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Traffic Accidents Forecasting using Singular Value Decomposition and an Autoregressive Neural Network Based on PSO

Lida Barba and Nibaldo Rodríguez

Abstract—In this paper, we propose a strategy to improve the forecasting of traffic accidents in Concepción, Chile. The forecasting strategy consists of four stages: embedding, decomposition, estimation and recomposition. At the first stage, the Hankel matrix is used to embed the original time series. At the second stage, the Singular Value Decomposition (SVD) technique is applied. SVD extracts the singular values and the singular vectors, which are used to obtain the components of low and high frequency. At the third stage, the estimation is implemented with an Autoregressive Neural Network (ANN) based on Particle Swarm Optimization (PSO). The final stage is recomposition, where the forecasted value is obtained. The results are compared with the values given by the conventional forecasting process. Our strategy shows high accuracy and is superior to the conventional process.

Index Terms—Autoregressive neural network, particle swarm optimization, singular value decomposition.

I. INTRODUCTION

PORECASTING of time series with neural networks has been widely implemented due to its capability of approximation and universal generalization [1], [2] in diverse areas of knowledge [3], [4]. Conventionally, the neural networks show difference and improvement through the adequate selection of transfer and activation functions [5], [6], the variation in the input dimension and the time delay [7], also changing the number of hidden nodes [8], others researchers propose modifications in the learning algorithms [9], is common also the use of explanatory variables [10], there are works that implement hybrid solutions reaching good performance [11], [12], whereas the decomposition, disaggregation or aggregation of the time series before the forecasting have demonstrated to be an effective strategy [13], [14]. The combination ANN-PSO has improved the forecasting over some classical algorithms [15], [16], [17]

Based on these arguments, in this work we propose a strategy of improving traffic accidents forecasting based on

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the decomposition of a time series in components of low and high frequency from the singular values of the Hankel matrix. The strategy is applied in four stages, embedding with Hankel matrix, decomposing with SVD, estimation with ANN-PSO, and recomposing with simple addition. The time series are the traffic accidents of Concepción - Chile, sinister number and injured, from year 2000 to 2012, with weekly sampling.

The paper is structured as follows. Section II describes the time series forecasting strategy. Section III presents the forecasting accuracy metrics. Section IV presents the results and discussion. Section V gives conclusions.

II. TIME SERIES FORECASTING STRATEGY

Our forecasting strategy is presented in Figure 1. It consists of four stages: embedding, decomposition, estimation, and recomposition. Embedding means to map the time series in a Hankel matrix, decomposition is developed with SVD, the singular values are used to extract the components of low and high frequency, the estimation of the found components is based on an ANN based on PSO, and the recomposition is developed with the simple addition of the ANNs outputs.

The original time series is represented with x, H is the Hankel matrix, S, V, and U are the matrix elements obtained with SVD, C_L is the component of low frequency, C_H is the component of high frequency, $\hat{C_L}$, and $\hat{C_H}$ are the estimated components, \hat{x} is the forecasted time series, and er is the error computed between x and \hat{x} .

A. Embedding the time series

The time series is embedded in the Hankel matrix, the process is illustrated as follows:

$$H_{M \times L} = \begin{bmatrix} x_1 & x_2 & \dots & x_L \\ x_2 & x_3 & \dots & x_{L+1} \\ \vdots & \vdots & \vdots & \vdots \\ x_M & x_{M+1} & \dots & x_N \end{bmatrix}$$
(1)

where H is a matrix of order $M \times L$, $x_1 \dots x_N$, are the original values of the time series, of length N. The value of L is computed as

$$L = N - M + 1. \tag{2}$$

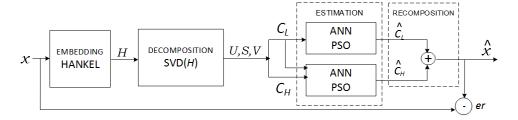


Fig. 1. Time series forecasting strategy

B. Singular Value Decomposition

Let H be an $M \times n$ real matrix, then there exist an $M \times M$ orthogonal matrix U, an $n \times n$ orthogonal matrix V, and and $M \times n$ diagonal matrix S with diagonal entries $s_1 \ge s_2 \ge ... \ge$ s_p , with p = min(M, n), such that $U^T H V = S$. Moreover, the numbers s_1, s_2, \dots, s_p are uniquely determined by H [18].

$$H = U \times S \times V^T \tag{3}$$

The extraction of the components is done by means of the singular values s_i , the orthogonal matrix U, and the orthogonal matrix V, for each singular value is obtained one matrix A_i , with $i = 1 \dots m$:

$$A_i = s(i) \times U(:,i) \times V(:,i)^T \tag{4}$$

Therefore, the matrix A_i contains the i-th component, the extraction process is:

$$C_i = [A_i(1,:) \quad A_i(2,n:m)^T]$$
 (5)

where C_i is the i-th component, the elements of C_i are located in the first row and last column of A_i .

The optimal number of components (M) is given by the maximum peak of differential energy ΔE of each pair of sequential components, and it computation is

$$\Delta E_i = E_i - E_{i+1} \tag{6}$$

where E_i is the energy of the i-th component, and i= $1, \dots, M-1$. The energy of each singular is computed with

$$E_i = s_i^2 / (\sum_{i=1}^M s_i^2) \tag{7}$$

where s_i is the i-th singular value of the Hankel matrix obtained before. The first component extracted is the component C_L and the second is the component C_H (if M=2). When the optimal number of components M>2, the component C_H is computed with the summation of the components from 2 to M-th, as follows

$$C_H = \sum_{i=2}^{M} C_i \tag{8}$$

C. Estimation of components with an Autoregressive Neural Network based on PSO

The ANN is based on the algorithm PSO, it performs the estimation to obtain \hat{C}_L , and \hat{C}_H . The ANN inputs are the lagged terms of C_L and C_H . The ANN has a common structure of three layers [19], at the hidden layer the sigmoid transfer function is applied, and at the output layer the estimated value is obtained. The ANN output is

$$\hat{x} = \phi(net) \times b \tag{9}$$

where \hat{x} is the estimated value, *net* is the output of the hidden layer, b is the vector that contains the weights on the connections from the hidden layer to the output layer, net is computed with

$$net = x \times w \tag{10}$$

where x is the data input matrix, with order $N \times P$, N is the sample length, and P is the number of input variables (lags terms), w is the weight matrix of order $P \times N_h$, with N_h hidden units. The sigmoid transfer function is applied at hidden layer with

$$\phi(net) = 1/(1 + e^{-net}) \tag{11}$$

The weights of the ANN connections, w and b are adjusted with PSO learning algorithm. In the swarm the N_p particles has a position vector $X_i = (X_{i1}, X_{i2}, \dots, X_{iD})$, and a velocity vector $V_i = (V_{i1}, V_{i2}, \dots, V_{iD})$, each particle is considered a potential solution in a D-dimensional search space. During each iteration the particles are accelerated toward the previous best position denoted by p_{id} and toward the global best position denoted by p_{gd} . The swarm has $N_p xD$ values and is initialized randomly, D is computed with $P \times N_h + N_h$; the process finish when the lowest error is obtained based on the fitness function evaluation, or when the maximum number of iterations is reached [20], [21].

$$V_{id}^{l+1} = I^{l} \times V_{id}^{l} + c_{1} \times rd_{1}(p_{id}^{l} + X_{id}^{l}) + c_{2} \times rd_{2}(p_{gd}^{l} + X_{id}^{l})$$

$$I^{l+1} = X_{id}^{l} + V_{id}^{l+1}$$

$$I^{l} = I_{max}^{l} - \frac{I_{max}^{l} - I_{min}^{l}}{iter_{max}} \times l,$$

$$(14)$$

$$X_{id}^{l+1} = X_{id}^l + V_{id}^{l+1} (13)$$

$$I^{l} = I^{l}_{max} - \frac{I^{l}_{max} - I^{l}_{min}}{iter_{max}} \times l, \tag{14}$$

where $i = 1, ..., N_p$, d = 1, ..., D; I denotes the inertia weight, c_1 and c_2 are learning factors, rd_1 and rd_2 are positive random numbers in the range [0,1] under normal distribution,

l is the lth iteration. Inertia weight has linear decreasing, in equation 14, I_{max} is the maximum value of inertia, I_{min} is the lowest, and $iter_{max}$ is total of iterations.

The particle X_{id} represents the optimal solution of the set of weights in the neural network, therefore X_id contains the ANN connections weights w and b.

D. Recomposing the time series

The recomposition of the time series is done with the addition of the estimated components, then the forecasted time series is obtained using

$$\hat{x} = \hat{C}_L + \hat{C}_H. \tag{15}$$

III. FORECASTING ACCURACY METRICS

The number of lags for the ANN is determined with the metric: Generalized Cross Validation (GCV), this determines the best number based on the accuracy of the forecasting probing a determined range of values. The evaluation of the forecasting is computed with the metrics: Mean Absolute Percentage Error (MAPE), Coefficient of determination R^2 , Root Mean Squared Error (RMSE), and Relative Error (RE).

$$RMSE = \sqrt{\frac{1}{N_{\nu}} \sum_{i=1}^{N_{\nu}} (x_i - \hat{x}_i)^2}$$
 (16)

$$GCV = \frac{RMSE}{(1 - K/N_v)^2} \tag{17}$$

$$MAPE = \left[\frac{1}{N_v} \sum_{i=1}^{N_v} |(x_i - \hat{x}_i)/x_i|\right] \times 100$$
 (18)

$$R^2 = 1 - \frac{\sigma^2(er)}{\sigma^2(x)} \tag{19}$$

$$RE = \sum_{i=1}^{N_{\nu}} (x_i - \hat{x}_i) / x_i$$
 (20)

where N_v is the validation (testing) sample size, x_i is the *i*-th observed value, $\hat{x_i}$ is the *i*-th estimated value, and K is the number of lagged values.

IV. RESULTS AND DISCUSSION

The applied data are available from the CONASET web site [22], and they represent the number of accidents and the injured of Concepción-Chile, from year 2000 to 2012 with weekly sampling. The training data set contains the 70% of the sample, consequently the testing data set contains the 30% In the next subsections are evaluated the time series forecasting strategy presented in Fig. 1.

A. Embedding and Decomposition

The time series is embed in a Hankel matrix, the optimal number of components M was determined using and initial number M = N/2 components. Once obtained the number the components, the differential energy ΔE , of each component

was computed, this is shown in the Fig. 2, the maximum peak represents the optimal M. The embedding and the decomposing is executed again with the optimal M, for time series number of accidents the optimal was M = 6, and for the time series injured people the optimal found was M = 4. The component of low frequency extracted and estimated for the time series number of accidents is shown in the Fig. 4a, while the component of high frequency the same time series is shown in the Fig. 4b. The component of low frequency extracted and estimated for the time series injured people is shown in the Fig. 5a, while the component of high frequency the same time series is shown in the Fig. 5b.

B. Estimation and Recomposition

The calibration of the number of lags of the ANN was determined with the GCV metric, for the two time series was found an optimal $ANN(K, N_h, 1)$, with K = 7 inputs for the time series number of accidents and K = 5 for the time series injured people as shown the Fig. 3, and the number of hidden nodes was assigned in $N_h = 6$ for the two time series, this value was computed with the natural logarithm of the training data set length (normally used in our experiments).

The PSO learning algorithm was applied to determine the weights of the ANN, after trial and error they were configured with a swarm of $N_p \times D$ dimension, $N_p = 40$ particles, and $D = Np \times N_h + N_h$, inertia weight parameter I has linear decreasing with a maximum value of 1 and a minimum value of 0.2, the acceleration factors c_1 and c_2 were fixed in 1.05 and 2.95 respectively, the $iter_m ax$ is 2500.

The evaluation performed at the testing stage for the time series number of accidents is presented in the Fig. 6 and Table I. The observed values vs. the estimated values are illustrated in the Fig. 6a, reaching a good accuracy, while the relative error is presented in the Fig. 6b, which shows that the 98.5% of the points present an error lower than the $\pm 10\%$.

The evaluation performed at the testing stage for the time series number of injured people is presented in the Fig. 7 and Table II. The observed values vs. the estimated values are illustrated in the Fig. 7a, reaching a good accuracy, while the relative error is presented in the Fig. 7b, which shows that the 95.54% of the points present an error lower than the $\pm 10\%$.

TABLE I Number of Accidents Forecasting

-	SVD-ANN-PSO	ANN-PSO
Components	6	_
RMSE	0.0211	0.087
MAPE	3.17%	14.48%
R^2	98.29%	70.71%
$RE \pm 10\%$	98.5%	48.76%

The results presented in Table I show that the major accuracy of the forecasting of the time series number of accidents is achieved with the model SVD-ANN-PSO(7,6,1), with a RMSE of 0.0211, and a MAPE of 3.17%, the 98.5% of the points have an relative error lower than the $\pm 10\%$.

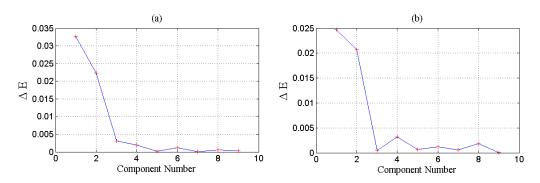


Fig. 2. ΔE : (a) Number of Accidents, (b) Injured people

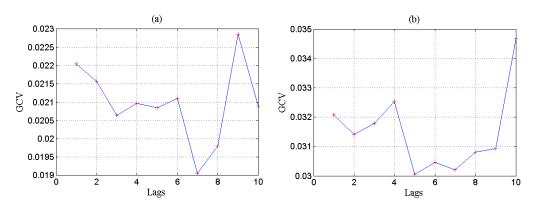


Fig. 3. Lags calibration (a) Number of accidents (b) Injured people

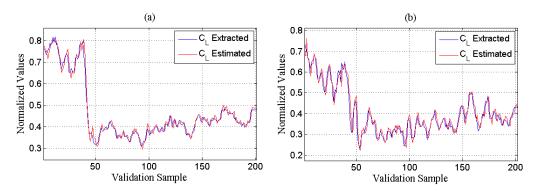


Fig. 4. Number of Accidents components (a) C_L , (b) C_H

TABLE II Injured people Forecasting

	SVD-ANN-PSO	ANN-PSO
Components	4	_
RMSE	0.0172	0.101
MAPE	3.58%	21.42%
R^2	98.5%	46.08%
$RE \pm 10\%$	95.54%	40.59%

The results presented in Table II show that the major accuracy of the forecasting of the time series injured people is achieved with the model SVD-ANN-PSO(5,6,1), with a *RMSE* of 0.0172, and a *MAPE* of 3.58%, the 95.54% of the points have an relative error lower than the $\pm 10\%$.

V. CONCLUSIONS

The proposed forecasting strategy is based on the time series decomposition using the singular values of the Hankel matrix. The strategy consists of four stages: embedding, decomposition, estimation, and recomposition. The embedding consists in mapping the time series in a Hankel matrix. The decomposition is based on SVD technique, SVD extracts the components of low and high frequency of the time series, the estimation is executed with an ANN based on PSO, while the recomposition is made with the single addition of the estimated components.

For evaluation of this strategy, we implemented a conventional ANN based on PSO. The best result was obtained

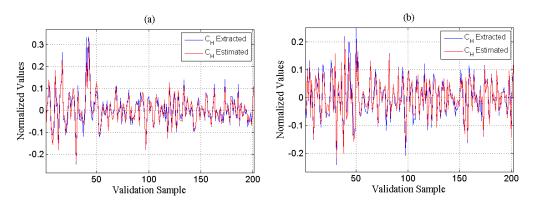


Fig. 5. Injured people components(a) C_L , (b) C_H

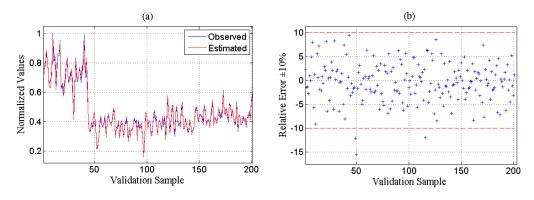


Fig. 6. SVD-ANN-PSO(7,6,1) (a) Observed vs. Estimated (b) Relative Error

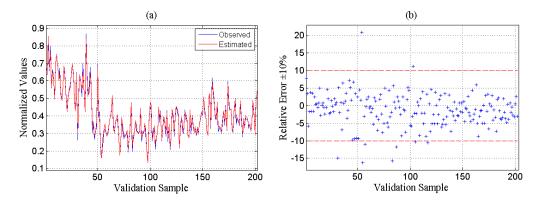


Fig. 7. SVD-ANN-PSO(5,6,1) (a) Observed vs. Estimated (b) Relative Error

with the proposed strategy for the two time series analyzed, SVD-ANN-PSO shows superiority regards the conventional implementation. For the time series number of accidents, SVD-ANN-PSO reaches an *RMSE* of 0.0211, and a *MAPE* of 3.17%, in front of the conventional ANN-PSO that reaches an *RMSE* of 0.087, and a *MAPE* of 14.48%. For traffic accidents reaches an *RMSE* of 0.0172, and a *MAPE* of 3.58%, in front of the conventional ANN-PSO that reaches an *RMSE* of 0.101, and a *MAPE* of 21.42%.

In the future, this strategy will be evaluated with data of traffic accidents of other regions of Chile, other countries, and with time series of other engineering fields.

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