact, highly volatile periods generate very high costs of equity that are just as inappropriate as very low ones. One way of overcoming this problem is to follow the suggestion that Walker (2003) has called the “Damodaran’s conjecture” that assumes a RVR equal to 1.50. Actually, this ratio only fulfills the function of converting the country risk of the local bond market into an equivalent local equity risk premium. Walker (2003) suggests that in order to test Damodaran’s conjecture the following model could be estimated:

$$R_i - R_B^{US} = \alpha_i + \beta_i^{US} (R_M^{US} - R_B^{US}) + \beta_i^{B,EM} (R_B^{EM} - R_B^{US}) + e_i \quad (7c)$$

where:

$\beta_i^{B,EM}$: Sensitivity of the security to the sovereign yield spread

If Damodaran’s conjecture is to be valid, the sensitivity of the returns of the security with respect to sovereign yield spread should not be statistically different from 1.5 since it is the relative volatility ratio (RVR). If the constant is not significantly different from zero then one has been built a mimicking portfolio of the security’s return by investing β_i^{US} in the US portfolio, $\beta_i^{B,EM}$ in the sovereign bonds of the emerging market and the difference $(1 - \beta_i^{US} - \beta_i^{B,ME})$ in the US Treasury Bonds (Walker, 2003).

MODELS FOR ESTIMATING THE COST OF EQUITY IN THE CASE OF IMPERFECTLY DIVERSIFIED INSTITUTIONAL INVESTORS

The literature has neither established an adequate way to measure the degree of diversification of an investor portfolio nor whether a situation of imperfect diversification should bear a ‘market price’. Damodaran (2002b) has suggested that the situation of imperfect diversification should increase the cost of capital, so it must bear a ‘market price’ and one way to take account of it is by means of the adjusted or total beta:

$$\beta_i = \frac{\sigma_i}{\sigma_M} \rho_{i,M} \Rightarrow \frac{\sigma_i}{\sigma_M} = \frac{\beta_i}{\rho_{i,M}} = \beta_i^T$$

where:

σ_i : Standard deviation of the security
 σ_M : Standard deviation of the market
 $\rho_{i,M}$: Correlation coefficient between the security returns and the market returns
 β_i^T : Total beta of the security

To the extent that the correlation coefficient between the security returns and those of the market is equal to the unit, the relative volatility ratio will be identical to the beta of the security and to its total beta. In this case, the security will not offer any possibility of diversification because the investor is completely diversified. To the extent that the correlation coefficient is lower than the unit, the investor will be less diversified, and there will be a ‘market price’ for not being well-diversified; then, the total or adjusted beta will be higher than the normal beta.

In the literature, three models have been proposed to adjust for imperfect diversification: (a) the model of Godfrey and Espinosa (1996); (b) the Estrada’s model (2000); and (c) the Damodaran’s model (2002b). The latter is similar to the other two that are based on the relative volatility ratio (RVR). For this reason, this study only considers the first two models.

Godfrey and Espinosa's model

Godfrey and Espinosa (1996) suggested using the so-called adjusted beta or total beta, which, as observed, is none other than the relative volatility ratio (RVR). The model is as follows:

$$E(R_i) = R_B^{US} + (R_B^{EM} - R_B^{US}) + (R_M^{US} - R_B^{US})(0.6) \left(\frac{\sigma_i}{\sigma_M^{US}} \right) \quad (8)$$

These authors accounted for the country risk in the risk-free rate. According to Erb, Harvey and Viskanta (1995), the volatility of the emerging stock markets explains at least 40% of the variation in the credit quality. Then, a way to avoid taking twice the country risk is to adjust 'ad hoc' downwards the relative volatility ratio by 40%. This is the reason why the authors use an 'ad hoc' correlation coefficient equal to 0.60. In this case, they are in fact lowering the beta, but their approach is considered as being an adjusted beta because they use 'ad hoc' adjustments of it.

Finally, note that the sovereign yield spread is added to the risk-free rate without making any assumption. Furthermore, there is no theoretical foundation to make an arbitrary adjustment in the correlation coefficient. Despite these problems, this model gained some attention from practitioners at the end of the nineties.

Estrada's model

In line with the argument that the downside risk is truly relevant for investors in emerging markets, Estrada (2000, 2001) proposes the following general expression to estimate the cost of equity using the relative volatility ratio (RVR):

$$E(R_i) = R_B^{US} + (R_M^G - R_B^{US})(RVR_i^G) \quad (9a)$$

where:

RVR_i^G : Relative volatility ratio of the security with respect to the global market.

In turn, the RVR may take one of the following specifications:

$$RVR_i^G = \frac{\beta_i}{\beta_G} \quad (9b)$$

$$RVR_i^G = \frac{\sigma_i}{\sigma_G} \quad (9c)$$

$$RVR_i^G = \frac{S_i}{S_G} \quad \text{where:}$$

$$\sqrt{\left(\frac{1}{T} \right) \sum (R_i - \mu)^2 \quad \forall R_i < \mu} \quad (9d)$$

The three specifications may be replaced in the equation (9a) to obtain one of the three versions of Estrada's model⁸. Despite this, it is important to point out that none of the three specifications has a sound theoretical foundation, and that they are 'ad hoc' adjustments to estimate the cost of equity capital.

ESTIMATION OF REQUIRED RETURNS FOR NON-DIVERSIFIED ENTREPRENEURS

As Mongrut and Fuenzalida (2007) state, more than 95% of all the companies in Latin America are micro, small or medium companies. Thus, it is highly unlikely to find well-diversified investors among the owners; therefore, all the models studied above are inadequate. This is due to the fact that these investors are exposed to their investment total risk and not only to the systematic market risk.

Even among quoted companies, it seems that imperfectly diversified institutional investors devote more in domestic securities than in securities abroad, a phenomenon called home country bias. In this sense, one should expect that local factors influence more in the security pricing rather than global factors.

⁸ Estrada proposed these measures for stock exchange indexes in his work of year 2000, and for industries in his paper of year 2001. Nevertheless, his argument can be extended to individual securities.

In fact, Koedijk, Kool, Schotman and Van Dijk (2002) carried out a study in order to find out whether local and global factors affected the estimation of the cost of equity capital. They concluded that the local factors accounted for a substantial part of the estimated cost of capital, which they attributed to the so-called home country bias.

More recently, Koedijk and Van Dijk (2004) have verified, from a sample of nine industrialized countries, that in the case of approximately 95% of this sample of 3,300 stocks the estimate of the cost of equity capital with the local CAPM does not differ significantly from that obtained with the International Capital Asset Pricing Model (ICAPM) that includes a premium for exchange rate risk. This indicates once again that local factors are sufficient to estimate the cost of equity capital in some developed markets.

Furthermore, Harvey (2000) showed that historical returns in emerging markets are explained by the total volatility of these returns, suggesting that total risk is one of the most important factors. Stevenson (2001), in turn, has shown that, if investors want to have an improvement in the performance of their international investment portfolio in emerging markets, it is useful to consider measures of downside risk in building such portfolio.

The relationship between total risk and returns is given not only in historical terms, but also this relationship persists with ex ante estimations of risk and profitability. Mishra and O'Brien (2005) examined the relationship between ex ante estimates of cost of capital and total risk (volatility of returns) for a sample of securities in emerging markets during the period 1990-2000. They found that total risk was the most significant factor in explaining the ex ante estimations of cost of capital.

In a consistent way with this study, Harvey (2004) saw a significant relationship between the different components of country risk, estimated ex ante and the implicit estimation of the cost of capital in emerging

markets⁹. This implies that not only total risk but also political, economic and financial risk — which are components of country risk — are associated to an ex ante estimation of the cost of capital. On the other hand, Erb, Harvey and Viskanta (1996a) have shown that these components are positively correlated to the measure of credit risk rating made by the *Institutional Investor Magazine*.

Twice a year, since 1979, this magazine publishes a Country Credit Rating (CCR) of each developed and emerging country, covering a total of 150 countries. To the extent that this CCR is closer to one hundred it means less credit risk for the country as a whole; and to the extent that it is closer to zero it indicates a greater credit risk. Erb, Harvey and Viskanta (1996b) have proposed the following model (EHV) to estimate the required return (based in the CCR) for the countries that are included in this credit risk ranking:

$$E(R_{i,t}) = R_B^{US} + \alpha_0 - \alpha_1 \text{LN}(\text{CCR}_t) \quad (10a)$$

where:

$\text{LN}(\text{CCR}_t)$: Natural logarithm of the country credit rating for period t

The two alpha parameters are estimated on the basis of the following cross-section and times series regression:

$$R_{i,t} = \alpha_0 - \alpha_1 \text{LN}(\text{RRC}_{i,t-1}) + e_{i,t} \quad (10b)$$

In this case, a cross-section time series regression analysis is performed between the series of the semi-annual market returns indexes for all countries (developed and emerging) against the natural logarithm of the CCR lagged one semester to avoid “looking ahead bias”. Once the required semi-annual return is estimated using equation (10a), the CCR from the contemporaneous semester is applied to estimate the forward looking

⁹ The implicit cost of capital is the discount rate that makes the present value of the expected cash flows of a company (based on the projections from analysts) equal to the current market value of the company (Harvey, 2004).

required return. Finally, the equivalent annual figure is estimated for each country¹⁰.

A great advantage of this method is that it can estimate the forward looking required return for a country. Given that the number of countries that have a CCR is higher than the number of countries that have a stock exchange market, the model can be estimated with all the countries with CCR and capital market, and, then, substitute the corresponding CCR for a country in the equation (10a) without a capital market and obtain its corresponding required return.

Despite this advantage, the model also has some disadvantages; one of them is that the CCR is only developed twice a year by *Institutional Investor*. In this way, the rating exhibits little volatility, and the estimation of the model (10b) will have a low explanatory power (a low goodness of fit), even if the parameters obtained are statistically significant. A more serious disadvantage is that the model can only be applied to a country as a whole and not to an individual company. The CCR, which includes political, economic and financial risk, is expected to have a systematic component and a specific component. This implies that credit risk will not affect companies operating in the country in the same way and, therefore, required returns should be different for each company.

ESTIMATING DISCOUNT RATES IN LATIN AMERICAN EMERGING MARKETS

This section estimates the discount rates for the different economic sectors in six Latin American emerging markets: Argentina, Brazil, Colombia, Chile, Peru and Mexico. Venezuela was not included in the sample because it has very few liquid stocks. The following summarizes the result of seven models for estimating the cost of equity assuming global well-diversified investors, two models for estimating the cost of equity assuming imperfectly diversified institutional investors, and one model for non-diversified entrepreneurs.

Sample and methodology

We estimated costs of equity according to different models for six periods of five years: 1995-2000, 1996-2001, 1997-2002, 1998-2003, 1999-2004 and 2000-2005. We have avoided estimating the costs of equity for more recent periods because the goal is to find out what is the situation of Latin American markets at the beginning of the 21st Century.

One important filter for the data was liquidity. Table No. 1 shows the total number of liquid securities by country that had a stock market presence higher than

Table 1.

Number of securities considered by year for the period 1995 – 2005

Period	Argentina	Brazil	Colombia	Chile	Mexico	Peru	Total
95-00	35	113	13	56	43	28	278
96-01	37	129	14	57	44	29	301
97-02	39	136	16	58	46	24	319
98-03	43	137	16	58	47	24	325
99-04	46	141	20	58	49	25	339
00-05	49	143	22	60	50	25	349

Source: Prepared by authors

¹⁰ Upon estimating the alpha parameters in equation (10b) the last observation corresponding to the CCR must be left aside so that this value may be replaced in equation (10a).

75% within each one of the periods of five years. Stock market presence is defined as the ratio between the days that the stock has traded divided by the total number of trading days at the stock exchange¹¹.

Thus, for the first period 278 securities were considered to estimate the cost of capital, whereas in the last period 349 securities were taken into account. It is worth mentioning that the number of liquid securities does not coincide with the number of different companies because sometimes there are two or three types of liquid stocks attached to one company.

The next step was to estimate the cost of equity models for each liquid security using equations 1, 2a, 3, 4c, 5b, 6a, 7b, 8 and 9c. In the case of model 7b, the Damodaran's conjecture was considered. The local risk-free rate was approximated using the shortest-term rate offered by the bill notes from the emerging markets Central Banks. In the case of the US, the return of the one-month bill notes was used. Due to the fact that the cost of equity at the end of every year was estimated, the risk-free rates values used to calculate the costs of equities were those from the end of each year.

With the exception of models 1 and 6a, all market risk premiums were estimated with respect to the US market, so the value of 5.5% was applied to compare this study with previous studies that used the same figure such as the ones of Stulz (1995), Lessard (1996), and Estrada (2000, 2001 and 2002). For models 1 and 6a, we used the average continuously compounded excess return of the MSCI local stock market index for the longest time-span¹².

As it is standard in financial literature, the securities' betas were calculated using linear regressions with monthly returns for the last five years. The estimations

were updated each year using a rolling window of five years in a way that the variations in the cost of equity are due to variations in the securities' betas through time. All the stock returns were continuously compounded returns and in US dollars.

Costs of equity in Latin American emerging markets

Tables A1 to A6 in the Appendix show the annual costs of equity for the different economic sectors in the six countries. To obtain these results, simple averages of the costs of equity of all the securities in the same sector within the same model were calculated. Also, the authors followed the industry classification given by Economática.

In the case of globally well-diversified investors, under a completely integrated market and under a complete segmented market, the costs of equity were obtained through simple averages of the estimates by sectors using the Global CAPM and the Local CAPM models, respectively.

In the case of a partial integrated market, the costs of equity were estimated by averaging the results of the following models (Mariscal & Lee, 1993; Lessard, 1996, D-CAPM, & Damodaran, 2002, 2003)¹³. The results from the hybrid model were not considered to calculate the averages per sector because they were negative costs of equity for two markets (Argentina, Chile).

In the case of imperfectly diversified local institutional investors, the costs of equity were obtained by averaging the results of the Godfrey and Espinosa's model and the Estrada's model (2000, 2001)¹⁴. This

¹¹ The number of securities considered by economic sector and per country is available upon request.

¹² Note that currently the estimated US annual market risk premium is around 3% using more than 200 years of data (Dimson, Marsh, & Staunton, 2003; and Siegel, 2002). This would be the most adequate US market risk premium to use instead of the 5.5% that it is used here for comparison purposes.

¹³ The estimated costs of equity using each one of these models are not reported in this work, but are available on request.

¹⁴ An alternative methodology is the one followed by Collins and Abrahamson (2006). These authors obtained a market index per sector and per country and then they estimated the cost of equity of each economic sector. This methodology is not adequate for Latin American capital markets because they are heterogeneous with respect to the number of liquid securities per sector.

procedure of averaging the resulting costs of equity through the different models per economic sector was proposed in the work of Fama and French (1997). These authors found that standard errors in the estimation of the Local CAPM and the Three-Factor Model of Fama and French (1993) could be higher than 3% on an annual basis, so one way to reduce these standard errors is by averaging the results from different models that assume the same degree of market integration¹⁵.

Table A1 to Table A6 may raise some observations. For instance, the estimated costs of equity for well-diversified investors under a total segmented market (Local CAPM) are extremely volatile, in many cases negative and in other cases excessively high such as in Argentina. This latter result could be explained because, under a situation of bear markets, emerging markets become more correlated with developed markets and, given the high volatility, it is not surprising to have high costs of equity estimations. However, if the crisis is more localized to a region, the low correlation between emerging market returns and developed market returns do not change and the costs of equity estimations tend to be small.

On the other hand, given the excessive volatility of Latin American emerging markets and the properties of their stock returns (negative skewness and excess of kurtosis), it is not surprising that in some cases there are negative estimations of the market risk premium and, consequently, of the costs of equity using the Local CAPM. Together, all these problems render the Local CAPM model useless for the estimation of the cost of equity in these markets.

In the case of complete integration, under either a regional contagion or financial markets' stability,

the estimation of the costs of equity are rather of low magnitude given the low correlation between emerging markets and developed markets. In other words, the estimated betas do not capture the complete systematic risk that a global investor faces when investing in Latin American emerging markets. In Chile, for example, there are a few sectors where the costs of equity are excessively volatile due to very high systematic risk estimations (betas).

When a situation of partial integration is considered, it can be seen that the costs of equity estimations are usually higher than the ones estimated under complete integration for all capital markets. However, the absolute magnitude of the estimated costs of equity is still quite low because they are on average in the neighborhood of 10%. This magnitude is counter intuitive because a global well-diversified investor probably will require a higher cost of equity to invest in Latin American markets.

Higher costs of equity are obtained using the models of imperfectly diversified institutional investors because, on average, they are higher than the costs of equity obtained in the case of partially integrated markets (with the exception of Brazil and Mexico). Unfortunately, the applied models lack sound theoretical foundation.

Note that all estimated costs of equity decrease across the six five-year periods for most of the economic sectors and in all countries (with the exception of the ones estimated using the Local CAPM). In other words, the cost of equity estimated at December 31st of the year 2000 decreased substantially when compared to the cost of capital estimated at October 31st of the year 2005. This fact indicates a process of financial integration with the world market.

Table A7 to Table A12 show the average statistical significance of the securities' betas projected with each model by degree of investor's diversification. Each beta was estimated with the continuous last sixty monthly compounded returns in dollars and adjusted by dividends within in each one of the following five

¹⁵ The Three Factor Model is a multifactor model assumes that additionally to the market risk premium there are two other factors that help to explain the cross-sectional variation of stock returns: the book-to-market ratio and size. These latter two factors are being considered anomalies and are supposed to disappear in the long-term; this is the reason why one does not consider this model in this research.

periods: 1995-2000, 1996-2001, 1997-2002, 1998-2003, 1999-2004 y 2000-2005¹⁶.

Table A7 shows that Local CAPM, on average, is the model that has a high proportion of significant betas at 95% confidence level in all countries: Argentina (86%), Brazil (90%), Colombia (77%), Chile (95%), Mexico (87%) and Peru (75%). This is consistent with the current literature that shows that local factors are more important than global factors to estimate the cost of equity. For instance, the betas' significant proportion using the Global CAPM was Argentina (56%), Brazil (78%), Colombia (12%), Chile (75%), Mexico (79%), and Peru (40%). Note that this is a simple way to assess which country is more integrated than the other and the results are according to the intuition. Furthermore, it is possible to observe that in the case of Argentina the proportion of statistically significant betas decreases in the more recent periods, probably due to the Argentinean crisis, while the opposite occurs with Brazil and Chile. This shows that Latin American countries do not have the same degree of integration, and it also shows that the speed of integration is quite different.

In the case of those markets that are less integrated (Argentina, Colombia and Peru), the D-CAPM plays a very important role because the proportion of statistically significant betas increases if only the downside systematic risk is considered: Argentina (87%), Colombia (74%) and Peru (76%). In the same way, the use of the D-CAPM in the other three markets increases the proportion of statistically significant betas, but on average these are of a lower magnitude than those obtained with the Global CAPM.

In general, the majority of the estimated costs equity is statistically significant; this is even true in the case of partially integrated markets where global betas were used to estimate Damodaran's model and global and local betas to estimate the Lessard's model, which are

not reported. Furthermore, in the case of imperfectly diversified local institutional investors, the relative volatility ratio with Estrada's model and with the Godfrey and Espinosa's model, on average, is statistically significant at 95% confidence level in all countries.

Required return in Latin American emerging markets

This section shows the results of estimating equation (10a) using the cross-section time series method of Erb, Harvey and Viskanta (EHV). First, the equation (10b) was estimated using the semi-annual returns of the MSCI stock market indexes and the semi-annual country credit rating (CCR) for each country from September 1987 to March 2005. Then, the estimated parameters were used to fill equation (10a) to estimate the forward looking semi-annual required return per country using the last CCR corresponding to September 2005. This figure was finally annualized.

Table A13 shows the estimated required returns (RR) for seven Latin American emerging markets (including Venezuela). The first table shows the results considering all markets (emerging and developed); the second table shows the results considering only emerging markets and the third table shows the results considering developed markets and only Latin American emerging markets jointly.

As can be seen, the best results are obtained in the third estimation implying that Latin America as a region is different from the remaining emerging markets regions in the world; so, it only makes sense to compare it, as a region, with developed markets. However, the three results of Table A13 are consistent in the sense that they show that Chile has the lowest required return, while Argentina has the highest required return. Furthermore, the required returns obtained are higher than the costs of equity obtained before, which must be the case because we are dealing with credit risk as a total risk.

Even though these required returns are appropriate in the case of non-diversified entrepreneurs, there are two problems associated with these estimations: the

¹⁶ All periods begin in January of the corresponding year and end in December of the fifth consecutive year, with the exception of the last estimation period that begins in January of the year 2000 and ends on October 31st, 2005.

CCR is updated only twice every year, and the required returns could only be estimated for the whole country. In fact, it is important to state that the goodness of fit of the regression between the stock exchange returns of the 46 countries considered (25 classified as emerging economies and 21 as developed countries) with the corresponding CCR is practically null (1%) (not reported). This implies that the variability of the returns is poorly accounted by the variability of the CCR due to its low frequency.

CONCLUSION

Given the previous results, it is important to point out that none of the previous methods account for all the features that one could face in emerging markets when trying to assess an investment project. These features are associated with the non-normality of stock and bond returns (negative skewness and excess of kurtosis), the lack of an enough time span for historical market data, the fact that markets are incomplete, the situation of partial integration and the heterogeneous degrees of diversification among investors in emerging economies.

Given the fact that stock returns are not allocated according to a normal distribution, it is not possible to use this argument to apply the CAPM as asset pricing model in emerging markets. The other possibility would be to assume a quadratic utility function, but it is well known in the literature that this specification is not adequate because it requires that the representative investors have a constant absolute risk aversion (CARA), which, in turn, implies that they will not change its optimal decision across time. This is clearly an unrealistic assumption.

Alternatively, the Arbitrage Pricing Theory (APT) or the three factor model of Fama and French (1993) may be used. However, there is no clear guidance concerning what are the right factors to apply in the case of the APT, and the investor is looking for long-term capital asset pricing model to value real investments. Therefore, the three factor model of Fama and French

cannot be used because it is a short-term asset pricing model that takes into account anomalies that, in the long-term, should disappear.

Concerning the short time span for the historical market data, the situation is not possible to solve because, in order to estimate a decent market risk premium, it is necessary to have a long time span; otherwise, the standard error will be of such dimensions that it will leave a lot of uncertainty around the estimation. However, the latter problem is not the most important; the real concern is the negative market risk premiums obtained given the stock returns' properties. In this case, a negative market risk premium does not have any financial meaning. Unfortunately, the local CAPM, the Lessard's model, and the hybrid model rely upon local stock market data, that usually is not available or it is biased, due to the problems discussed above.

A market is called complete when it is simple to find a *twin security* that spans the risk of the non-traded asset for every possible state of nature and future period. In other words, when finding a quoted stock that can be used as a benchmark for the non-traded asset is relatively easy. Mongrut and Fuenzalida (2007) have shown that Latin American emerging markets are highly illiquid and that liquid stocks are concentrated around certain economic sectors. Hence, for the vast majority of economic sectors, it is not possible to find a *twin security*. Besides, as Bodnar et al. (2003) pointed out, the option of completing markets using market data from other stock markets is not a good choice given the restrictive assumptions that must be imposed and the poor estimations for emerging markets. Furthermore, it is important to state that the use of the CAPM is not justified in incomplete markets, even if *twin assets* could be found.

In particular, Herings and Kluber (2000) showed that the CAPM did not adjust to incomplete markets even with different probability functions for stock returns and different utility functions. However, given the low magnitude of the estimation errors obtained, these authors suggest that it is possible to apply it in incomplete markets, although it does not produce the

desired results. Unfortunately, none of the previous models tackle really the problem of the emerging market incompleteness because this would imply to have many possible values for the investment project instead of just one *market value*. Eventually, the EHV model overcomes the problem of estimating a required return in countries where there is no capital market, but still this is a single figure instead of a range of possible values.

Most of the models deal with the situation of partial integration. Certainly it seems that the literature has been focused in this important fact and that the main variable to characterize this situation has been the country risk premium. All models of partial integration took into account the country risk either in the risk-free rate, the estimation of betas or in the market risk premium. From these three ways of including the adjustment for country risk, the D-CAPM and the Damodaran's models are the only ones which are theoretically sound, given their assumptions, and realistic. The Hybrid and the Lessard's models are also theoretically sound, but somehow misspecified because the partial integration is not necessarily linear and additive, and the systematic risk is not a crucial risk in emerging markets but total risk.

Hence, although the Damodaran's and the Estrada's models (D-CAPM) are the ones which are theoretically sound, they do not cope with all the necessary issues that must be taken into account when evaluating investment proposals in emerging markets. They do not deal with the problem of imperfect or non-diversification. It could be argued that this criticism is somehow unfair because these two models were put forward for well-diversified investors, but the fact that practitioners are using a version of these models to estimate the cost of equity for imperfectly diversified institutional investors produces a mental bias.

The Godfrey and Espinosa model lacks a theoretical foundation and certainly is an 'ad hoc' specification based upon circumstantial empirical evidence. The Estrada (2000, 2001) specification is well-grounded in the capital market line (CML) when using the specification (9c). In fact, the underlying assumption is that

the stock is perfectly correlated with the market index. However, this fails to recognize that many investment projects are actually not perfectly correlated with the market and an entrepreneur must pursue this goal. A better application of the Estrada proposal would be for estimating the required returns of venture capitalists that could have already a diversified investment portfolio that is not correlated to the market portfolio, and in RVR would be between the project and the venture capitalist investment portfolio instead of that of the market.

All the models, with the exception of the EHV model, seek to estimate the value of the project as if it were traded on the capital market; that is, they seek to estimate a market value for the investment project. However, in Latin American emerging markets there are numerous non-diversified entrepreneurs (more than 95% of the total number of companies) that are not corporate firms. In this sense, the valuation task in emerging markets goes far beyond finding a value for the investment project; it must aim to anticipate contingent strategies to face possible future scenarios. It must recognize that to find a unique estimation of the cost of equity would bias the investor mentality towards the illusion of one possible future instead of many possible ones.

In this sense, there are four main challenges that financial valuers must face in emerging markets:

1. To move from single point estimates of discount rates and project values to a range of possible values given the anticipated scenarios and contingent strategies that have been devised.
2. To develop theoretically sound models for estimating the cost of equity for imperfectly diversified institutional investors in emerging markets.
3. To develop theoretically sound models for non-diversified entrepreneurs in emerging markets.
4. To search for a better specification to characterize the situation of partial integration of emerging markets.

Besides, it should be noted that country risk affects in a different way each company. As Sabal (2004) has

pointed out, in the case that the country risk is completely unsystematic, it would be incorrect to include it in the estimation of the discount rate. This is precisely the case of the non-diversified entrepreneurs that are fully exposed to country risk through the unanticipated variations in the local interest rates.

In this sense, it would more convenient to incorporate the country risk in the estimation of cash flows of the project through a prospective and risk analysis process instead of trying to summarize it into the discount rate. It should be considered that the underlying rationality of non-diversified entrepreneurs is quite different from the underlying rationality of global well-diversified investor¹⁷. Hence, valuers should stop using versions of the CAPM for well-diversified investors in the cases where non-diversified entrepreneurs want to assess their investment opportunities.

In the latter case, the discount rate will have necessarily a strong subjective component and the same will occur with the value of the project. This implies that the same project could have different values depending on the competitive advantages that entrepreneurs bring with them to the project. In this sense, the value obtained will no longer be a market value, but a required value given the project total risk that the entrepreneur is facing.

Paradoxically, proposals about how to estimate discount rates when subjectivity becomes relevant (i.e. non-diversified entrepreneurs) are scarce. This lack of proposals is really striking considering that these cases are the most important ones in Latin American emerging markets. Unless financial valuers address seriously the previous challenges, the practitioners will continue to value companies and investment projects as they value the 0.03% of traded companies in Latin America.

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APPENDIX

Table A1.

*Estimated Costs for Argentina Period: 1995-2005**Totally integrated market*

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fishery	6.37%	6.05%	5.71%	5.23%	4.87%	5.09%
Food and Beverages	7.58%	7.20%	7.11%	6.71%	5.45%	5.63%
Construction	7.42%	7.22%	6.77%	6.49%	5.65%	5.03%
Electric Energy	7.12%	6.79%	6.43%	6.41%	6.45%	6.49%
Finance and Insurance	8.11%	7.85%	7.46%	6.99%	7.02%	7.06%
Industrial Machinery	5.41%	5.11%	5.41%	5.24%	5.54%	5.74%
Non-metallic Minerals	6.32%	6.25%	6.02%	6.11%	6.05%	5.93%
Others	7.73%	7.34%	6.97%	6.44%	6.00%	6.18%
Pulp and Paper	6.21%	6.36%	6.24%	6.08%	6.45%	6.44%
Oil and Gas	6.33%	6.19%	5.90%	6.23%	6.41%	6.41%
Chemicals	6.53%	6.12%	5.85%	5.16%	4.99%	4.82%
Steel Industry and Metallurgy	8.22%	7.97%	7.73%	7.09%	6.56%	6.49%
Telecommunications	8.01%	7.81%	7.69%	7.13%	7.25%	7.33%
Textiles	8.58%	8.66%	8.73%	8.50%	8.48%	8.46%
Vehicles, Parts and Accessories	5.38%	5.23%	4.96%	5.02%	5.78%	5.77%

Partially integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fishery	10.63%	10.07%	9.55%	8.74%	8.27%	9.03%
Food and Beverages	12.82%	11.84%	11.50%	11.15%	8.63%	9.23%
Construction	13.99%	13.27%	12.26%	10.36%	8.39%	8.72%
Electric Energy	12.45%	11.52%	10.82%	10.16%	10.18%	10.34%
Finance and Insurance	13.50%	12.53%	11.67%	10.52%	10.34%	10.87%
Industrial Machinery	10.78%	9.46%	7.99%	7.17%	7.20%	7.53%
Non-metallic Minerals	11.24%	10.98%	10.47%	10.99%	11.07%	9.93%
Others	13.06%	11.46%	10.60%	9.89%	8.93%	9.53%
Pulp and Paper	12.52%	13.17%	12.82%	12.11%	12.82%	12.39%
Oil and Gas	11.02%	10.90%	10.54%	10.75%	11.50%	11.57%
Chemicals	12.40%	11.13%	10.40%	8.53%	8.13%	7.56%
Steel Industry and Metallurgy	14.16%	13.32%	12.77%	11.55%	10.45%	10.39%
Telecommunications	14.47%	12.94%	12.95%	12.61%	12.43%	12.82%
Textiles	15.86%	16.17%	16.36%	16.50%	16.83%	17.75%
Vehicles, Parts and Accessories	9.37%	9.16%	8.77%	7.86%	9.16%	9.31%

(continues) →

Totally segmented market (continues)

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fishery	44.03%	45.40%	46.30%	48.26%	48.91%	48.17%
Food and Beverages	40.51%	41.55%	40.88%	42.61%	47.00%	46.54%
Construction	39.75%	40.02%	41.73%	42.98%	45.20%	47.13%
Electric Energy	41.84%	42.34%	43.43%	42.56%	42.54%	42.55%
Finance and Insurance	38.73%	38.41%	42.04%	41.51%	40.73%	41.11%
Industrial Machinery	44.66%	46.29%	44.97%	45.91%	45.90%	46.04%
Non-metallic Minerals	42.92%	43.28%	45.12%	43.56%	44.43%	45.80%
Others	39.92%	40.33%	42.86%	42.91%	44.01%	43.57%
Pulp and Paper	46.88%	46.71%	45.96%	44.41%	44.00%	43.96%
Oil and Gas	44.26%	44.56%	45.49%	44.22%	43.64%	43.81%
Chemicals	43.31%	44.41%	45.73%	45.71%	45.98%	46.01%
Steel Industry and Metallurgy	36.79%	37.52%	39.28%	40.87%	41.93%	43.11%
Telecommunications	37.61%	37.20%	40.00%	41.27%	40.96%	40.82%
Textiles	38.86%	39.34%	40.20%	40.70%	41.25%	42.29%
Vehicles, Parts and Accessories	46.58%	47.08%	48.84%	47.52%	44.41%	45.64%

Imperfectly diversified investors

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fishery	16.60%	14.21%	13.41%	14.18%	14.70%	15.31%
Food and Beverages	19.12%	16.78%	16.63%	17.04%	15.92%	15.81%
Construction	20.99%	18.73%	17.84%	15.13%	14.68%	13.91%
Electric Energy	17.11%	15.00%	15.72%	20.94%	21.58%	21.31%
Finance and Insurance	23.31%	18.83%	17.67%	20.93%	21.90%	21.55%
Industrial Machinery	18.87%	16.90%	19.31%	19.46%	21.05%	20.88%
Non-metallic Minerals	17.09%	15.60%	14.71%	19.04%	20.25%	17.75%
Others	22.17%	21.14%	18.47%	19.31%	19.35%	18.88%
Pulp and Paper	23.59%	21.47%	20.37%	18.34%	19.26%	17.75%
Oil and Gas	15.61%	13.15%	12.99%	16.44%	18.22%	17.92%
Chemicals	16.40%	13.92%	13.43%	14.33%	15.04%	16.12%
Steel Industry and Metallurgy	21.93%	19.38%	18.76%	19.37%	19.52%	18.75%
Telecommunications	17.99%	16.47%	17.17%	19.06%	20.22%	20.34%
Textiles	23.86%	22.78%	22.21%	23.60%	24.87%	26.34%
Vehicles, Parts and Accessories	25.19%	21.32%	19.69%	20.32%	17.76%	16.59%

Table A2.
Estimated costs of capital for Brazil Period: 1995-2005

Totally integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	6.12%	5.87%	4.95%	5.34%	5.49%	5.79%
Commerce	7.09%	6.90%	5.78%	6.11%	6.06%	6.19%
Construction	5.51%	5.65%	4.62%	4.96%	5.17%	5.34%
Electronics	5.82%	5.81%	4.72%	4.97%	5.36%	5.45%
Electric Energy	7.09%	6.81%	5.66%	5.89%	5.91%	6.07%
Finance and Insurance	6.90%	6.63%	5.57%	5.98%	6.04%	6.25%
Industrial Machinery	5.78%	5.60%	4.61%	5.04%	5.28%	5.35%
Non-metallic Minerals	6.11%	5.75%	4.84%	5.40%	5.33%	5.52%
Mining	6.59%	6.29%	5.16%	5.34%	5.31%	5.55%
Others	6.51%	6.14%	5.24%	5.74%	6.07%	6.26%
Pulp and Paper	6.25%	6.12%	5.10%	5.35%	5.45%	5.62%
Oil and Gas	6.57%	6.40%	5.32%	5.70%	5.88%	6.07%
Chemicals	6.27%	6.02%	5.06%	5.42%	5.68%	5.78%
Steel Industry and Metallurgy	6.34%	6.13%	5.26%	5.64%	5.94%	6.01%
Telecommunications	7.03%	6.86%	5.99%	6.28%	6.28%	6.46%
Textiles	6.12%	6.08%	5.02%	5.34%	5.34%	5.51%
Transport	6.34%	5.80%	5.01%	5.31%	5.92%	6.50%
Vehicles, Parts and Accessories	5.74%	5.71%	4.92%	5.16%	5.55%	5.70%

Partially integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	11.00%	10.43%	9.81%	10.59%	11.07%	11.67%
Commerce	13.98%	13.61%	12.24%	12.93%	12.65%	12.74%
Construction	9.34%	10.11%	8.99%	9.41%	10.13%	10.29%
Electronics	10.66%	11.03%	9.73%	9.45%	10.59%	10.48%
Electric Energy	13.64%	12.81%	11.25%	11.79%	11.96%	12.36%
Finance and Insurance	12.99%	12.37%	11.28%	12.20%	12.32%	12.82%
Industrial Machinery	9.37%	9.15%	8.43%	9.40%	10.11%	10.47%
Non-metallic Minerals	10.78%	9.90%	9.32%	10.71%	10.34%	10.77%
Mining	12.78%	12.06%	10.60%	10.80%	10.99%	11.09%
Others	11.76%	10.97%	10.47%	11.67%	12.68%	13.03%
Pulp and Paper	11.78%	11.60%	10.60%	10.90%	11.56%	11.08%
Oil and Gas	12.25%	12.02%	10.82%	11.53%	12.15%	12.51%
Chemicals	11.43%	10.94%	10.07%	10.93%	11.94%	11.72%
Steel Industry and Metallurgy	11.34%	11.04%	10.55%	11.42%	12.40%	12.45%
Telecommunications	13.15%	13.34%	12.95%	13.55%	13.76%	13.96%
Textiles	11.12%	11.18%	10.12%	10.70%	10.73%	10.83%
Transport	11.98%	10.02%	9.87%	10.53%	12.21%	13.74%
Vehicles, Parts and Accessories	9.41%	9.69%	9.49%	9.86%	11.07%	11.52%

(continues) →

Totally segmented market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	4.23%	4.37%	4.88%	5.41%	6.27%	6.51%
Commerce	7.78%	8.03%	8.57%	8.80%	9.05%	8.56%
Construction	3.90%	4.60%	4.81%	4.55%	4.97%	4.20%
Electronics	4.93%	5.33%	5.57%	4.71%	5.85%	4.69%
Electric Energy	8.80%	9.21%	9.21%	8.37%	8.41%	7.57%
Finance and Insurance	7.90%	7.82%	7.96%	8.40%	8.75%	8.21%
Industrial Machinery	5.07%	4.88%	5.00%	5.47%	6.13%	4.89%
Non-metallic Minerals	4.28%	4.02%	4.46%	5.85%	6.37%	5.96%
Mining	5.14%	5.20%	5.25%	5.09%	5.08%	5.59%
Others	6.46%	5.94%	6.42%	7.11%	7.98%	8.15%
Pulp and Paper	3.66%	3.95%	4.26%	4.49%	4.45%	5.52%
Oil and Gas	7.09%	7.02%	6.89%	7.13%	7.69%	7.19%
Chemicals	6.14%	6.03%	6.32%	6.44%	7.14%	6.30%
Steel Industry and Metallurgy	6.01%	5.91%	6.62%	6.99%	8.01%	7.33%
Telecommunications	8.57%	9.20%	9.64%	9.18%	8.80%	8.37%
Textiles	5.49%	5.53%	5.57%	6.03%	6.06%	5.81%
Transport	4.19%	3.76%	4.82%	5.14%	6.29%	7.59%
Vehicles, Parts and Accessories	5.27%	5.21%	5.64%	5.30%	6.53%	5.78%

Imperfectly diversified investors

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	11.03%	10.46%	9.14%	9.18%	9.24%	9.25%
Commerce	11.95%	11.26%	9.88%	9.79%	9.88%	9.83%
Construction	12.03%	10.73%	9.05%	9.32%	9.95%	10.13%
Electronics	12.35%	10.91%	9.21%	8.86%	8.92%	8.75%
Electric Energy	12.57%	11.92%	10.18%	10.08%	10.04%	9.89%
Finance and Insurance	11.86%	10.94%	9.40%	9.64%	9.76%	9.53%
Industrial Machinery	11.25%	10.39%	8.97%	8.90%	8.96%	8.43%
Non-metallic Minerals	9.97%	9.38%	8.19%	8.53%	8.63%	8.60%
Mining	10.70%	9.93%	8.47%	8.25%	8.07%	8.39%
Others	12.21%	11.77%	10.12%	10.34%	10.52%	10.36%
Pulp and Paper	11.10%	10.46%	8.96%	8.91%	8.60%	8.68%
Oil and Gas	11.34%	10.48%	9.11%	9.32%	9.48%	9.47%
Chemicals	11.37%	10.54%	9.08%	9.12%	9.36%	9.22%
Steel Industry and Metallurgy	11.69%	10.84%	9.36%	9.36%	9.48%	9.26%
Telecommunications	11.79%	11.22%	9.75%	9.93%	9.96%	9.98%
Textiles	11.44%	10.38%	8.89%	8.91%	8.84%	8.54%
Transport	12.33%	11.88%	10.40%	10.35%	10.79%	10.44%
Vehicles, Parts and Accessories	13.59%	12.10%	10.15%	9.99%	9.78%	9.56%

Table A3.

*Estimated costs of capital for Colombia Period: 1995-2005**Totally integrated market*

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	6.09%	5.83%	4.78%	5.00%	4.86%	5.07%
Commerce	5.99%	5.56%	4.38%	4.68%	4.48%	4.72%
Electric Energy					4.71%	5.21%
Finance and Insurance	5.86%	5.60%	4.48%	4.72%	4.76%	5.03%
Non-metallic Minerals	5.87%	5.55%	4.54%	4.79%	4.88%	5.16%
Mining	5.32%	4.22%	4.11%	4.31%	4.49%	5.22%
Others			3.82%	4.32%	4.49%	4.87%
Textiles	5.36%	5.02%	3.95%	4.46%	4.26%	5.07%

Partially integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	9.83%	9.31%	7.49%	8.99%	8.20%	7.56%
Commerce	11.50%	9.42%	6.27%	8.39%	7.20%	5.90%
Electric Energy					7.92%	7.62%
Finance and Insurance	9.73%	9.07%	6.76%	8.25%	8.39%	7.26%
Non-metallic Minerals	9.13%	7.94%	5.86%	7.59%	8.34%	7.34%
Mining	7.04%	6.47%	6.39%	6.33%	6.89%	8.16%
Others			2.58%	6.54%	9.60%	8.46%
Textiles	6.86%	5.86%	2.92%	8.66%	8.79%	8.93%

Totally segmented market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	2.24%	0.97%	-1.72%	-1.24%	-0.45%	-0.46%
Commerce	4.41%	3.54%	1.30%	1.58%	2.98%	2.66%
Electric Energy					3.32%	-0.33%
Finance and Insurance	5.79%	4.10%	1.24%	1.02%	1.65%	0.16%
Non-metallic Minerals	2.78%	1.10%	-2.01%	-1.82%	-1.97%	-2.31%
Mining	22.29%	33.05%	17.23%	3.21%	1.74%	-0.21%
Others			2.39%	2.14%	-0.76%	2.78%
Textiles	7.67%	7.42%	2.78%	2.77%	-1.12%	-0.58%

Imperfectly diversified investors

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Food and Beverages	9.31%	8.82%	7.49%	7.52%	7.33%	7.17%
Commerce	9.28%	8.57%	7.11%	7.21%	6.91%	7.12%
Electric Energy					6.76%	7.36%
Finance and Insurance	9.36%	9.14%	7.84%	7.88%	7.66%	7.89%
Non-metallic Minerals	9.32%	8.86%	7.56%	7.62%	7.48%	7.43%
Mining	12.19%	11.28%	9.84%	8.08%	7.08%	8.58%
Others			8.47%	8.31%	7.76%	7.15%
Textiles	10.33%	9.10%	8.03%	7.59%	8.02%	8.11%

Table A4.

*Estimated costs of capital for Chile Period: 1995-2005**Totally integrated market*

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	6.58%	6.03%	5.19%	5.39%	6.76%	6.55%
Food and Beverages	18.07%	0.50%	8.31%	23.30%	23.37%	5.58%
Commerce	43.72%	-8.24%	15.32%	40.85%	41.51%	4.87%
Construction	7.35%	6.87%	5.72%	5.72%	6.43%	6.70%
Electric Energy	6.60%	5.98%	4.98%	5.25%	6.05%	6.55%
Finance and Insurance	6.34%	5.92%	4.91%	5.09%	5.82%	6.33%
Funds	6.63%	6.06%	4.75%	5.13%	5.49%	6.08%
Non-metallic Minerals	5.97%	5.52%	4.58%	4.83%	5.94%	6.48%
Others	27.11%	-3.81%	13.22%	28.88%	31.01%	4.74%
Pulp and Paper	6.38%	5.84%	4.84%	5.00%	5.74%	6.07%
Oil and Gas	6.19%	5.81%	4.90%	5.13%	6.38%	6.71%
Chemicals	6.32%	5.93%	4.74%	4.89%	5.08%	5.65%
Steel Industry and Metallurgy	6.73%	6.29%	5.28%	5.36%	6.48%	6.76%
Telecommunications	6.96%	6.61%	5.58%	5.75%	7.24%	7.41%
Transport	37.94%	-8.47%	26.98%	30.82%	32.09%	5.10%

Partially integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	7.83%	6.93%	6.28%	6.51%	6.60%	6.27%
Food and Beverages	7.75%	7.09%	6.11%	6.46%	6.14%	6.47%
Commerce	7.94%	6.95%	6.06%	6.32%	6.40%	6.71%
Construction	8.73%	8.14%	7.16%	7.25%	6.41%	6.56%
Electric Energy	7.62%	6.80%	5.90%	6.17%	6.06%	6.53%
Finance and Insurance	7.21%	6.73%	5.75%	6.00%	5.97%	6.54%
Funds	7.61%	6.81%	5.47%	6.04%	5.82%	6.30%
Non-metallic Minerals	6.65%	5.95%	5.22%	5.63%	5.97%	6.37%
Others	6.76%	6.22%	5.38%	5.63%	5.71%	6.18%
Pulp and Paper	7.34%	6.60%	5.69%	5.96%	5.93%	6.24%
Oil and Gas	7.12%	6.58%	5.81%	6.04%	6.13%	6.54%
Chemicals	7.55%	6.87%	5.68%	5.90%	5.14%	5.26%
Steel Industry and Metallurgy	8.24%	7.47%	6.56%	6.57%	7.01%	7.22%
Telecommunications	8.21%	7.73%	6.84%	7.08%	7.04%	7.10%
Transport	7.23%	6.63%	5.85%	6.28%	6.54%	7.13%

(continues) →

Totally segmented market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	-29.30%	8.93%	11.44%	-55.81%	18.22%	13.67%
Food and Beverages	-23.06%	8.98%	10.65%	-27.73%	-2.41%	28.15%
Commerce	-9.97%	8.90%	10.45%	9.08%	-29.02%	51.45%
Construction	-28.90%	10.34%	12.36%	-55.54%	16.34%	12.15%
Electric Energy	-29.85%	8.25%	10.03%	-56.59%	16.20%	12.52%
Finance and Insurance	-29.98%	8.34%	10.15%	-56.54%	15.82%	11.89%
Funds	-29.97%	8.13%	9.57%	-56.64%	15.44%	11.85%
Non-metallic Minerals	-30.55%	7.56%	9.50%	-56.79%	16.25%	12.40%
Others	-18.99%	7.63%	9.13%	-8.81%	-18.73%	40.41%
Pulp and Paper	-29.37%	9.19%	10.87%	-56.23%	16.76%	12.58%
Oil and Gas	-29.64%	8.77%	10.57%	-56.30%	16.73%	12.75%
Chemicals	-29.60%	8.95%	11.03%	-56.14%	17.18%	11.55%
Steel Industry and Metallurgy	-29.04%	9.79%	11.49%	-56.09%	18.52%	14.50%
Telecommunications	-29.24%	9.25%	11.18%	-55.98%	17.99%	13.38%
Transport	-11.15%	8.90%	10.79%	17.11%	-40.11%	48.46%

Imperfectly diversified investors

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	8.09%	7.65%	6.67%	6.75%	6.60%	7.29%
Food and Beverages	8.32%	7.72%	6.50%	6.45%	6.17%	6.42%
Commerce	8.79%	7.85%	6.50%	6.48%	6.23%	6.56%
Construction	9.30%	8.61%	7.25%	7.23%	6.39%	6.61%
Electric Energy	8.34%	7.73%	6.49%	6.61%	6.52%	6.83%
Finance and Insurance	8.04%	7.49%	6.25%	6.32%	6.08%	6.28%
Funds	9.04%	8.23%	6.63%	6.44%	6.23%	6.55%
Non-metallic Minerals	8.08%	7.61%	6.40%	6.30%	6.24%	6.44%
Others	8.25%	7.78%	6.46%	6.43%	6.35%	6.57%
Pulp and Paper	8.14%	7.60%	6.32%	6.34%	5.96%	6.19%
Oil and Gas	7.93%	7.32%	6.15%	6.27%	6.04%	6.33%
Chemicals	8.15%	7.55%	6.34%	6.49%	5.97%	5.90%
Steel Industry and Metallurgy	8.65%	8.15%	6.79%	6.85%	6.87%	7.29%
Telecommunications	8.66%	7.88%	6.61%	6.66%	6.47%	6.64%
Transport	8.68%	8.06%	6.75%	6.63%	6.34%	6.55%

Table A5.

*Estimated costs of capital for Mexico Period: 1995-2005**Totally integrated market*

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	6.34%	5.88%	4.58%	4.73	4.52%	4.82%
Food and Beverages	6.43%	6.25%	5.09%	5.18%	5.06%	5.38%
Commerce	6.99%	6.95%	5.82%	5.80%	5.83%	5.96%
Construction	7.04%	6.72%	5.44%	5.67%	5.29%	5.95%
Finance and Insurance	7.36%	7.06%	5.96%	5.98%	5.63%	5.73%
Industrial Machinery	7.04%	6.77%	5.55%	5.50%	5.08%	5.35%
Non-metallic Minerals	7.13%	6.43%	5.22%	5.33%	4.87%	5.13%
Mining	6.03%	5.87%	4.69%	4.87%	4.86%	5.53%
Others	7.77%	7.38%	6.17%	6.33%	6.09%	6.22%
Pulp and Paper	6.44%	6.27%	4.97%	5.13%	4.96%	5.16%
Chemicals	6.22%	6.00%	4.70%	4.74%	4.58%	4.90%
Steel Industry and Metallurgy	7.28%	6.94%	5.64%	5.71%	5.49%	5.72%
Telecommunications	6.91%	6.61%	5.61%	5.75%	5.86%	6.14%
Transport	6.19%	5.64%	4.51%	5.06%	4.95%	5.27%

Partially integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	14.31%	11.93%	8.60%	8.01%	7.53%	7.74%
Food and Beverages	13.34%	12.87%	10.88%	10.02%	9.47%	10.09%
Commerce	17.29%	18.31%	15.70%	13.89%	13.75%	13.49%
Construction	17.00%	15.62%	12.39%	12.17%	9.85%	13.27%
Finance and Insurance	19.51%	17.80%	15.90%	14.20%	12.19%	11.68%
Industrial Machinery	18.02%	16.66%	13.45%	11.35%	9.49%	9.88%
Non-metallic Minerals	16.93%	13.57%	11.18%	10.33%	8.51%	9.03%
Mining	11.67%	11.17%	9.01%	8.70%	8.36%	10.87%
Others	22.60%	20.44%	17.68%	16.81%	15.10%	14.66%
Pulp and Paper	13.57%	13.49%	10.30%	10.41%	9.37%	9.28%
Chemicals	11.48%	11.16%	8.32%	7.01%	7.27%	8.22%
Steel Industry and Metallurgy	18.88%	17.35%	12.93%	12.55%	12.33%	12.19%
Telecommunications	16.76%	15.68%	14.67%	13.83%	13.74%	14.10%
Transport	12.72%	10.37%	8.35%	9.30%	8.92%	9.99%

(continues) →

Totally segmented market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	11.79%	10.18%	4.25%	6.19%	3.96%	7.84%
Food and Beverages	12.16%	9.69%	3.48%	5.42%	2.04%	4.38%
Commerce	9.74%	7.07%	0.09%	2.13%	-0.99%	2.45%
Construction	9.38%	7.61%	0.79%	1.96%	-1.16%	1.26%
Finance and Insurance	8.46%	6.52%	-0.14%	1.74%	-0.27%	3.01%
Industrial Machinery	10.08%	7.64%	0.92%	3.08%	1.09%	3.56%
Non-metallic Minerals	8.86%	8.47%	2.15%	4.05%	2.65%	5.73%
Mining	13.57%	10.86%	4.24%	5.86%	2.80%	3.92%
Others	7.40%	5.04%	-1.12%	0.11%	-2.58%	0.69%
Pulp and Paper	11.17%	8.99%	2.86%	4.98%	2.42%	6.11%
Chemicals	10.69%	8.74%	3.12%	5.39%	3.31%	8.42%
Steel Industry and Metallurgy	8.30%	6.33%	0.29%	2.03%	0.15%	3.59%
Telecommunications	10.55%	8.03%	1.04%	2.41%	-1.79%	0.50%
Transport	12.75%	11.57%	4.92%	5.48%	2.52%	5.07%

Imperfectly diversified investors

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries	9.56%	8.67%	7.11%	7.02%	6.87%	6.74%
Food and Beverages	9.84%	9.14%	7.45%	7.41%	6.81%	7.00%
Commerce	10.29%	9.85%	7.91%	7.81%	7.73%	7.75%
Construction	10.36%	9.81%	8.53%	8.57%	8.58%	7.97%
Finance and Insurance	10.01%	9.22%	7.92%	7.80%	7.19%	6.99%
Industrial Machinery	9.23%	8.72%	7.72%	7.65%	7.45%	7.67%
Non-metallic Minerals	10.60%	9.35%	7.78%	7.65%	7.04%	6.81%
Mining	8.75%	8.71%	7.52%	7.74%	8.12%	8.11%
Others	10.89%	9.85%	8.23%	8.14%	7.62%	7.77%
Pulp and Paper	9.35%	8.67%	7.08%	6.83%	6.73%	6.67%
Chemicals	9.43%	8.60%	7.29%	7.30%	7.25%	6.79%
Steel Industry and Metallurgy	10.50%	9.66%	8.21%	8.14%	7.72%	8.07%
Telecommunications	9.49%	8.75%	7.45%	7.70%	7.39%	7.56%
Transport	9.28%	8.38%	7.20%	7.71%	7.99%	8.30%

Table A6.

*Estimated costs of capital for Peru Period: 1995-2005**Totally integrated market*

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries		5.74%	3.98%	4.36%	5.47%	5.00%
Food and Beverages	5.81%	5.68%	4.58%	4.79%	5.41%	5.60%
Construction	6.31%	6.29%	4.95%	5.20%	7.02%	6.29%
Electric Energy	5.70%	5.50%	4.44%	4.66%	4.62%	4.77%
Finance and Insurance	6.01%	5.90%	4.75%	4.93%	5.79%	5.62%
Non-metallic Minerals	5.99%	5.73%	4.58%	4.77%	5.31%	4.99%
Mining	6.50%	6.24%	4.88%	5.04%	6.12%	6.29%
Others	6.11%	6.05%	4.86%	5.17%	6.71%	6.28%
Chemicals	6.15%	5.93%	4.87%	5.00%	4.83%	4.93%
Steel Industry and Metallurgy	6.79%	6.37%	5.08%	5.17%	4.80%	4.85%
Telecommunications	6.74%	6.42%	5.39%	5.51%	6.95%	6.50%

Partially integrated market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries		9.71%	5.40%	5.97%	6.60%	6.48%
Food and Beverages	8.30%	8.30%	7.02%	7.28%	7.09%	7.67%
Construction	9.90%	10.74%	7.79%	8.08%	7.80%	9.03%
Electric Energy	7.84%	7.74%	6.49%	6.65%	6.50%	6.74%
Finance and Insurance	8.78%	8.88%	7.19%	7.27%	6.87%	6.80%
Non-metallic Minerals	8.42%	7.96%	6.28%	6.19%	5.28%	5.71%
Mining	10.16%	9.74%	6.66%	6.90%	6.97%	7.47%
Others	8.74%	8.92%	7.10%	7.77%	7.25%	7.55%
Chemicals	9.23%	9.06%	7.80%	7.65%	6.20%	6.48%
Steel Industry and Metallurgy	11.10%	10.08%	7.72%	7.19%	5.64%	6.45%
Telecommunications	10.96%	9.90%	9.32%	9.85%	9.99%	10.25%

Totally segmented market

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries		6.52%	5.09%	3.75%	3.50%	4.22%
Food and Beverages	12.50%	6.00%	2.92%	1.82%	2.44%	2.84%
Construction	11.16%	5.07%	2.02%	1.13%	1.56%	2.55%
Electric Energy	12.93%	6.67%	3.57%	2.53%	4.10%	4.28%
Finance and Insurance	11.88%	5.36%	2.45%	1.83%	3.30%	3.51%
Non-metallic Minerals	11.32%	5.09%	2.14%	1.45%	3.06%	3.82%
Mining	10.34%	4.10%	0.95%	0.44%	1.72%	1.89%
Others	10.86%	4.42%	1.41%	0.74%	1.85%	2.39%
Chemicals	11.35%	5.34%	2.19%	1.97%	3.75%	4.27%
Steel Industry and Metallurgy	9.70%	3.77%	0.97%	0.37%	2.55%	3.44%
Telecommunications	10.42%	3.81%	1.19%	1.45%	1.66%	2.51%

(continues) →

Imperfectly diversified investors

Sector	95-00	96-01	97-02	98-03	99-04	00-05
Agriculture and Fisheries		10.51%	8.06%	7.67%	7.64%	7.11%
Food and Beverages	9.79%	8.89%	7.27%	7.34%	7.12%	6.96%
Construction	9.81%	9.22%	7.60%	7.36%	7.37%	7.50%
Electric Energy	7.73%	7.10%	5.79%	5.83%	5.52%	5.79%
Finance and Insurance	8.99%	8.70%	7.53%	7.36%	7.22%	7.20%
Non-metallic Minerals	8.13%	7.55%	6.30%	6.30%	5.79%	5.97%
Mining	9.99%	9.15%	8.37%	8.18%	7.69%	8.00%
Others	8.65%	8.20%	6.76%	6.67%	6.00%	6.30%
Chemicals	10.28%	8.13%	6.94%	6.75%	6.72%	6.88%
Steel Industry and Metallurgy	10.35%	9.49%	7.74%	7.54%	6.46%	6.12%
Telecommunications	8.63%	8.71%	7.44%	7.00%	6.99%	7.26%

Table A7.

*Statistical significance of estimated securities' betas in Argentina at 95% level of confidence.**(Period: 1995-2005)**Totally segmented market*

Local CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.848	0.790	0.664	0.659	0.636	0.620	0.703
Probability	0.030	0.060	0.021	0.016	0.042	0.036	0.027
Significant Proportion	92%	90%	93%	87%	72%	83%	86%
R2	42%	39%	37%	28%	25%	25%	33%
Number Observations	50	56	54	52	53	60	54

Totally integrated market

Global CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.513	1.249	1.082	0.788	0.718	0.818	1.028
Probability	0.059	0.046	0.074	0.236	0.288	0.237	0.157
Significant Proportion	82%	80%	69%	43%	28%	33%	56%
R2	20%	18%	15%	7%	6%	6%	12%
Number Observations	55	56	54	52	53	60	55

Partially integrated market

D-CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.855	0.798	0.722	0.673	0.632	0.631	0.718
Probability	0.021	0.024	0.054	0.041	0.069	0.053	0.044
Significant Proportion	89%	90%	90%	87%	82%	81%	87%
R2	55%	47%	41%	30%	25%	26%	37%
Number Observations	55	56	54	52	53	60	55
Goldman Sachs	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.285	1.050	0.909	0.746	0.676	0.777	0.907
Probability	0.075	0.064	0.109	0.226	0.290	0.243	0.168
Significant Proportion	74%	78%	69%	45%	28%	35%	55%
R2	17%	0%	13%	7%	6%	6%	8%
Number Observations	55	56	54	52	53	60	55

Imperfectly diversified investors

Estrada	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.461	2.916	2.793	3.235	3.344	3.205	3.159
Standard Deviation	1.054	0.994	0.939	1.026	1.068	1.009	1.015
t – statistic	3.28	2.93	2.97	3.15	3.13	3.18	3.11
Godfrey and Espinosa	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.755	2.928	2.736	3.327	3.614	3.687	3.341
Standard Deviation	1.539	1.192	0.866	0.952	0.991	0.999	1.090
t - statistic	2.44	2.46	3.16	3.49	3.65	3.69	3.07

Table A8.

*Statistical significance of estimated securities' betas in Brazil at 95% level of confidence.**(Period: 1995-2005)**Totally segmented market*

Local CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.772	0.811	0.861	0.847	0.929	0.868	0.848
Probability	0.052	0.049	0.036	0.030	0.016	0.016	0.033
Significant Proportion	85%	87%	90%	92%	94%	95%	90%
R2	36%	37%	39%	45%	48%	42%	41%
Number Observations	49	53	54	56	57	60	55

Totally integrated market

Global CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.393	1.408	1.476	1.611	1.817	1.780	1.581
Probability	0.155	0.134	0.105	0.063	0.033	0.025	0.086
Significant Proportion	64%	66%	74%	80%	91%	93%	78%
R2	12%	14%	17%	21%	24%	26%	19%
Number Observations	55	56	54	52	53	60	55

Partially integrated market

D-CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.635	0.671	0.722	0.748	0.872	0.793	0.740
Probability	0.095	0.084	0.067	0.044	0.025	0.017	0.055
Significant Proportion	80%	83%	106%	92%	94%	94%	91%
R2	35%	36%	36%	43%	49%	44%	41%
Number Observations	55	56	54	52	53	60	55
Goldman Sachs	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.004	0.999	1.114	1.279	1.530	1.574	1.253
Probability	0.220	0.197	0.153	0.090	0.046	0.034	0.123
Significant Proportion	45%	47%	63%	76%	88%	87%	68%
R2	8%	9%	12%	16%	19%	22%	14%
Number Observations	54	53	54	56	57	60	56

Imperfectly diversified investors

Estrada	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	4.827	4.167	3.678	3.440	3.487	3.021	3.770
Standard Deviation	1.781	1.492	1.234	1.090	1.103	0.977	1.280
t – statistic	2.71	2.79	2.98	3.15	3.16	3.09	2.95
Godfrey and Espinosa	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	4.765	4.213	3.794	3.614	3.795	3.564	3.958
Standard Deviation	1.594	1.357	1.108	1.021	1.066	1.151	1.216
t – statistic	2.99	3.10	3.42	3.54	3.56	3.10	3.25

Table A9.

*Statistical significance of estimated securities' betas in Colombia at 95% level of confidence.**(Period: 1995-2005)**Totally segmented market*

Local CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.786	0.666	0.806	0.830	0.800	0.751	0.773
Probability	0.049	0.080	0.098	0.066	0.048	0.061	0.067
Significant Proportion	79%	87%	69%	75%	75%	77%	77%
R2	42%	42%	39%	40%	37%	34%	39%
Number Observations	48	49	49	51	47	54	49

Totally integrated market

Global CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.588	0.332	0.225	0.358	0.414	0.562	0.413
Probability	0.334	0.427	0.445	0.521	0.390	0.286	0.400
Significant Proportion	14%	7%	6%	13%	5%	27%	12%
R2	4%	2%	2%	2%	3%	5%	3%
Number Observations	48	49	49	51	47	54	49

Partially integrated market

D-CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.652	0.537	0.628	0.602	0.607	0.738	0.627
Probability	0.145	0.097	0.178	0.204	0.112	0.101	0.140
Significant Proportion	79%	80%	69%	69%	70%	77%	74%
R2	34%	34%	31%	31%	37%	36%	34%
Number Observations	48	49	49	51	47	54	49
Goldman Sachs	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.312	0.203	0.186	0.289	0.381	0.463	0.307
Probability	0.369	0.482	0.476	0.534	0.431	0.351	0.440
Significant Proportion	14%	7%	13%	13%	5%	27%	13%
R2	3%	2%	2%	2%	3%	4%	3%
Number Observations	48	49	49	51	47	54	49

Imperfectly diversified investors

Estrada	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.985	3.596	3.082	2.700	2.360	2.168	2.983
Standard Deviation	1.480	1.182	0.839	0.702	0.787	0.778	0.961
t – statistic	2.69	3.04	3.69	3.85	3.00	2.79	3.10
Godfrey and Espinosa	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.957	3.414	3.151	2.973	2.810	3.093	3.233
Standard Deviation	1.286	0.989	0.786	0.790	0.871	1.562	1.047
t – statistic	3.08	3.45	4.01	3.76	3.23	1.98	3.09

Table A10.

*Statistical significance of estimated securities' betas in Chile at 95% level of confidence.**(Period: 1995-2005)**Totally segmented market*

Local CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.860	0.844	0.847	0.847	0.884	0.909	0.865
Probability	0.028	0.034	0.026	0.009	0.020	0.011	0.021
Significant Proportion	95%	95%	93%	97%	95%	93%	95%
R2	38%	37%	39%	40%	35%	36%	38%
Number Observations	56	58	58	59	58	60	58

Totally integrated market

Global CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.992	0.744	0.764	0.792	0.789	0.864	0.824
Probability	0.080	0.118	0.081	0.058	0.056	0.060	0.075
Significant Proportion	70%	64%	71%	73%	83%	87%	75%
R2	14%	11%	13%	15%	16%	18%	15%
Number Observations	56	58	58	59	58	60	58

Partially integrated market

D-CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.079	0.777	0.767	0.744	0.602	0.684	0.776
Probability	0.097	0.143	0.112	0.082	0.085	0.055	0.096
Significant Proportion	77%	62%	73%	73%	105%	102%	82%
R2	18%	12%	14%	16%	15%	15%	15%
Number Observations	56	58	58	59	58	58	58
Goldman Sachs	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.844	0.587	0.642	0.687	0.682	0.762	0.701
Probability	0.114	0.184	0.121	0.077	0.078	0.070	0.107
Significant Proportion	65%	55%	56%	71%	80%	84%	68%
R2	12%	9%	11%	13%	13%	16%	12%
Number Observations	56	58	58	59	58	60	69

Imperfectly diversified investors

Estrada	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	2.979	2.574	2.275	1.976	1.727	1.688	2.203
Standard Deviation	0.782	0.717	0.651	0.505	0.536	0.524	0.619
t – statistic	3.81	3.59	3.49	3.91	3.22	3.22	3.56
Godfrey and Espinosa	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	2.943	2.442	2.258	2.081	2.061	2.177	2.327
Standard Deviation	0.655	0.555	0.511	0.463	0.534	0.734	0.575
t - statistic	4.49	4.40	4.42	4.50	3.86	2.97	4.05

Table A11.

*Statistical significance of estimated securities' betas in Mexico at 95% level of confidence**(Period: 1995-2005)**Totally segmented market*

Local CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.938	0.876	0.862	0.859	0.883	0.861	0.880
Probability	0.031	0.052	0.051	0.074	0.068	0.058	0.056
Significant Proportion	93%	91%	91%	87%	76%	82%	87%
R2	46%	39%	39%	36%	31%	33%	37%
Number Observations	53	57	57	57	56	60	57

Totally integrated market

Global CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.888	1.690	1.445	1.224	1.082	1.142	1.412
Probability	0.042	0.057	0.069	0.094	0.088	0.042	0.065
Significant Proportion	86%	82%	76%	74%	73%	82%	79%
R2	24%	23%	22%	18%	19%	22%	21%
Number Observations	53	57	57	57	56	60	57

Partially integrated market

D-CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.917	0.893	0.903	0.920	0.862	0.905	0.900
Probability	0.019	0.040	0.048	0.064	0.110	0.037	0.053
Significant Proportion	95%	91%	89%	87%	78%	90%	88%
R2	53%	48%	48%	45%	31%	37%	44%
Number Observations	53	57	57	57	56	60	57
Goldman Sachs	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	1.626	1.483	1.288	1.081	0.958	1.045	1.247
Probability	0.059	0.072	0.083	0.113	0.095	0.067	0.081
Significant Proportion	81%	82%	76%	70%	67%	78%	76%
R2	22%	21%	21%	17%	17%	20%	20%
Number Observations	53	57	57	57	56	60	57

Imperfectly diversified investors

Estrada	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.999	3.462	3.050	2.767	2.467	2.233	2.996
Standard Deviation	1.080	0.847	0.767	0.757	0.850	0.739	0.840
t - statistic	3.70	4.09	3.98	3.65	2.90	3.02	3.57
Godfrey and Espinosa	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	4.376	3.783	3.294	3.103	2.928	2.609	3.349
Standard Deviation	2.179	1.938	1.560	1.482	1.287	1.038	1.581
t – statistic	2.01	1.95	2.11	2.09	2.27	2.51	2.12

Table A12.

*Statistical significance of estimated securities' betas in Peru at 95% level of confidence.**(Period: 1995-2005)**Totally segmented market*

Local CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.904	0.856	0.864	0.809	0.681	0.552	0.778
Probability	0.039	0.064	0.056	0.076	0.128	0.177	0.090
Significant Proportion	84%	86%	83%	79%	56%	60%	75%
R2	37%	32%	30%	27%	13%	11%	25%
Number Observations	48	54	53	55	56	60	54

Totally integrated market

Global CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.904	0.877	0.467	0.487	0.439	0.488	0.610
Probability	0.118	0.088	0.159	0.183	0.308	0.286	0.190
Significant Proportion	53%	62%	33%	38%	24%	32%	40%
R2	9%	9%	7%	7%	6%	6%	7%
Number Observations	53	54	53	55	56	60	55

Partially integrated market

D-CAPM	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.84	0.82	0.84	0.83	0.81	0.68	0.80
Probability	0.061	0.067	0.094	0.112	0.095	0.129	0.093
Significant Proportion	84%	90%	79%	71%	64%	68%	76%
R2	41%	36%	31%	30%	14%	12%	27%
Number Observations	53	54	53	55	56	60	55
Goldman Sachs	95-00	96-01	97-02	98-03	99-04	00-05	Average
Beta	0.672	0.722	0.384	0.407	0.362	0.398	0.491
Probability	0.216	0.145	0.182	0.209	0.325	0.306	0.230
Significant Proportion	32%	43%	29%	25%	24%	20%	29%
R2	7%	2%	6%	6%	5%	4%	5%
Number Observations	53	54	53	55	56	60	55

Imperfectly diversified investors

Estrada	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.494	3.133	3.046	2.678	2.461	2.341	2.859
Standard Deviation	0.978	0.870	1.435	1.327	1.429	1.293	1.222
t – statistic	3.57	3.60	2.12	2.02	1.72	1.81	2.34
Godfrey and Espinosa	95-00	96-01	97-02	98-03	99-04	00-05	Average
RVR	3.506	3.123	3.032	2.914	2.976	3.067	3.103
Standard Deviation	1.159	1.083	1.426	1.592	1.659	1.606	1.421
t – statistic	3.02	2.88	2.13	1.83	1.79	1.91	2.18

Table A13.
Required Returns (RR) for September 2005

Model estimated for all countries

Variable	Argentina	Brazil	Colombia	Chile	Mexico	Peru	Venezuela
CRR (Sept 2005)	26.4	48.2	46.2	71.60	63.0	45.5	38.8
LN (CRR)	3.27	3.88	3.83	4.27	4.14	3.82	3.66
Intercept	0.91	0.91	0.91	0.91	0.91	0.91	0.91
t – Statistic	-5.28	-5.28	-5.28	-5.28	-5.28	-5.28	-5.28
Slope	-0.22	-0.22	-0.22	-0.22	-0.22	-0.22	-0.22
t – Statistic	5.43	5.43	5.43	5.43	5.43	5.43	5.43
Risk-free rate (Annual)	3%	3%	3%	3%	3%	3%	3%
RR (Semi-annual)	20.48%	7.48%	8.40%	-1.06%	1.70%	8.73%	12.17%
RR (Annual)	43.96%	17.96%	19.79%	0.87%	6.40%	20.45	27.33%

Model estimated for emerging countries

Variable	Argentina	Brazil	Colombia	Chile	Mexico	Peru	Venezuela
CRR (Sept 2005)	26.4	48.2	46.2	71.60	63	45.5	38.8
LN (CRR)	3.27	3.88	3.83	4.27	4.14	3.82	3.66
Intercept	0.84	0.84	0.84	0.84	0.84	0.84	0.84
t – Statistic	-3.27	-3.27	-3.27	-3.27	-3.27	-3.27	-3.27
Slope	-0.21	-0.21	-0.21	-0.21	-0.21	-0.21	-0.21
t – Statistic	4.12	4.12	4.12	4.12	4.12	4.12	4.12
Risk-free Rate (Annual)	3%	3%	3%	3%	3%	3%	3%
RR (Semi-annual)	14.32%	1.41%	2.32%	-7.07%	-4.33%	2.65%	6.06%
RR (Annual)	31.64%	5.82%	7.64%	-11.5%	-5.66%	8.29%	15.12%

Model estimated for developed countries

Variable	Argentina	Brazil	Colombia	Chile	Mexico	Peru	Venezuela
CRR (Sept 2005)	26.4	48.2	46.2	71.60	63.0	45.5	38.8
LN (CRR)	3.27	3.88	3.83	4.27	4.14	3.82	3.66
Intercept	1.04	1.04	1.04	1.04	1.04	1.04	1.04
t – Statistic	-2.57	-2.57	-2.57	-2.57	-2.57	-2.57	-2.57
Slope	-0.23	-0.23	-0.23	-0.23	-0.23	-0.23	-0.23
t – Statistic	2.62	2.62	2.62	2.62	2.62	2.62	2.62
Risk-Free Rate (Annual)	3%	3%	3%	3%	3%	3%	3%
RR (Semi-annual)	28.34%	14.43%	15.41%	5.30%	8.25%	15.77%	19.44%
RR (Annual)	59.67%	31.87%	33.83%	13.59%	19.50%	34.53%	41.89%

