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Ground-Wave Propagation Effects on Transmission Lines through Error Images

Efectos de la propagación de ondas en tierra en líneas de transmisión a través de imágenes de error

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Abstract

Electromagnetic transient calculation of overhead transmission lines is strongly influenced by the natural resistivity of the ground. This varies from 1-10K (Ω ·m) depending on several media factors and on the physical composition of the ground. The accuracy on the calculation of a system transient response depends in part in the ground return model, which should consider the line geometry, the electrical resistivity and the frequency dependence of the power source. Up to date, there are only a few reports on the specialized literature about analyzing the effects produced by the presence of an imperfectly conducting ground of transmission lines in a transient state. A broad range analysis of three of the most often used ground-return models for calculating electromagnetic transients of overhead transmission lines is performed in this paper. The behavior of modal propagation in ground is analyzed here into effects of first and second order. Finally, a numerical tool based on relative error images is proposed in this paper as an aid for the analyst engineer to estimate the incurred error by using approximate ground-return models when calculating transients of overhead transmission lines.

Keywords:

- ground-return effects
- earth impedances
- low frequency effects
- electromagnetic transients
- error images

Resumen

El cálculo de transitorios electromagnéticos en líneas aéreas de transmisión está fuertemente influenciado por la resistividad natural eléctrica del suelo. Esta puede variar de 1-10K (Ω ·m) dependiendo de diversos factores en el medio y de la composición física del suelo. La precisión en el cálculo de la respuesta transitoria en un sistema depende en parte del modelo de retorno por tierra, el cual debe considerar la geometría de la línea, la resistividad eléctrica y la dependencia frecuencial de la fuente de alimentación. Hasta la fecha hay pocos reportes en la literatura especializada acerca del análisis de los efectos producidos por la presencia de un suelo conductor imperfecto de líneas de transmisión en estado transitorio. En este artículo se realiza un análisis de amplio rango a tres de los modelos de tierra actualmente más utilizados para cálculo de transitorios electromagnéticos en líneas aéreas de transmisión. El comportamiento de la propagación modal en tierra se analiza aquí en dos tipos de efectos de retorno por tierra. Finalmente, se propone en este artículo una herramienta numérica basada en imágenes de error relativo como una ayuda para que el ingeniero analista pueda estimar el error incurrido por utilizar modelos aproximados de tierra para el cálculo de transitorios en líneas aéreas de transmisión.

Descriptores:

- efectos de retorno por tierra
- impedancias de tierra
- efectos de baja frecuencia
- transitorios electromagnéticos
- imágenes de error

Introduction

The analysis of wave propagation effects on overhead transmission systems due to the presence of an imperfectly conducting ground, is critically important to assess the frequency dependent losses and phase delay of ground modes. By its own structure, the electric line parameters Z (series-impedance) and Y (shunt-admittance) characterize the ground-return effects on a first and second order, respectively.

First order effects arise when the influence of the ground prevails over the geometric influence of the line. This is the case when the characteristic impedance of the system, $Z_C = \sqrt{Z/Y}$, plays an important role in the simulation; $e.\ g.$, on transient short-circuit currents calculation (Marti and Uribe, 2002). In this case, the frequency dependence of Z_C is entirely due to the ground-return path (Wedepohl, 1965).

The second order effects arise in the calculation of the modal voltage propagation function of the line $e^{-\gamma\lambda}$ where $\gamma = \sqrt{Z \cdot Y}$ and l is the line length. In terms of propagation functions, when forming the product $Z \times Y$ the geometric effects tend to cancel out each other, except for the different influence of the ground (Marti and Uribe, 2002).

The problem here is that, up-to-date, there is no general criterion to evaluate the ground conduction effects on transmission line propagation. Another problem is the evaluation of how the ground-return conduction effects impact on transmission line systems when switching transients occur.

Thus, it is the main idea of this paper to perform a new algorithmic methodology to analyze the first and second order ground-return conduction effects on voltage and current transient waveforms of overhead transmission systems.

First, a broad range solution of the Carson's integral (Carson, 1926) is developed and implemented in this paper based on a previously established algorithmic technique published in (Uribe *et al.*, 2004; Ramirez and Uribe, 2007). In addition, normalized dimensionless parameter comparisons with the Carson's series and complexdepth closed-form approximations (Gari, 1976; Kostenko, 1955; Deri *et al.*, 1981; Alvarado and Betancourt, 1983) are obtained here through the relative error criterion. This methodology yields a new technique proposed here as an aid to estimate ground-return modeling error on transients calculation through error images.

Finally, the impact of ground-return modeling errors on transients calculation is identified here with an application example accurately solved via the Numerical Laplace Transform (Uribe *et al.*, 2002).

Algorithmic solution of carson's integral

Figure 1 shows two overhead infinite thin perfect conductors over an imperfectly conducting ground $0 < \sigma_2 < \infty$. The series-impedances contribution (in Ω ·m) is given by (Marti and Uribe, 2002)

$$Z = \frac{j\omega\mu_0}{2\pi}P_M + Z_{Con} + Z_E, \tag{1}$$

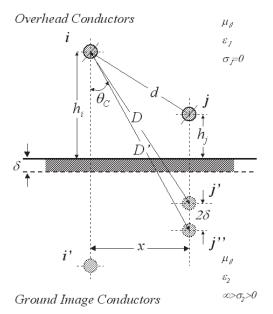


Figure 1. Two overhead conductors and their ground-images

where P_M is the dimension-less Maxwell's potential-coefficient, Z_{Con} is the internal conductor impedance and Z_E introduces the ground-return impedance contribution. Assuming a uniform line, homogeneous soil and neglecting inner displacement currents, the self or mutual ground-return impedances are given by the Carson's integral (in MKS system) (Carson, 1926)

$$Z_{E} = \frac{\omega \mu}{\pi} J(p, q). \tag{2}$$

where

$$J(p,q) = \int_{0}^{+\infty} (\sqrt{\alpha^2 + j} - \alpha) \cdot \exp(-p \cdot \alpha) \cdot \cos(q \cdot \alpha) d\alpha.$$
 (3)

A characterization of the Carson's dimensionless parameters p and q is useful to analyze the regular oscillating pattern of the integrand where α is the dummy variable. Carson introduced in (Carson, 1926) the following physical variables of the medium properties according to Figure 1

$$h' = h\sqrt{\omega\mu\sigma}$$
 (4a)

and

$$X' = x \sqrt{\omega \mu \sigma}$$
 (4b)

Expression (4a) and (4b) are normalized by the magnitude of the Skin Effect (Marti and Uribe, 2002; Wedepohl, 1965; Carson, 1926; Uribe *et al.*, 2004; Ramírez and

Uribe, 2007; Gari, 1976; Kostenko, 1955; Deri *et al.*, 1981; Alvarado and Betancourt, 1983; Uribe *et al.*, 2002; Piessens *et al.*, 1983; Using MATLAB, 2011; Dommel, 1986). Now, Carson's dimensionless parameter *p* and *q* for the self-impedance case are given by

$$p = 2h' \text{ and } q = 0, \tag{5a,b}$$

and for mutual impedances:

$$p = h'_i + h'_i$$
 and $q = x'$. (6a,b)

The integrand in (3) contains three factors. The first two are of the damping type while the third is regular oscillatory. The pattern of these factors suggests a new strategy for its numerical efficient solution. Consider the solution of the first factor radical function in (3) as (Uribe *et al.*, 2004; Ramirez and Uribe, 2007)

$$\sqrt{\alpha^2 + j} = F(\alpha) + j \cdot G(\alpha), \tag{7a}$$

where

$$F(\alpha) = \frac{\alpha}{\sqrt{2}} \sqrt{1 + \sqrt{1 + 1/\alpha^4}} \tag{7b}$$

$$G(\alpha) = \frac{\alpha}{\sqrt{2}} \sqrt{\sqrt{1 + 1/\alpha^4} - 1}.$$
 (7c)

Functions $F(\alpha)$ and $G(\alpha)$ provide the additional damping components to the integrand. Substituting (7b) and (7c) in (3) and decomposing into real and imaginary components, (3) becomes

$$J(p,q) = \int_{0}^{+\infty} \left[F(\alpha) - \alpha \right] \cdot \exp(-p\alpha) \cdot \cos(q\alpha) \, d\alpha \dots$$

$$+j\int_{0}^{+\infty} \left[G(\alpha) \right] \cdot \exp(-p\alpha) \cdot \cos(q\alpha) \, d\alpha \tag{8}$$

Functions $F(\alpha) - \alpha$ and $G(\alpha)$ in the first complex factor of (8) are monotonically decreasing. Figure 2 illustrates the behavior of these functions that for $\alpha > 1$ tends asymptotically to " $1/(8\alpha^3)$ " and " $1/(2\alpha)$ ", respectively (Uribe *et al.*, 2004; Ramirez and Uribe, 2007).

The second complex factor in (8) only depends on the normalized parameter *p*. This factor is a pure damping exponential function. The truncation criterion developed in (Uribe *et al.*, 2004; Ramirez and Uribe, 2007) with a relative error control can be extracted from its properties as

$$\varepsilon_{rror} = \exp\left(-p \cdot \alpha_{\text{máx}}\right),\tag{9}$$

and the truncating criterion by approximating "J(p,q)" for the new truncated range would be (Uribe *et al.*, 2004; Ramírez and Uribe, 2007)

$$\alpha_{\text{max}} = \lambda / p \tag{10a}$$

and

$$\lambda = -\ln(\varepsilon_{rror}) \tag{10b}$$

The error level can be controlled refining λ . A value of $\lambda = 10$ has proved satisfactory enough for many practical application cases.

The third factor in (8) provides regular oscillations to the integrand which increases equal times as the argument $q \times \alpha$ exceeds the value of π / 2. This argument is related to the horizontal distance between conductors (x in Figure 1) and to the magnitude of Skin Effect Layer Thickness (Carson, 1926; Uribe et al., 2004; Ramírez and Uribe, 2007). Within the range $[0, \alpha_{max}]$ this factor will not oscillate if

$$\alpha_{\max} \le \pi / (2q). \tag{11a}$$

If condition (11a) is not satisfied, the integrand oscillations would produce magnified round-off errors when integrating with generic quadrature routines (Piessens *et al.*, 1983). To avoid this problem, it is necessary to detect the zero crossings with:

$$k = \inf\left\{\frac{1}{2} + \frac{q\alpha}{\pi}\right\}, \quad k = 1, 2, 3, ..., K_{\text{max}}$$
 (11b)

where k is the corresponding oscillation sequence, "int" is the complete integer value and K_{\max} indicates the maximum number of oscillations that are given by

$$K_{\text{max}} = \text{int}\left\{\frac{1}{2} + \frac{\lambda}{\pi} \cdot \left(\frac{q}{p}\right)\right\}.$$
 (11c)

Notice in (11c) that (q/p) = (x'/h'). Obviously, from (11b) for each value of k the integrand zero crossing would be

$$\alpha_k = \frac{\pi(2k-1)}{2q}, \qquad k = 1, 2, 3, ..., K_{\text{max}}$$
 (11d)

A new reliable and efficient broad range algorithmic evaluation of the Carson's integral has been obtained by using the truncating criterion in (10) with the zero crossing identification in (11) for 10×532 samples insi

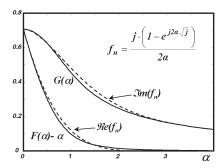


Figure 2. Carson's integrand first factor analysis

de Table 1 ranges (Uribe *et al.*, 2004; Ramirez and Uribe, 2007).

The physical variable ranges in Table 1 have been used to calculate the normalized Carson parameters shown in Table 2 to perform the algorithmic calculation of (8).

Figures 3a and 3b depict the broad solution set obtained with the algorithmic technique proposed in this paper.

The figures were generated solving Carson's integral 10 × 532 times which takes about more than one second on a 3.4GHz, 8GB RAM computer, running MATLAB® V. 7.12 (Using MATLAB®, 2001).

Table 1. Application ranges for physical variables

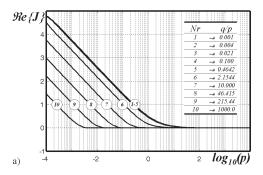
$0.1 \le h_{i,j} \le 2 \times 10^2$	[m]
$10^{-1} \le x \le 10^3$	[m]
$2\pi \le \omega \le 2\pi \times 10^6$	[rad/s]
$10^{-4} \le \sigma \le 1$	S/m

Table 2. Ranges for Normalized Dimensionless Vector Parameters

10^{-4}	≤	р	≤	10^4	
10^{-7}	<	q	<	10^{7}	

Implementation of Carson's series and complex depth formulae

In the synthesis of frequency dependent electromagnetic transients the need of a higher sampling refinement interval is often required (Wedepohl, 1965; Uribe *et al.*, 2002). There are cases when it is necessary to handle very small or high ground conductivity values; *e.g.*, from rocky to moist ground (Dommel, 1986). Also there are other cases when the distance between conductors is wider ($\theta_C > \pi/4$); *e.g.*, interference on communication lines due to a power line fault (Dommel, 1986). In all these cases, it is highly convenient to have an accurate methodology for calculating the mutual ground-return impedances between both energy systems.



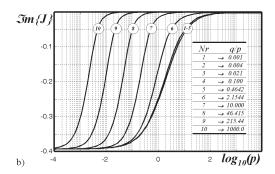


Figure 3. Carson's integral algorithmic solution for ranges shown in Table 2, a) curves of $\Re\{\{(p,q)\}\}$, b) curves of $\Im\{\{(p,q)\}\}$

A numerical version of the Carson's series has been also implemented here to test and verify the efficiency and accuracy of the algorithmic solution proposed in this paper (Carson, 1926; Dommel, 1986). However, in the treated application case, the series solution presented some serious disadvantages; the number of terms is practically unpredictable, numerical discontinuities emerges when switching from infinite to finite convergence ranges and also, it turns time consuming. For these reasons, the original series solution in Carson (1926) cannot be used to generate the error images proposed in the following paper section.

Thus, using the original Carson's parameters the following normalized distance according to Figure 1 is introduced as (Carson, 1926)

$$D = \sqrt{p^2 + q^2} \tag{12a}$$

with a Carson's angle between vectors of

$$\theta_C = \tan^{-1}(q/p) \tag{12b}$$

Regarding the component partition (8), one can infer that

$$J(p,q) = P + j \cdot Q, \tag{12c}$$

and according to this paper nomenclature

$$P = \int_{0}^{+\infty} \left[F(\alpha) - \alpha \right] \cdot \exp(-p\alpha) \cdot \cos(q\alpha) \, d\alpha \tag{12d}$$

$$Q = \int_{0}^{+\infty} \left[G(\alpha) \right] \cdot \exp(-p\alpha) \cdot \cos(q\alpha) \, d\alpha \tag{12e}$$

The following Carson parameter introduces the normalized distance between a real conductor in the air and the image of the other conductor inside the ground. This parameter also was used as a boundary quantity to

adjust the switching process of the series when changing from a finite range $a \le 5$ into an infinite one a > 5 (Carson, 1926; Dommel, 1986):

$$a = 4\pi\sqrt{5} \times 10^{-4} \cdot D \cdot \sqrt{\omega\sigma/2\pi}$$
 (12f)

As an application example, consider an aerial transmission line with conductor height h=20 m. The distance between conductors is $0 \le x \le 1$ Km. The ground conductivity is 0.01 S/m and the frequency range is $1 \le \omega/2\pi \le 10^6$ Hz.

To test accuracy and efficiency of the here developed algorithmic technique, an equivalent solution of J(p,q) in (12c) has been calculated using the Carson series (Carson, 1926). The real and imaginary components are shown in Figure 4. At first sight the differences appear to be indistinguishable, but in Figure 5, two types of numeric discontinuities arise when calculating the relative error (Ramirez and Uribe, 2007).

The first one is due to the series adjustment, while the second (in the form of peak discontinuities) is due to the switching series process, when changing from an infinite range into the new truncated range (Dommel, 1986).

For this example layout, Figure 6 shows the magnitude and angle relationship between the vector components *P* and *Q* from (12d, e) calculated with the Carson series varying parameter *D*. The here obtained curves match with the obtained ones in Carson's paper confirming the accuracy of the method (Carson, 1926).

In addition, the obtained algorithmic solution set is used to confirm the accuracy ranges of the complex-depth based formulas of Gary (1976), Kostenko (1955), Deri *et al.* (1981) and Alvarado *et al.* (1983).

Basically, classical images complex depth formulas are based in the following expression

$$\frac{2\beta}{\beta + \sqrt{\beta^2 + 1/\delta^2}} = 1 - e^{-2\beta \cdot \delta},\tag{13a}$$

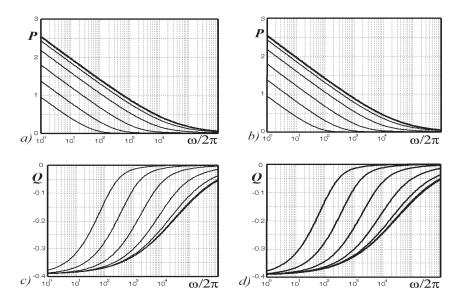


Figure 4. Application example layout, a) series real component, b) algorithm real component, c) series imaginary component, d) algorithm imaginary component

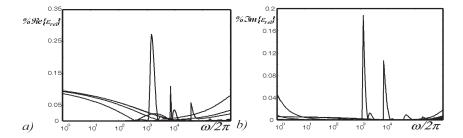


Figure 5. Numerical discontinuities presented between algorithmic solution set and the Carson series when calculating the relative error, a) real component, b) imaginary component

where $\beta=\alpha\cdot\sqrt{\omega\mu_0\sigma}$. After some algebraic manipulations (13a) is transformed into (Ramirez and Uribe, 2007)

$$f_n = F(\alpha) - \alpha + j \cdot G(\alpha) \approx \frac{j}{2\alpha} \left(1 - e^{j2\alpha\sqrt{j}} \right).$$
 (13b)

The behavior of $F(\alpha)$ and $G(\alpha)$ is shown in Figure 2, as well as for f_n . On introducing the right side of (13b) into (8) we have

$$J(p,q) = \int_{0}^{+\infty} \left[\frac{-j}{2\alpha} e^{j2\alpha\sqrt{j}} \right] \cdot e^{-p\alpha} \cdot \cos(q\alpha) \, d\alpha \dots$$
$$+ j \int_{0}^{+\infty} \left[\frac{j}{2\alpha} \right] \cdot e^{-p\alpha} \cdot \cos(q\alpha) \, d\alpha$$
(13c)

An analytical solution can be obtained directly from (13c) (Gary, 1976; Kostenko, 1955; Deri *et al.*, 1981; Alvarado *et al.*, 1983). Now, the complex depth formulae are transformed into a normalized dimensionless parameter expression of p and q. Thus, according to Z_E in (2) the self-impedance J_s and the mutual-impedance J_m for the

Gary, Kostenko, Deri et. al., and Alvarado et. al. formulae becomes

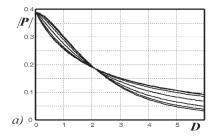
$$J_{s \text{ Gary}} = \frac{j}{2} \ln \left(1 - \frac{j \cdot \sqrt{j}}{p} \right) \tag{14a}$$

$$J_{sAlv} = \frac{j}{2} \left\{ \ln \left(1 - \frac{j\sqrt{j}}{p} \right) - \frac{1}{12} \cdot \frac{1}{\left(1 + \sqrt{j} \cdot p \right)^3} \right\}. \tag{14b}$$

$$J_{s Kost} = \frac{j}{2} \ln \left(\sqrt{\frac{p^2 \left(1 + q^2 / p^2\right) - 4j \left(1 + p \cdot \sqrt{j}\right)}{p^2 + q^2}} \right)$$
(14c)

And for the mutual impedance case

$$J_{m Gary} = \frac{j}{2} \ln \left\{ \sqrt{\frac{q^2 + (p - 2j \cdot \sqrt{j})^2}{p^2 + q^2}} \right\}$$
 (14d)



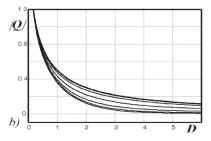


Figure 6. Series solution varying physical parameters p and q in Table 1, a) magnitude of the real component P/P, b) magnitude of the imaginary component |Q|

$$J_{m \ Alv} = \frac{j}{2} \left\{ \frac{1}{2} \ln \left(\frac{\left(1 - \frac{2j \cdot \sqrt{j}}{p}\right)^{2} + \frac{q^{2}}{p^{2}}}{1 + \frac{q^{2}}{p^{2}}} \right) - \frac{1}{24} \left[\frac{1}{\left[\frac{p\sqrt{j}}{2} \cdot \left(1 + j \cdot \frac{q}{p}\right) + 1\right]^{3}} \dots \right] \right\}$$

$$+\frac{1}{\left[\frac{p\sqrt{j}}{2}\cdot\left(1-j\cdot\frac{q}{p}\right)+1\right]^{3}}\right]$$
(14e)

$$J_{m \text{ Kost}} = \frac{j}{2} \ln \left\{ \frac{\sqrt{4 \cdot \left(1 + p\sqrt{j}\right) + j \cdot p^2 \cdot \left(1 + \frac{p^2}{q^2}\right)}}{p\sqrt{j} \cdot \sqrt{1 + \frac{p^2}{q^2}}} \right\}$$
(14f)

The approximation (14) for self or mutual Z_E in (2), substitutes J(p,q) in (8). In essence Gary, Kostenko, Deri *et al.* formulas have presented almost identical behavior between each other when plotting their error images. In consequence, only the images formed with the Gary and Alvarado *et al.* expressions are the only ones studied in this paper. Thus, the broad range result set is used now to generate the curves shown in Figure 7 for the P and Q components of (12c) in a parametric version of (14d) and (14e).

Error images estimation of ground models

The ground resistivity magnitude is introduced here into the electromagnetic transient calculation via the Z_E model. Thus, an important problem arises when estimating the ground modeling error. A new technique to estimate ground modeling errors on electromagnetic transient calculation is proposed in this paper section through error images. First, the broad range algorithmic solution (8), the approximated formulas by Gary in

(14d) and the one by Alvarado *et al.* in (14e) are compared here through the relative error criterion as (Uribe *et al.*, 2004; Ramirez and Uribe, 2007)

$$\varepsilon_{rel} = \left| 1 - \left(Z_{E,Approx} / Z_E \right) \right| \times 100 \tag{15a}$$

where Z_E is the algorithmic solution ground impedance and $Z_{E, \, \mathrm{Approx}}$ is the approximate images ground impedance formula. Figure 8 shows the generated error images (15a) using 10^2 samples inside data in Table 2. Each image shows five error regions. The error levels lie in the range of $1\% \le \varepsilon_{\mathrm{rel}} \le 10\%$.

Thus, a practical ground-modeling error estimation algorithm through images is proposed as follows:

First step. Using physical variables (h_i, h_j, x, r) and relative medium properties $(\mu_r, \sigma, \varepsilon_r)$, evaluate the parameter relation q/p for each voltage coupling loop inside the system. The larger number of circuit loops, the more error line paths images are generated.

Second step. Calculate the NLT parameters (Uribe *et al.*, 2002). Set the observation time $T_{\rm obs}$ and the number of samples $N_{\rm samp}$, then the other parameters can be calculated as

$$\Delta t = T_{\text{obs}} / N_{\text{samp}} \tag{15b}$$

$$\Omega = \pi/\Delta t \tag{15c}$$

$$\Delta \omega = 2\Omega/N_{\text{samp}} \tag{15d}$$

$$c = -\ln(v)/T_{\text{obs}}. (15e)$$

where ω is the angular frequency, Δt is the sampled time increment, Ω is the truncating frequency, $\Delta \omega$ is the sampled frequency increment, c is the complex frequency damping coefficient and v is the discretization relative error level. Further, evaluate the complex frequency variable

$$s = c + j \cdot \omega, \tag{15f}$$

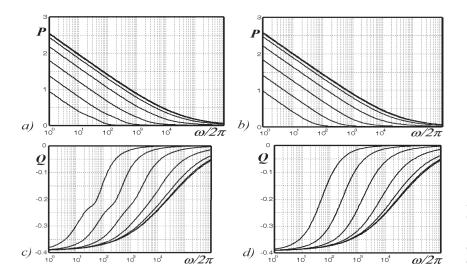


Figure 7. *J*(*p*,*q*) complex depth based formulae varying physical parameters in Table 1, a) Gary *P* component (1976), b) Alvarado et al., *P* component (1983), c) Gary *Q* component (1976), d) Alvarado et al. *Q* component (1983)

Third step. Find the maxima and minima boundary values of the transient Skin Effect variable using (15f) for calculating δ

$$\delta_{Tran} = 1 / \sqrt{\frac{s}{\max/\min} \cdot \mu_0 \sigma}, \qquad (15g)$$

then, evaluate the normalized function $p_{\text{max/min}}$ as

$$p_{\text{max/min}} = 2 \cdot h / \left| \delta_{\text{Tran}} \right|_{\text{max/min}}$$
 (15h)

Fourth step. Plot the previously generated error image for the ground-model and trace the error line paths according q/p sorting min and max frequency samples.

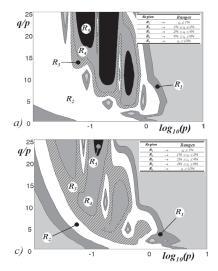
Fifth step. Check the sampled error points region in the images. Their influence area would be their corresponding error levels.

Ground-return conduction effects in transients

In this research paper, the ground-return effects are analyzed according to a first and second order kind. On one hand, first order effects are given when the influence of the ground prevails over the geometric influence of the line. This is the case when $Z_{\mathbb{C}}$ has an important role in the numerical simulation. In the frequency limits $Z_{\mathbb{C}}$ becomes

$$Z_{C} \cong \sqrt{\frac{\mu_{0}}{\varepsilon_{0}}} \cdot \frac{P_{M}}{2\pi} + \frac{1}{\sqrt{\omega}} \cdot \sqrt{\frac{P_{M}}{j2\pi\varepsilon_{0}}} \cdot \sqrt{Z_{Con} + Z_{E}}$$
 (16a)

$$Z_{C} \cong \sqrt{\frac{\mu_{0}}{\varepsilon_{0}}} \cdot \frac{P_{M}}{2\pi}$$
 (16b)



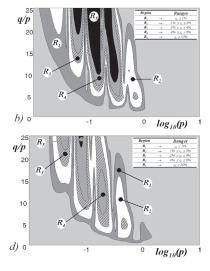


Figure 8. Error images to estimate numerical accuracy of complex depth formulas (Gary, 1976; Alvarado and Betancourt, 1983), a) P component of $J_m(p,q)_{\text{Gary}}$, b) P component of $J_m(p,q)_{\text{Gary}}$, d) Q component of $J_m(p,q)_{\text{Alva}}$, c) Q component of $J_m(p,q)_{\text{Alva}}$

The frequency dependency of (16a) is entirely due to the ground-return contribution, since $Z_{Con} \rightarrow 0$.

On the other hand, the second order effects arise when forming the product $Z \cdot Y$, because the geometric effects tend to cancel out each other, except for the different influence of the ground (Marti, 2002).

This is the case of the voltage propagation function $e^{-\gamma xl}$. Thus, γ tends asymptotically to

$$\gamma \cong 0 \tag{16c}$$

$$\gamma \cong j\omega\sqrt{\mu_0\,\varepsilon_0} \cdot \mathbf{U} \tag{16d}$$

where **U** is the unit matrix (Wedepohl, 1965).

Consider a typical overhead transmission system as the one depicted in Figure 9. This is a homogeneous three-phase power line with a ground wire and a single communications line sharing a common right of way. The system length is 10 Km. The corresponding conductors radii are r_i = 3.20 cm, r_j = 2.5 cm and r_k = 1.5 cm. The soil conductivity is σ = 0.005 S/m.

The frequency dependent behavior of modal propagation functions Z_C and e^{-rl} for each numbered conductor in Figure 9 is illustrated in Figure 10. The impact of Gary and Alvarado ground-return models (Gary, 1976; Kostenko, 1955; Deri *et al.*, 1981; Alvarado *et al.*, 1983) in the transient step response is illustrated here the by means of a two circuit test using the NLT for the energy system shown in Figure 9 (Uribe *et al.*, 2002).

The first test is the calculation of the transient step voltage-response at the remote end with an open circuit condition of the system using the here treated groundreturn models for comparison.

Figures 11a and 11b show the receiving end voltage response at the energized conductor (No. 1 in Figure 9) and the induced voltage response at the communications line (No. 5 in Figure 9), respectively.

Figure 11c and 11d show the corresponding relative errors (15a) calculated for the obtained voltages, for the Gary and Alvarado-Betancourt models with respect to the Carson solution (Gary, 1976; Kostenko, 1955; Deri *et al.*, 1981; Alvarado *et al.*, 1983). In this case the Gary model is amazingly accurate.

The second test consists in the calculation of the transient step current response at the remote end with a short circuit condition of the system calculated with the here treated approximated ground-return models.

Figure 12a show the current transient step response calculated at the energized conductor (No. 1), while Fi-

gure 12b depicts the corresponding circulating current at the victim circuit of communications line (No. 5).

Figures 12c and 12d, show the calculated relative errors (15a) for the circulating currents at the energized conductor and at the induced communications line, respectively. One more time the accuracy of the Gary model can be noticed from these figures.

As ground-return models are strong frequency dependent as can be seen in Figure 10b, a better general tool for analyzing the effects of a ground-return model in electromagnetic transients calculation is the images methodology proposed in Figure 13.

Consider the error images in Figure 8 calculated in magnitude quantities for the Deri *et al.* (1981) and Alvarado *et al.* (1983) models. Two sets of error line paths have been traced in each of both figures. The horizontal error line path, represents a particular coupling circuit loop for any set of two specific conductors present in the transmission system shown in Figure 9.

As an application example, consider the two sets of traced error line paths shown in Figure 13. The first set p_1 - p_2 and p_5 - p_6 corresponds to the loop formed between the energized power conductor and the victim communications line.

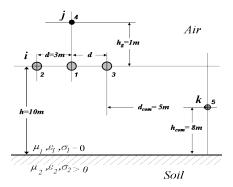
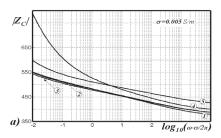


Figure 9. Power transmission system with a ground wire in the proximity of a victim communications line

The second set of error line paths p_3 - p_4 and p_7 - p_8 correspond to the hypothetical case of calculating four times the magnitude q/p. An error less than 1% corresponds to the image points p_5 and p_7 , which have an implicit frequency of 220 Hz. The error of p_6 lies well within 1% and 2%. Points p_1 , p_2 and p_3 have an error between 4% and 6%. The image points p_4 and p_8 lie into region five, having an error greater than 10%. In this application case, any other image point has an implicit truncating frequency of 102 KHz.



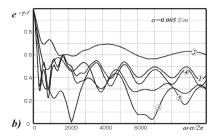


Figure 10. Frequency behavior of propagation modal functions, *a*) characteristic impedance Z_C and *b*) propagation function e^{-T}

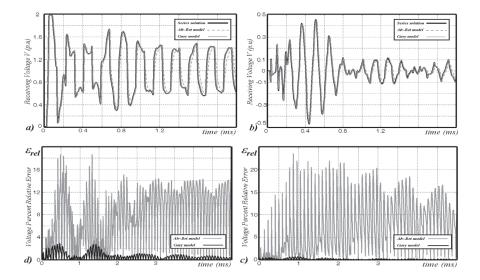


Figure 11. Voltage transient responses at the remote and ground modeling errors, a) voltage response at energized conductor, b) induced over-voltage at the remote end of communications line, c) relative error at energized conductor, d) relative error at induced communications line

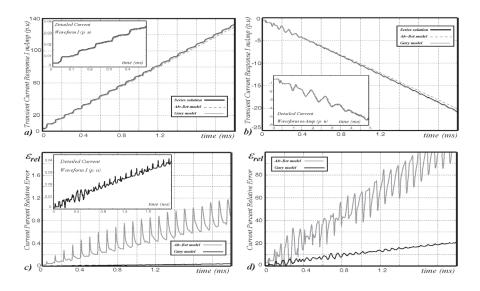
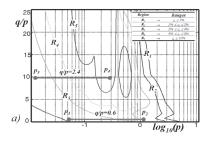


Figure 12. Current transient step response and relative ground modeling errors, a) response at the energized conductor, b) circulating current at the communications line, c) relative error at the energized conductor, d) relative error at the communications line



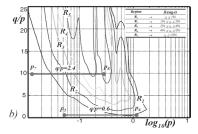


Figure 13. Magnitude of relative error images and traced line paths for the system example shown in Figure 9, a) Deri et al. ground model image, b) Alvarado et al. ground model image

Conclusions

An accurate numerical algorithm for solving the Carson's integral, their classical series expansion and complex-depth approximate formulae, has been implemented in this paper for a broad range of applications, emphasizing the case $\theta_C > \pi/2$.

In the specific application example presented in this paper the transient-step responses calculated at the remote end of open-circuit voltages and short-circuit circulating currents, the ground-return model of Gary presented a more accurate result than the Alvarado *et al.* model. The main differences are probably due to the validity ranges of the implicit frequency in the transient calculation and, of the separation distance between conductors of the latter model.

A new technique for estimating ground-return modeling errors on electromagnetic transients calculation is proposed in this paper through error images.

The frequency dependence of the ground has been separated here into effects of first and second order. These are mainly due to the modal propagation functions in the ground $\gamma(\omega)$ and to the characteristic impedance function $Z_C(\omega)$.

A methodology to analyze the impact of ground modeling errors on low frequency transients has been proposed here through error images, tracing simple error line paths on each image for a certain ground model having a universal applicability.

Nomenclature

 ω = angular frequency

 μ_0 = magnetic permeability of vacuum and air

 ε_0 = dielectric permittivity of vacuum and air

 σ = soil conductivity

δ = complex depth of the Skin Effect layer thickness $\delta = 1/\sqrt{j_0\mu_0\sigma}$

 $h = \text{conductor height } (h_i \text{ or } h_i)$

x = horizontal distance between conductors

d = distance between conductors

D = distance between one real conductor and the image of the other

 θ_C = Carson's angle

h' = conductor height "h" normalized by the magnitude of the Skin Effect layer " δ ",

x' = horizontal distance between conductors "x" normalized by the magnitude of the Skin Effect layer "/ δ /"

p = sum of normalized conductor heights $h_i' + h_j'$ or h' for the self impedance case

q = normalized horizontal distance between con ductors x´ or equal to zero for the self impedance case

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