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## Simulating gas-liquid mass transfer in a spin filter bioreactor

## Simulación de la transferencia de masa en un biorreactor de perfusión operado con un filtro rotativo

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### Abstract

Computational fluid dynamics (CFD) and population balance model (PBM) model have been used to simulate hydrodynamics and mass transfer in a 0.014 m<sup>3</sup> Spin Filter Bioreactor. The operating conditions chosen were defined by typical settings used for culturing plant cells. Turbulence, rotating flow, bubbles breakage and coalescence were simulated by using the k- $\epsilon$ , MRF (Multiple Reference Frame) and PBM approaches, respectively. The numerical results from different operational conditions are compared with experimental data obtained from measurements and good fitting data is achieved. Interested by these simulated and experimental results CFD simulations are qualified as a very promising tool not only for predicting gas-liquid hydrodynamics but also for finding design requirements that must be implemented to optimize an aerobic bioprocessing useful for plant cell culture applications which are characterized by the constrain of achieving relatively high mass transfer conditions and avoiding cellular damage due to hydrodynamic conditions.

-----**Keywords:** bioreactor, scale up, multiple reference frame (MRF), population balance model (PBM), spin filter

### Resumen

Mediante dinámica de fluidos computacional (CFD) y métodos de balance poblacional (PBM) se simuló la hidrodinámica líquido-gaseosa y la transferencia de masa en un biorreactor de 0,014 m<sup>3</sup> operado con un Spin Filter para cultivos en modo perfusión. Las condiciones de operación fueron definidas con base en los requerimientos para células vegetales

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en suspensión. Los fenómenos de turbulencia, flujo giratorio, ruptura y coalescencia de burbujas fueron simulados utilizando los modelos k- $\epsilon$ , MRF (Multiple Reference Frame) y PBM. Se logra una predicción aceptable mediante la comparación entre los resultados numéricos de las diferentes condiciones de operación y los datos experimentales de los valores del coeficiente de transferencia de masa. Con la motivación de estos resultados simulados y validados experimentalmente, se observa que CFD puede ser una herramienta muy prometedora, no sólo para la predicción de la hidrodinámica líquido-gaseosa, sino también para encontrar los requisitos de diseño que se deben implementar para optimizar un proceso biológico aerobio útil para aplicaciones de cultivos celulares de plantas, que son comúnmente caracterizados por el requerimiento de mantener condiciones relativamente altas tasa de transferencia de masa y simultáneamente evitar el daño celular debido a las condiciones hidrodinámicas.

-----**Palabras clave:** biorreactor, escalado, marco de referencia múltiple, método de balance poblacional, filtro rotativo

## Introduction

Global productivity in large scale processes depends on gas-liquid conditions. Supplying adequate oxygen levels in aerobic cell culturing is a common problem in fermentation technology. This problem is increased in high cell density bioreactors due to oxygen transfer rate limitations affecting cell growth and productivity. Such limitations are common in perfusion cell cultures leading to anoxic process, cellular damage and therefore loss of cell viability [1].

Perfusion technology is used for increasing the productivity of such compounds. One of the most common devices for perfusion processes is the Spin-Filter, which is used for animal and plant cell cultures in continuous production processes. Such bioreactors incorporate a rotating filter device into a stirred tank reactor. Cells are inoculated and cultivated by continuous addition of fresh nutrient medium. The spin-filter device minimizes the loss of cells through the bioreactor harvest. Consequently biomass productivity is increased substantially compared to batch or fed batch mode [1]. However oxygen requirements are proportional to cell density causing mass transfer limitations. There has been rapid progress in the modeling of large-scale performance by

the application of computational fluid dynamics (CFD). Successful examples are given covering the range from agitation systems, including models from single phase rotating impeller systems [2-6] to the use of population balance models [7-14]. The main purpose of these approaches is the knowledge of the flow fields in conventional stirred tanks (hydrodynamics) related to mass transfer profiles.

Spin-filters (SF) were proposed as cell retention devices for animal cell culture several decades ago [15] and became a popular device for perfusion cultivations both for small-scale studies and large-scale processes [16-18].

Although several works have dealt with the understanding flow field and particle dynamics of these devices, gas-liquid mass transfer phenomena and hydrodynamics has not yet been studied. To the authors knowledge CFD simulations for gas-liquid hydrodynamics in Spin Filter Bioreactor had never been used previously for evaluating mass transfer prediction. For this reason detailed understanding of hydrodynamic behavior can be useful not only for identifying mass transfer limitations but also for finding design requirements that must be implemented to optimize an aerobic bioprocessing. Hence it is

the motivation of this work to simulate gas-liquid hydrodynamics in a Spin Filter bioreactor using a CFD approach for mass transfer.

## Materials and methods

### Bioreactor setup

A Spin Filter stirred tank bioreactor (New Brunswick Celligen 310) with 0.008 m<sup>3</sup> working volume ( $T = 0.21$  m) was used in this study. The mixing is driven by a conventional Pitched Blade Impeller ( $D = 0.1$  m) mounted on a 0.02 m diameter shaft and placed at the center line of the bioreactor. The gas is supplied through a 0.02 m diameter cylinder micro-sparger. The operating conditions chosen were defined by typical settings used for culturing plant cells:  $N_i = 70, 140$  and  $210$  rpm, aeration rate =  $0.04$  vvm. The properties used in the primary phase (water) are:  $\rho_L$ :  $998.2 \text{ kgm}^{-3}$ ;  $\mu_L$ :  $0.001 \text{ kgm}^{-1} \text{ s}^{-1}$ ;  $\sigma$ :  $0.07 \text{ Nm}^{-1}$ . Secondary phase properties (air) are:  $\rho_G$ :  $1.225 \text{ kgm}^{-3}$ ,  $\mu_G = 1.789 \cdot 10^{-5} \text{ kgm}^{-1} \text{ s}^{-1}$  [19].

### Computational Fluid Dynamic Model

#### Multiphase Flow Equations

The gas and liquid phase are treated as interpenetrating continua and conservation of mass and momentum equations are solved for each phase. The conservation equations for each phase are derived to obtain a set of equations, which have similar structure for all phases [13, 20-25].

The Eulerian model is the most complex multiphase model in ANSYS FLUENT 13.0. It solves a system of  $n$ -momentum and continuity equations for each phase. The coupling is achieved through pressure and interfacial exchange coefficients. The mass conservation equation for each phase is shown (Eq. 1):

$$\frac{\partial}{\partial t}(\rho_i \alpha_i) + \nabla \cdot (\alpha_i \rho_i \vec{U}_i) = 0 \quad (1)$$

Where  $\rho_i, \vec{U}_i$  represent the density, volume fraction and mean velocity, respectively, of phase  $i$  (L or G). It is assumed that the liquid phase and the gaseous phase share space proportional to their volume, such that their volume fractions sum up to unity in the cell domain (Eq. 2):

$$\alpha_G + \alpha_L = 1.0 \quad (2)$$

The momentum equation for phase  $i$  is described below (Eq. 3):

$$\frac{\partial}{\partial t}(\rho_i \alpha_i \vec{U}_i) + \nabla \cdot (\alpha_i \rho_i \vec{U}_i \vec{U}_i) = \alpha_i \nabla p + \nabla \cdot \bar{\tau}_{effi} + \vec{R}_i + \vec{F}_i + \alpha_i \rho_i \vec{g} \quad (3)$$

$p$  is the pressure shared by both phases and  $\vec{R}_i$  represents the interfacial momentum exchange. The  $\vec{F}_i$  term represents the Coriolis and centrifugal forces expressed in the MRF (Multiple Reference Frame) model for rotating flows and is represented as (Eq. 4):

$$\vec{F}_i = -2\alpha_i \rho_i \vec{N} \times \vec{U}_i - \alpha_i \rho_i \vec{N} \times (\vec{N} \times \vec{r}) \quad (4)$$

$\vec{N}$  is the angular velocity,  $\vec{r}$  is the position vector. The Reynolds stress tensor  $\bar{\tau}_{effi}$  (Eq. 5) is related to the mean velocity gradients through the Boussinesq hypothesis [20]:

$$\bar{\tau}_{effi} = \alpha_i (\mu_{lam,i} + \mu_{t,i}) (\nabla \vec{U}_i + \nabla \vec{U}_i^T) - \frac{2}{3} \alpha_i (\rho_i k_i + (\mu_{lam,i} + \mu_{t,i}) \nabla \cdot \vec{U}_i) \bar{I} \quad (5)$$

$\mu_{lam,i}$  is the molecular viscosity of phase  $i$ ,  $\bar{I}$  is the strain tensor.

#### Interfacial Momentum Exchange

The most important interphase force is the drag force acting on the bubbles. This force (Eq. 6) depends on friction, pressure, cohesion, and other hydrodynamic effects [26].

$$R_L = -R_G = K (\vec{U}_G - \vec{U}_L) \quad (6)$$

$K$  is the exchange coefficient of liquid and gaseous phases and is determined by (Eq. 7):

$$K = \frac{3}{4} \rho_L \alpha_L \alpha_G \frac{C_D}{d} |\vec{U}_G - \vec{U}_L| \quad (7)$$

$d$  is the bubble diameter, and the drag coefficient  $C_D$  is defined as a function of Reynolds number (Eq. 8):

$$Re_p = \frac{\rho_L |\vec{U}_G - \vec{U}_L| d}{\mu_L} \quad (8)$$

To calculate the drag coefficient the standard correlation [27] was applied (Eq. 9):

$$C_D = \begin{cases} \frac{24(1 + 0.15 Re_p^{0.687})}{Re_p}, & Re_p \leq 1000 \\ 0.44, & Re_p > 1000 \end{cases} \quad (9)$$

### Equations for the turbulence model

The dispersed turbulence  $k - \varepsilon$  model can be considered as the multiphase standard turbulence approach. It represents the extension of the single phase  $k - \varepsilon$  model and is used when the secondary phase concentrations are diluted on primary phase.  $k$  and  $\varepsilon$  equations describing this model are as follows (Eqs. 10 and 11):

$$\frac{\partial}{\partial t} (\rho_L \alpha_L k_L) + \nabla \cdot (\rho_L \alpha_L \vec{U}_L k_L) = \nabla \cdot \left( \alpha_L \frac{\mu_{t,L} \nabla k_L}{\sigma k} \right) + \alpha_L G_{k,L} - \alpha_L \rho_L \varepsilon_L + \alpha_L \rho_L \Pi_{K,L} \quad (10)$$

$$\begin{aligned} & \frac{\partial}{\partial t} (\rho_L \alpha_L k_L \varepsilon_L) + \nabla \cdot (\rho_L \alpha_L \vec{U}_L \varepsilon_L) \\ &= \nabla \cdot \left( \alpha_L \frac{\mu_{t,L} \nabla \varepsilon_L}{\sigma \varepsilon} \right) + \alpha_L \frac{\varepsilon_L}{k_L} (C_{1\varepsilon} G_{k,L} - C_{2\varepsilon} \rho_L \varepsilon_L) + \alpha_L \rho_L \Pi_{\varepsilon,L} \end{aligned} \quad (11)$$

In these equations,  $G_{k,L}$  represents the generation of turbulent kinetic energy,  $k_L$  of the liquid phase due to mean velocity gradients,  $\varepsilon_L$  is the turbulent dissipation energy.  $\Pi_{K,L}$  and  $\Pi_{\varepsilon,L}$  represent the

influence of the dispersed phase in the continuous phase, respectively [28].

The turbulent viscosity  $\mu_{t,L}$ , is calculated from (Eq. 12):

$$\mu_{t,L} = \rho_L C_\mu \frac{k_L^2}{\varepsilon_L} \quad (12)$$

The values of the constants used in this experiment were  $C_{1\varepsilon}$ : 1.44,  $C_{2\varepsilon}$ : 1.92,  $C_\mu$ : 0.09  $\sigma_k$ : 1.00 and  $\sigma_\varepsilon$ : 1.30.  $\sigma_k$  and  $\sigma_\varepsilon$  represent turbulent Prandtl number for  $k$  and  $\varepsilon$ , respectively [28].

### Population balance model for bubble distributions

The discrete method [29-31] is used herein to solve the population balance equations. The bubble population is discretized into a finite number of intervals of bubble diameters. The population balance equations (Eq. 13) for different bubble classes can be written as [32-34]:

$$\frac{\partial}{\partial t} (\rho_G n_i) + \nabla \cdot (\rho_G \vec{U}_G n_i) = \rho_G (\Gamma_{B_{iC}} - \Gamma_{D_{iC}} + \Gamma_{B_{iB}} - \Gamma_{D_{iB}}) \quad (13)$$

Where  $n_i$  is the number of bubbles per class  $i$ ,  $\Gamma_{B_{iC}}$  and  $\Gamma_{B_{iB}}$  are birth rates due to coalescence and breakage, respectively,  $\Gamma_{D_{iC}}$  and  $\Gamma_{D_{iB}}$  are the death rates.

The terms of breakage and coalescence are (Eqs. 14-17):

$$\Gamma_{B_{iC}} = \frac{1}{2} \int_0^v a(v-v', v) n(v-v', t) n(v', t) dv' \quad (14)$$

$$\Gamma_{D_{iC}} = n(v) \int_0^\infty a(v, v') n(v', t) n(v', t) dv' \quad (15)$$

$$\Gamma_{B_{iB}} = \int_{\Omega_v} p g(v') \beta(v|v') n(v', t) dv' \quad (16)$$

$$\Gamma_{D_{iB}} = g(v) n(v, t) \quad (17)$$

$a(v, v')$  is the coalescence rate between bubbles of size  $v$  and  $v'$ ;  $g(v)$  is the breakup rate of bubbles of size  $v$ ;  $g(v')$ , is the breakup frequency of bubble  $v'$  and  $\beta(v | v')$  is the probability density function of bubbles broken from the volume  $v'$  in a bubble of volume  $v$ .

The bubble breakup is analyzed in terms of bubbles interaction with turbulent eddies. These turbulent eddies increase the bubble surface energy to cause deformation. The breakup occurs if the increase in the surface energy reaches a critical value. The break up rate (Eqs. 18-20) is defined as [3]:

$$g(v')\beta(v|v') = k \int_{\xi_{min}}^1 \frac{(1+\xi)^2}{\xi^{11/3}} \exp(-b\xi^{-11/3}) d\xi \quad (18)$$

$$k = 0.9238 \varepsilon^{1/3} d^{-2/3} \alpha \quad (19)$$

$$b = 12 \left( f^{2/3} (1-f)^{2/3} - 1 \right) \sigma \rho^{-1} \varepsilon^{-2/3} d^{-5/3} \quad (20)$$

Where  $d$  is the bubble diameter,  $\xi$  is the dimensionless eddy size,  $f$  is the breakage frequency. The bubble coalescence is modeled by considering the bubble collision due to turbulence, buoyancy and laminar shear. The coalescence rate (Eq. 21) is defined as the product of the collision frequency  $\omega_{ag}(v_i, v_j)$  and coalescence probability  $P_{ag}(v_i, v_j)$  and is defined as [3]:

$$a(v, v') = \omega_{ag}(v_i, v_j) P_{ag}(v_i, v_j) \quad (21)$$

The collision frequency is defined as (Eq. 22):

$$\omega_{ag}(v_i, v_j) = \frac{\pi}{4} (d_i^2 + d_j^2) n_i n_j \bar{u}_{ij} \quad (22)$$

Where  $\bar{u}_{ij}$  is the characteristic collision velocity of two bubbles with diameter  $d_i$  and  $d_j$  and bubble density  $n_i$  and  $n_j$  (Eq. 23):

$$P_{ag}(v_i, v_j) = \exp \left( -c_1 \frac{[0.75(1+x_{ij}^2)(1+x_{ij}^3)]^{1/2} \left( \frac{\rho_l d_i (\bar{u}_i^2 + \bar{u}_j^2)^{1/2}}{\sigma} \right)^{1/2}}{\left( \frac{\rho_2}{\rho_1 + 0.5} \right)^{1/2} 1 + x_{ij}^3} \right) \quad (23)$$

Where  $c_1$  is a first order constant,  $x_{ij} = d_i/d_j \rho_1$  and  $\rho_2$  the densities of primary and secondary phase.

The number of bubbles per class  $i$ ,  $n_i$  is related to the gas phase volume fraction as follows (Eq. 24):

$$n_i v_i = \alpha_i \quad (24)$$

The sum of the volume fractions of each group of bubbles is equal to the volume fraction of the dispersed phase (Eq. 25):

$$\sum_i \alpha_i = \alpha_G \quad (25)$$

The volume fraction of each group sizes is expressed in terms of the total fraction of the dispersed phase (Eq. 26):

$$f_i = \frac{\alpha_i}{\alpha_G} \quad (26)$$

Therefore, including Eq. (26) in Eq. (13), is (Eq. 27):

$$\frac{\partial}{\partial t} (\alpha_G \rho_G f_i) + \nabla \cdot (\alpha_G \rho_G \vec{U}_G f_i) = \rho_G v_i (B_{iC} - D_{iC} + B_{iB} - D_{iB}) \quad (27)$$

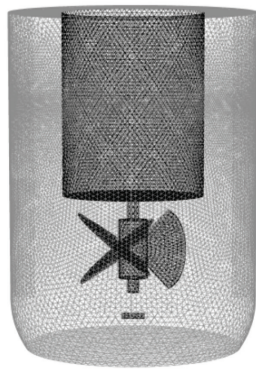
The Sauter diameter  $d_{32}$  is used to fit the population balance equations with the bioreactor hydrodynamics (Eq. 28):

$$d_{32} = \frac{\sum_i n_i d_i^3}{\sum_i n_i d_i^2} \quad (28)$$

### Mesh processing and numerical technique

A fine 3D mesh (Figure 1) is composed for tetrahedral cells with 1000 computational k cells for the Spin Filter Bioreactor.





**Figure 1** Mesh generation for the Spin Filter Bioreactor

The finite volume technique implemented in the CFD code Ansys Fluent 13.0 Software was used to convert the Navier- Stokes equations into algebraic equations which can be solved numerically. Tank walls, stirrer surfaces and baffles are treated with no slip conditions and standard wall functions.

The gas flow rate at the cylinder micro-sparger was defined via inlet-velocity type boundary condition with gas volume fraction equal to unity. MRF model was applied for the impeller (Pitched Blade) and Spin Filter device. PC SIMPLE algorithm was used for solving the partial differential equations. The second order upwind scheme was applied for the spatial terms. It was assumed that the solution converges when the scaled residuals remain with values smaller than  $10^{-5}$  and when the pseudo-regime for hold-up is reached [9, 10]. The size of the bubbles was set by the discretization scheme based on the geometric ratio [9]. The size of the bubbles for the Spin Filter Bioreactor was assumed from 75 to 2000  $\mu\text{m}$  in diameter. 13 size classes were used to discretize the population balance equations [10], who analyzed hydrodynamics of a propeller type stirrer and found satisfactory results using the same classifiers. Power input  $P$  (Eq. 29) is calculated using torque  $M$  of the impeller (in Ansys fluent called the Moment Center) [7]:

$$P = 2\pi N_i M \quad (29)$$

### Experimental measurements

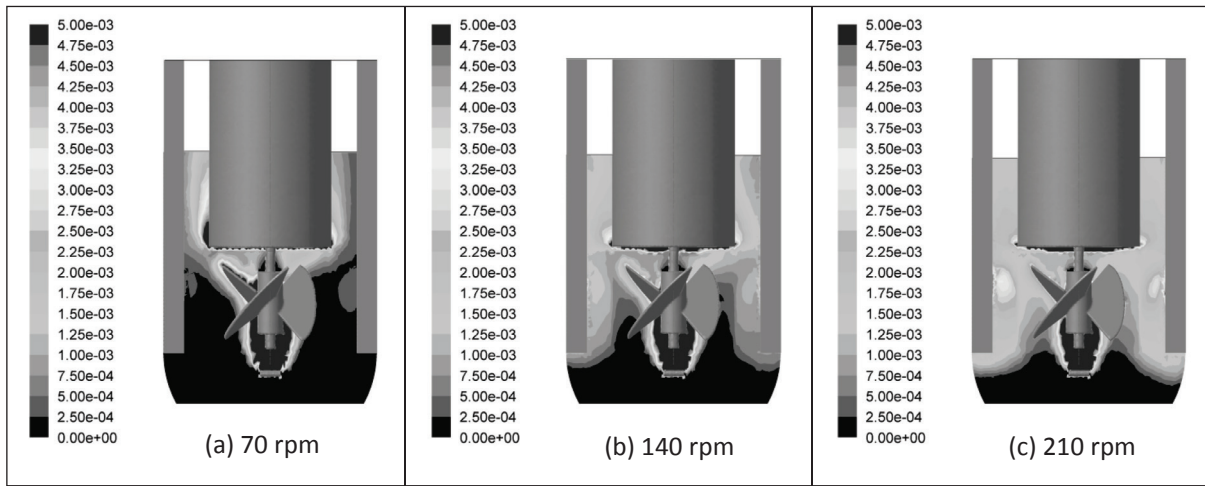
Experimental  $k_L a$  measurements were performed applying the  $\text{N}_2$ -stripping approach in aqueous medium. Time courses of increasing dissolved oxygen levels were monitored via an  $\text{O}_2$ -probe (Mettler Toledo, Germany).  $k_L a$  estimations (Eq. 30) resulted from non-linear parameter fitting using equation [13]:

$$k_L a = - \frac{\ln \left( \frac{C_{O_2}^* - C_{O_2,i-1}}{C_{O_2}^* - C_{O_2,i}} \right)}{t_i - t_{i-1}} \quad (30)$$

with  $i$  coding for subsequent time points  $t$  and \* indicating the saturating dissolved oxygen levels  $C_{O_2}$ . Time series of dissolved oxygen were corrected with respect to the delayed probe responses which had been identified as  $\sim 28$  seconds, relating to  $\tau = 0.035$  [1/s].

### Results

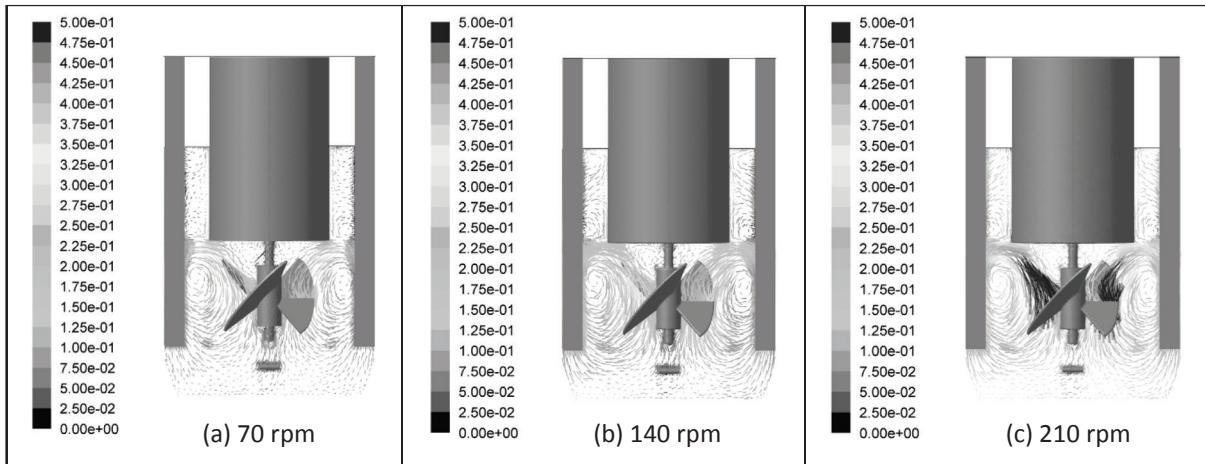
The main propose of this work was to study the gas-liquid mass transfer hydrodynamics using a Spin Filter bioreactor. For that reason detailed understanding of hydrodynamic behavior can be useful not only for identifying mass transfer limitations but also for finding design requirements that must be implemented to optimize an aerobic bioprocessing. The simulated operating conditions are based on typical values of plant cell cultivations. Special emphasis was given to the evaluation of local distributions. Figure 2 shows the CFD air volume fractions of the Spin Filter bioreactor operated at different impeller speed. It can be seen that relatively low air dispersion occurs in the bioreactor when it was operated at 70 rpm. Poor air volume fractions are caused by low centrifugal forces. Obviously, these centrifugal forces could not overcome the air buoyancy [13]. Contrary, air gradients are minimized when the stirrer tank is operated at 140 and 210 rpm.



**Figure 2** Air volume fraction [-] contours calculated for (a) 70, (b) 140 and (c) 210 rpm

Figure 3 shows the velocity vectors calculated for the Spin Filter bioreactor operated at: (a) 70 rpm, (b) 140 rpm and (c) 210 rpm. Similar results were demonstrated in all cases. The pitched blade geometry and bottom Spin filter pump the fluid slightly downwards around the impeller discharge region. Consequently, high mass transfer regions were generated in all the operating conditions tested by CFD. Noteworthy,

similar results were found by [13] who compared the gas-liquid hydrodynamics of a Rushton turbine with a new pitched blade impeller. It is observed that highest velocities are found in striking distance to the rotating Pitched Blade and Spin Filter. Moreover, the mean velocity decreases gradually away from the Impeller and becomes very low at the bottom and at the top of the bioreactor.



**Figure 3** Liquid phase velocity  $[V/V_{tip}]$  vectors [m/s] calculated for (a) 70, (b) 140 and (c) 210 rpm

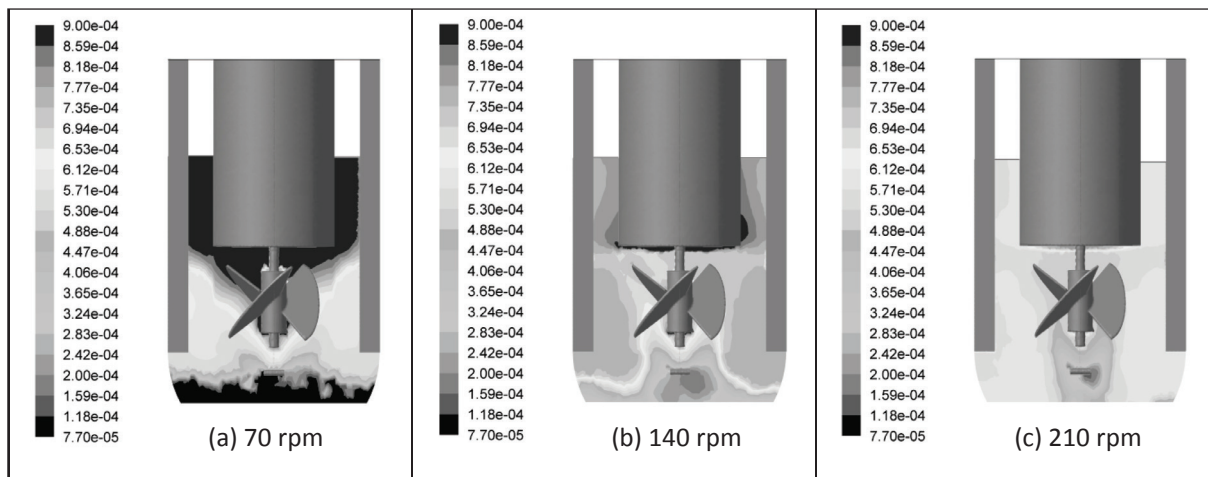
In aerobic fermentations, air flows continuously through the stirred tank reactor. The bubble size distribution results from physical interactions imposed on uprising bubbles and considers mechanisms



such as coalescence and breakage. These phenomena together with hydrodynamics, trigger the formation of dissolved oxygen and trace gases gradients of which can affect productivity in aerobic plant cell cultures. For that reason, when breakage phenomenon prevails, bubble size decreases, the interfacial area for mass transfer thereof is increased and consequently, the oxygen transfer is promoted. On the other hand, large bubbles generated by coalescence are characterized by higher rising velocities and short residence times. Thereby, bubbles cannot be uniformly dispersed for the agitation system. The most relevant parameter for analyzing these hydrodynamic mechanisms is the Sauter mean diameter. It can be interpreted as an integral parameter, summarizing all individual impacts affecting the bubble sizes and their distribution in one single value [13]. It is estimated from CFD-

based hydrodynamics and population balance models.

Figure 4 shows the Sauter mean diameter contours of the Spin Filter bioreactor operated at different impeller speeds: (a) 70 rpm, (b) 140 rpm and (c) 210 rpm. Interestingly, lowest values of  $5\text{e-}4\text{ m}$  were found when Spin Filter was operated at 210 rpm. These small Sauter diameters were dispersed homogeneously when relatively high local bubble breakage and downward pumping rates take place. This finding is in agreement with reports of [10], who analyzed hydrodynamics of a propeller type stirrer. Largest mean Sauter diameters of  $9\text{e-}4\text{ m}$  were simulated when 70 rpm was used as stirring velocity. These coalescing zones are caused by low mixing. Considering simulated mass transfer, these zones are candidates for poor oxygen mass transfer levels.



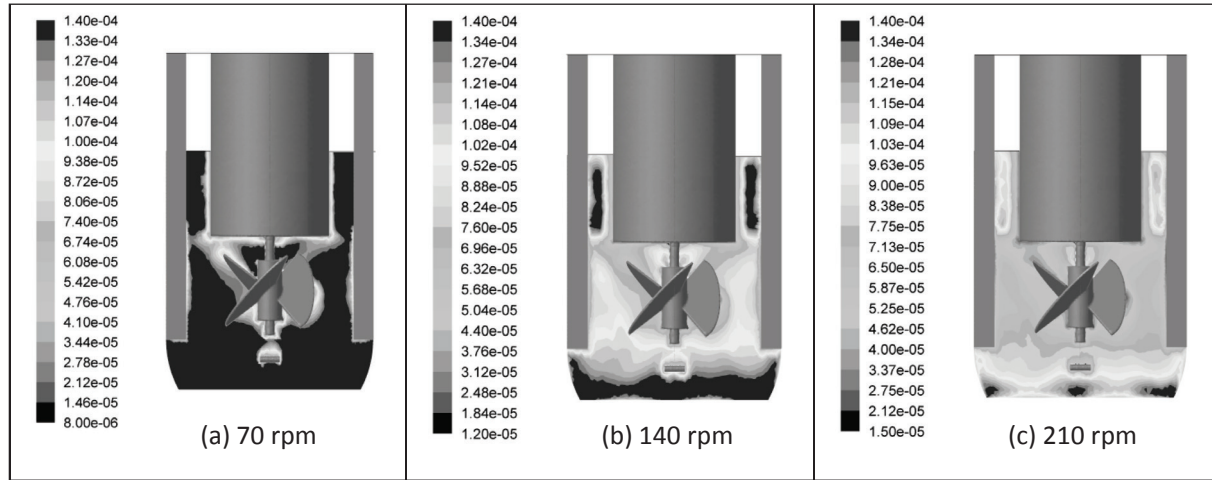
**Figure 4** Sauter diameter contours [m] calculated for (a) 70, (b) 140 and (c) 210 rpm

Therefore, this result shows that 70 rpm is not a good operational condition for the Spin Filter because of its low power input (0.03 W) can generate poor mixing and undesired large bubble sizes. Still, 210 rpm seems to be the best parameter for the Spin Filter device in terms of Sauter diameter, but the high power input required (0.77 W) can be a disadvantage in large

scale prototypes. Based on this information, a new prototype of bioreactor should be designed to disperse average bubble sizes of  $5\text{e-}4\text{ m}$  but it is important to bear in mind the constrain of avoiding large power input requirements. However, the cell damage theory of Kolmogorov suggests that any biological entity will damage if its size is greater than the Kolmogorov diameter

scale [14]. Figure 5 shows that Kolmogorov diameters were calculated as 140, 70 and 45  $\mu\text{m}$  for 70, 140 and 210 rpm, respectively. Considering that average size of a plant cell is 50  $\mu\text{m}$ , cell damage should be expected if the Spin Filter device is operated at 210 rpm. Interestingly,

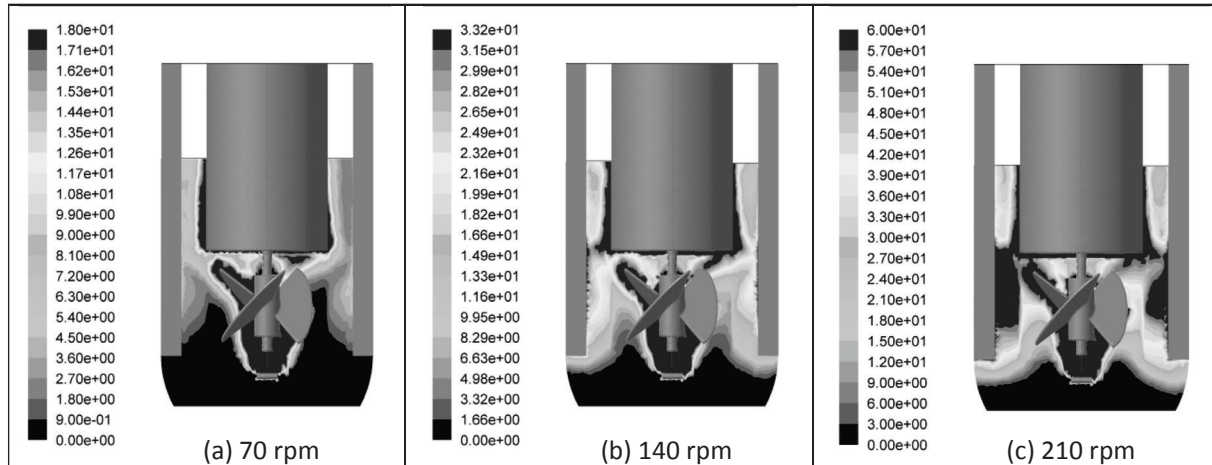
acceptable gas-liquid hydrodynamics were found by reducing 69 % the impeller power input (0.23 W) when CFD simulations were performed at 140 rpm. In terms of saving energy and cellular constraints, 170 rpm proved to be the best operational condition.



**Figure 5** Kolmogorov length scales  $\lambda_k$  calculated for (a) 70, (b) 140 and (c) 210 rpm

Maintaining an adequate oxygen supply to aerobic cell cultures has been a long-standing problem in fermentation technology. This problem is particularly amplified in high cell density cultures, in which insufficient oxygen transfer rates limit cell growth and ultimately process productivity [35].

$k_L a$  values (Figure 6) are considered as the principal criterion to analyze the gas/liquid mass transfer. In this work, Higbie's penetration theory is used for simulating  $k_L a$  from CFD. These values are obtained by the product of liquid mass transfer  $k_L$  and interfacial area  $a$  [34]. Interfacial area is expressed as a function of the local gas fraction and the local Sauter diameter.



**Figure 6** mass transfer coefficient  $[1/h]$  calculated for (a) 70, (b) 140 and (c) 210 rpm

Given the biochemical constraint that cell cultivations require optimum dissolved oxygen levels for growth ensuring a minimum of 5 % (at atmospheric conditions) [36], sufficient oxygen transfer rates are obviously only achieved if values reach fairly high levels [13]. Simulating the Spin Filter Bioreactor, oxygen mass transfer, expressed by (Figure 6), was found to be about 3 times higher with 210 rpm than values obtained at 70 rpm. At the given operational conditions (70 rpm), the Spin Filter system reached only an integral of 18.0 1/h while increasing the power input the values attained 33.2 and 60.0 1/h at 140 and 210 rpm, respectively. The latter is the consequence of the improved gas-liquid mass transfer which ensures the formation of uniform bubble sizes, generally caused by the hydrodynamics. In terms of saving energy and cellular constraints, 170 rpm remained to be the best operating condition for the Spin Filter bioreactor.

Moreover, experimental measurements were tested using the operating conditions of the CFD simulations. Experimental tests showed values of 20.0, 35.1 and 63.3 1/h for 70, 140 and 210 rpm, respectively, that fit very well to the simulations. The very good agreement is qualified as a proving for the accurate of coupling of the population balance models and gas-liquid hydrodynamics terms used in CFD.

## Conclusions

Numerical results from gas-liquid mass transfer in a Spin Filter Bioreactor are analyzed using CFD. Comparing CFD simulations with experimental measurements show that good agreement is achieved. Motivated by these simulated and experimental results CFD simulations are qualified as a very promising not only for predicting gas-liquid hydrodynamics but also for finding design requirements that must be implemented to optimize an aerobic bioprocessing especially useful for plant cell culture applications which are characterized by the constrain of achieving relatively high mass transfer conditions and avoiding cellular damage

due to hydrodynamic conditions. Gas-liquid mass transfer, bubble size diameter and Kolmogorov length scales can be treated as main criteria for designing a new stirred tank bioreactor applied to plant cell cultures.

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