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# Interplanetary Shock Parameters during Solar Activity Maximum (2000) and Minimum (1995-1996)

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Interplanetary shock parameters are analyzed for solar maximum (year 2000) and solar minimum (years 1995-1996) activity. Fast forward shocks are the most usual type of shock observed in the interplanetary medium near Earth's orbit, and they are 88% of the identified shocks in 2000 and 60% in 1995-1996. Average plasma and magnetic field parameters for upstream and downstream sides of the shocks were calculated, and the parameter variations through the shock were determined. Applications of the Rankine-Hugoniot equations were made, obtaining shock speeds and Alfvénic Mach number. Static and dynamic pressures variations through the shocks were also calculated. Every parameter have larger variation through the shock in solar maximum than in solar minimum, with exception of the proton density. The intensity of shocks relative to the interplanetary medium, quantified by the Alfvénic Mach Number, is observed to be similar in solar maximum and minimum. It could be explained because, during solar maximum, in despite of the higher shock speeds, the Alfvénic speed of the interplanetary medium is higher than in solar minimum.

## I Introduction

The interplanetary medium has a very low particle density, of about  $5\text{ cm}^{-3}$ , and it has a collisional mean free path of about 1 Astronomical Unit(AU) or  $1.5 \cdot 10^8\text{ km}$  [1]. Thus the occurrence of particle collisions is very sporadic. However, the interplanetary space is transiently disturbed by collisionless shock waves. In these shocks, the role that particle collisions make in ordinary shocks, is performed by long range Coulombian forces [1-4]. These Coulombian forces can have this very important role because the interplanetary medium is ceaseless permeated by the solar wind, a plasma resulting of the solar corona expansion and that carries with it the solar magnetic field through the solar system [1,5]

Shock waves detected near the Earth's orbit, 1 AU, are mainly caused by interplanetary remnants of solar ejecta, although some types of shocks could be generated by interaction regions between slow and high speed solar wind streams [5]. Solar ejecta are coronal material expelled from the Sun, the coronal mass ejections [1,6-10] which propagate through the interplanetary medium. A shock occurs when the relative speed between a high speed stream and the background solar wind is higher than the characteristic speed of the medium (Alfvénic, magnetossonic)[1,2,3,5].

Interplanetary structures can be geoeffective, causing magnetic storms, especially if an intense and long duration southward component of the magnetic field is present

[6,11,12]. Because shock waves have a larger spatial extent than the interplanetary structures, it is usual that spacecrafts near Earth's orbit measure only the shock. However, the shock itself can have geoeffective effects, especially sudden impulses - increase in the H component of the geomagnetic field observed in low and mid latitudes stations, due to the intensification of Chapman-Ferraro current in the magnetopause, and magnetohydrodynamics waves and micropulsations propagation inside Earth's magnetosphere [1,13].

In this work we are studying interplanetary shock parameters during high and low solar activity conditions. The years of 2000 (solar maximum) and solar minimum (1995-1996) were selected for analysis. Plasma and magnetic field parameter variations through the shocks were calculated, and derived quantities for shocks - shock speed, Alfvénic Mach Number, magnetic field and plasma compression and plasma and magnetic field pressures were calculated in order to evaluate the differences in these shock parameters during solar activity maximum and minimum.

## II Data

Interplanetary magnetic field and plasma high resolution data used in this study were obtained by sensors onboard the WIND (60 and 90 s, respectively) spacecraft [14] in solar minimum and the ACE (16 and 64 s respectively) space-

craft [15] in solar maximum. We have analyzed 15 fast forward shocks in 1995-1996 and 50 fast forward shocks in 2000. For 6 events during 2000, plasma sensor onboard ACE was saturated, and plasma data were obtained from Proton Monitor onboard the SOHO spacecraft [16]. All data were obtained via internet, through the International Solar-Terrestrial Physics Program data services.

### III Results and discussion

Figure 1 shows an example of a fast forward interplanetary shock on July 10th 2000. From the top to the bottom, panels are: proton temperature  $T_p$  (K), speed  $V_p$  (km/s) and density  $N_p$  ( $\text{cm}^{-3}$ ), total magnetic field  $B_t$  (nT), north-south magnetic field component  $B_z$  (nT) and the SYM geomagnetic index (nT). The shock is indicated by the letter "S" and by the continuous line. It is observed that plasma parameters

and total magnetic field jump through the shock, creating a discontinuity. Less than one hour after the shock, a sudden impulse (SI in the Fig. 1) is observed in the SYM index, indicating a H geomagnetic field component increase, corresponding to the Earth's magnetosphere compression by the shock and the intensification of the Chapman-Ferraro current in the magnetopause.

In order to calculate the plasma and  $B_t$  variation through the shock, three time windows were defined, each one of about 10 min. The boundaries of these time windows are limited by the dotted lines in Fig. 1. The central time window corresponds to the shock itself. The lateral time windows correspond to the upstream and downstream sides of shock [5] and are labeled in Fig. 1 by the letters "U" and "D" respectively. Average parameters were calculated for the interval limited by upstream and downstream time windows, and the difference between these averages is quantified as the parameter variation through the shock.

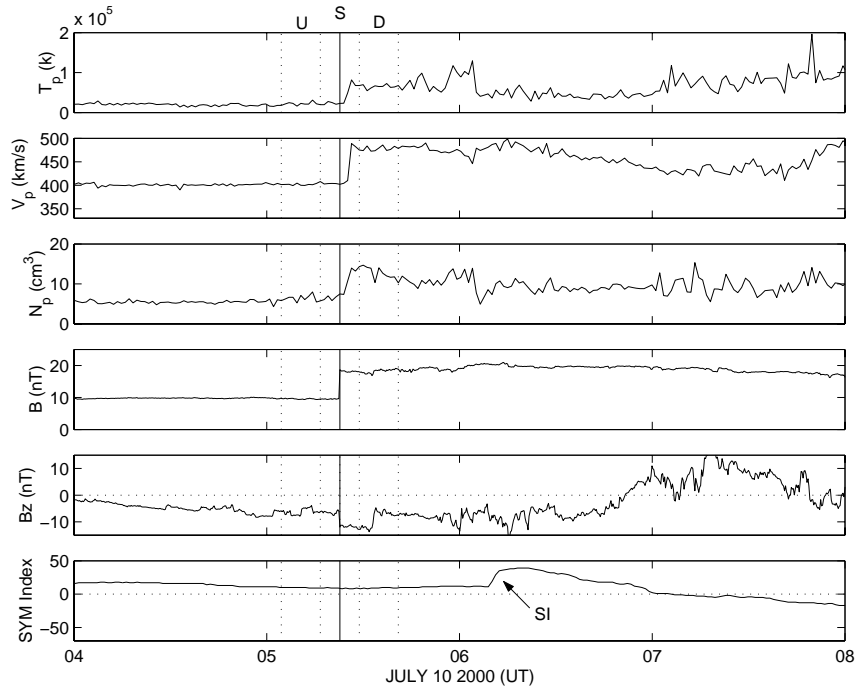


Figure 1. Example of a fast forward shock observed on 10th July 2000. Panels are proton temperature, speed and density, total magnetic field, north-south magnetic field component and the geomagnetic SYM index. The continuous line indicate the shock and the dashed lines indicates the upstream, shock and downstream time windows (see text).

During solar maximum and minimum a total of 57 and 25 shocks were identified, respectively. This difference occurs because during high solar activity, a larger number of solar transients are expelled from the solar corona [6,8,10] than during low solar activity. These shocks were classified analyzing the parameter variations, in forward (fast and slow) and in reverses (fast and slow). The parameter variations through every type of shock are shown in a sketch in Fig. 2.

Figure 2 shows the typical profiles of proton speed, temperature and density, and total magnetic field variations through the shocks. Parameter variations for fast forward and slow forward shocks are shown in upper panels, left and right, respectively. Fast and slow reverse shocks parameter variations are shown in lower panels, left and right, respectively. A forward shock is a shock that moves away from the Sun, relatively to the solar wind; a reverse shock moves toward the Sun relatively to the solar wind. However, be-

cause solar wind is moving supersonically away from the Sun, both types of shocks are moving away from the Sun, relatively to the Sun itself and any satellite that measures the parameters [5]. A shock is fast when its relative speed

to the solar wind is higher than the fast magnetosonic wave speed; a shock is slow when its relative speed is higher than the slow magnetosonic wave speed.

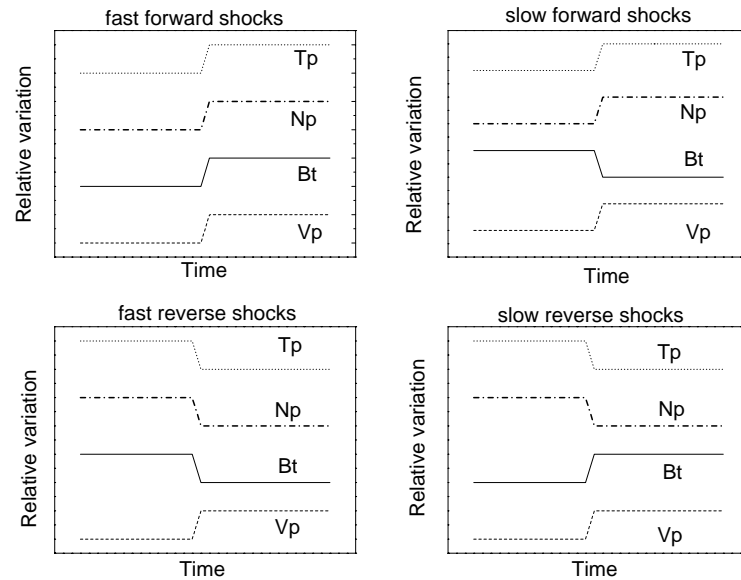


Figure 2. Sketch of parameter variations:  $T_p$ ,  $N_p$ ,  $V_p$  and  $B_t$ , for the four types of interplanetary shocks. Upper left panel, fast forward, right, slow forward shocks. Lower left panel, fast reverse, right, slow reverse shocks.

Fast forward shocks show positive jumps in all the variables,  $V_p$ ,  $T_p$ ,  $N_p$  and  $B_t$ . Slow forward shocks show positive jumps in  $V_p$ ,  $T_p$  and  $N_p$ , but negative in  $B_t$ , because slow magnetosonic waves have plasma and magnetic field variations anticorrelated [3]. Reverse shocks present positive jumps in  $V_p$ , because solar wind is dragging the shock. For both slow and fast reverse shocks,  $N_p$  and  $T_p$  have negative jumps. For fast reverse shocks,  $B_t$  has negative jumps, whereas for slow reverse shocks  $B_t$  has positive jumps (anticorrelated to plasma jump).

Figure 3 shows bar graphs expressing the percentage of every type of shock in solar maximum (left) and in solar minimum (right). It is seen in Fig. 3 that the large majority of shocks are of the fast forward type, in solar maximum (88% or 50 shocks of 57) and in solar minimum (60% or 15 shocks of 25). This distribution occurs because fast interplanetary ejecta are the main driver of shocks near Earth's orbit. It is also observed that in solar maximum the number of fast forward shocks is about ten times higher than in solar minimum, 50/year in maximum against 7.5/year in solar minimum; a proportion ten times higher in maximum was expected because coronal mass ejections rate is about ten times higher in solar maximum than in solar minimum [8].

Slow shocks (forward and reverse) occur in smaller numbers, and they are relatively more abundant in solar minimum than in solar maximum. Generally slow shocks occur near the stream interface, which are barriers to the flow and contribute to the plasma and magnetic field draping [5].

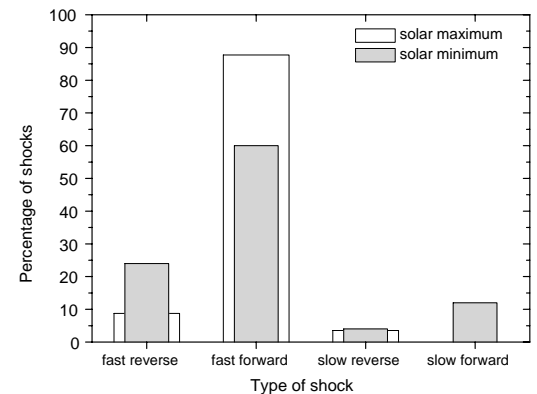


Figure 3. Bar graph distribution of types of interplanetary shocks in solar maximum (white bars) and in solar minimum (gray bars).

Fast reverse shocks are more abundant than the slow ones and are associated to corrotating streams [5]. In Fig.3 it is seen that there are relatively a larger number of reverse shocks in solar minimum (24%) than in solar maximum (9%). This result is reflecting the different conditions of solar activity and interplanetary medium during the solar cycle, because the higher occurrence of corrotating streams, in the descending phase and in solar minimum of solar cycle [6]. These corrotating streams are high speed streams, emitted from coronal holes. During solar maximum coronal holes are limited to high solar latitudes, whereas in the descending phase and solar minimum they are extending over low solar latitudes. These high speed streams from coronal

holes are long duration phenomena, during several solar rotations (27 days) and reaching the Earth recursively at periods near a solar rotation [6]. The high speed streams interact with the heliospheric current sheet, which is characterized by slow speed and high density streams, and their interaction creates the so-called corrotating interaction regions [6], that compress the interplanetary magnetic field, intensifying it. This interaction region is bounded by forward and reverse shocks. However, at 1 AU this CIR is not totally developed, and the so-called proto-CIRS are observed [6].

The reverse shocks observed in this work are probably related to the interaction regions. Fast forward shocks are mainly caused by coronal mass ejections, but it is possible that some fast forward shocks, especially in solar minimum,

are caused by interaction regions.

In the remaining of this paper fast forward shocks are selected to analyze the plasma and magnetic field parameter variations through the shock and the differences between solar maximum and solar minimum.

Figure 4 shows the averages of Bt, Vp, Tp and Np, respectively, for upstream and downstream sides of shocks. The continuous curve is the step-like variations for solar maximum and the dotted line for solar minimum. The time axis is in arbitrary units. Upstream averages can be considered as representative of the background solar wind conditions, whereas downstream average values are representative of the solar wind disturbed by shocks.

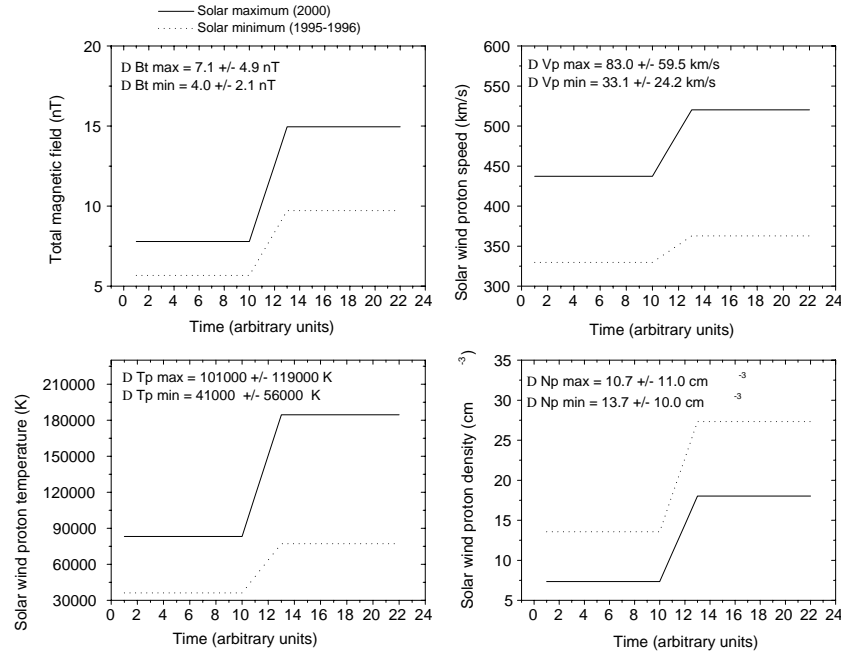


Figure 4. Step-like parameter variations through interplanetary shocks. Upper left panel, Bt variation and right, Vp variation. Lower left panel, Tp variation and, right Np variation. Continuous lines are for solar maximum and dotted line for solar minimum.

It is seen that upstream and downstream parameter averages of Bt, Vp and Tp are larger in solar maximum than in solar minimum, whereas for Np the higher values are observed in solar minimum. These averages are similar for the whole period, as seen in Table I, for 1995-1996 and 2000. These results can be explained because in solar minimum, the heliospheric plasma sheet/heliospheric current sheet is more stable, located near low solar latitudes and near to Earth; then the interplanetary medium near Earth has high

values of solar density and low speeds/temperature. In solar maximum, the heliospheric current sheet has a waving variation, and alternatively the interplanetary medium near Earth has periods with high and low density, that causes average density in solar maximum to be lower than in solar minimum [17]. Thus interplanetary shocks in solar minimum are propagating in a medium with higher densities than in solar maximum.

Table I Average solar wind parameters for solar maximum and minimum.

Parameter	Solar minimum 1995-1996	Solar maximum 2000
Vp	425.0 ± 95.0 km/s	455.0 ± 110.0 km/s
Tp	61000 ± 63000 K	76000 ± 91000 K
Np	9.5 ± 6.1 cm <sup>-3</sup>	7.7 ± 6.3 cm <sup>-3</sup>
Bt	5.4 ± 2.3 nT	7.1 ± 3.6 nT

During solar maximum the Sun is more active, launching more ejecta with higher magnetic field intensity and solar wind speed, what could justify the higher values of these parameters in solar maximum [18]. However, plasma and magnetic field parameters show a solar cycle variation superimposed with smaller-scale fluctuations and in each solar cycle the form of variation seems to be slightly different [18]. Particularly, total magnetic field seems to have a variation in phase with sunspot cycle, but density has an oscillation of around 5 years [20].

Density variation through shocks is slightly higher in solar minimum ( $13.7 \pm 10.0 \text{ cm}^3$ ) than in solar maximum ( $10.7 \pm 11.0 \text{ cm}^3$ ) but the difference is not very large. On the other hand, the proton speed and temperature, and total magnetic field averages are much higher in solar maximum than in solar minimum. Especially, the speed variation is on average more than two times higher in solar maximum than in solar minimum ( $83.0 \pm 59.0 \text{ km/s}$  against  $33 \pm 24.2 \text{ km/s}$ ) as a consequence of the fact that in solar maximum, solar ejecta and their interplanetary remnants are more intense and with higher speeds [10].

### Rankine-Hugoniot equations

Every type of magnetohydrodynamics shocks should observe the Rankine-Hugoniot equations [1,2,3,5], which are fundamental physical relationships for a plane surface of discontinuity (shock), through of it physical fields jump from the upstream to the downstream sides. These equations express the mass, normal momentum flux, tangential momentum flux, energy and magnetic flux conservations. Burlaga [5] presents these equations relative to a reference system with origin at the shock. It is supposed that the upstream and downstream speeds are radials, so the shock speed can be calculated, relative to the Sun, in eq.(1):

$$U = \frac{N_2 V_2 - N_1 V_1}{N_2 - N_1} \quad (1)$$

Where  $N_1$ ,  $N_2$ ,  $V_1$ ,  $V_2$  are average density and speed in the upstream and downstream sides, respectively. With eq. (1), the shock speed was calculated. The relative distribution (in percentage) of shock speeds are shown in upper panel of Fig. 5 for solar maximum (left) and solar minimum (right). The average shock speeds are higher for solar maximum than for solar minimum, as expected, with significant differences ( $594.4 \pm 192.0 \text{ km/s}$  in maximum against  $394.0 \pm 46.5 \text{ km/s}$  in minimum). During solar minimum the distribution of speeds is more concentrated, between 300-500 km/s, with the majority of shocks occurring between 350-400 km/s (53% of the events). During solar maximum, the distribution of shocks has a large spread, with events with shock speed around or larger than 1000 km/s.

The ratio between the flow speed and the characteristic speed of the medium is called the Mach number. For an interplanetary shock, its Mach number will be given in terms of the ratio of the relative speed between shock and the solar wind and the characteristic speed (magnetosonic

or Alfvénic). In this work the Alfvénic Mach number is calculated for the shocks studied. The Alfvén speed for the solar wind can be calculated using the parameters of the upstream side in eq. (2):

$$V_A = \frac{B_1}{(\mu_0 \rho_1)^{1/2}} \quad (2)$$

In eq. 2,  $B_1$  and  $\rho_1$  are the total magnetic field and mass density in the upstream side ( $\rho_1 = n_1 m^+$ ) and  $\mu_0$  is the magnetic permeability. The Alfvénic Mach number can then be calculated by eq. (3):

$$M_A = \frac{|U - V_1|}{V_A} \quad (3)$$

where  $U$  is the shock speed (equation 1) and  $V_1$  is the upstream speed.

In Fig. 5, in the intermediate panels, the Alfvénic Mach Number is shown for solar maximum, at left and for solar minimum, at right. At the solar system, shocks can be found to have until a Mach number of 20 [1]. In the present study it was observed that Alfvénic Mach number of shocks are in the range 2-3, with some extremes until 7-8.

It is seen that the average Mach numbers are very similar in solar minimum and in solar maximum, in despite of shock speeds higher during solar maximum. This result could be explained because the Alfvén speed depends on the density and magnetic field of the medium. Proton density is higher in solar minimum than in solar maximum, whereas magnetic field is greater in solar maximum, and the resulting Alfvén speed should be lower in solar minimum. Average values for upstream conditions for Alfvénic speed are  $69.6 \pm 26.2 \text{ km/s}$  in solar maximum and  $34.3 \pm 22.0 \text{ km/s}$  in solar minimum. Thus in solar minimum, the Alfvén speeds are on average 2 times lower than in solar maximum, and shocks with lower speeds than shocks in solar maximum will have Alfvénic Mach numbers higher or similar equal to faster shocks at solar maximum. These results show that shock strength, relatively to the solar wind, is similar in both solar activity periods, because the propagation medium is different and the variation in the Alfvénic speed compensates the shock speeds variation, for the period studied.

Intermediate lower panels in Fig. 5 show the total magnetic field ratio ( $(B_2)/(B_1)$ ). The compression ratio distribution and the average values are very similar for both solar minimum and maximum. It is also seen that the magnetic compression ratio is always higher than 1, and lower than 4. The value of 4 for compression is the theoretical finite compression limit in the case of high Mach numbers, for a monoatomic gas [1]. However, for density compression ratio, shown in the last panel in Figure 5, values of compression higher than 4 are seen in about 10% of shocks in solar maximum. The distributions are similar, with average density compression ratio higher in solar maximum ( $2.60 \pm 1.10$ ) than in solar minimum ( $2.10 \pm 0.62$ ). During solar minimum all shocks have density compression ratio lower than 4.0. The explanation for the occurrence of some shocks with higher compression than the limit of 4 should

be because this limit was derived for shocks exactly perpendicular [1], and in our dataset is possible to have a distribution of shocks between parallel and perpendicular types. Furthermore, the compression ratio of magnetic field and

plasma depends of the way as the shock heats the plasma and individual events could be different of the adiabatic approximation considered in obtaining the expression for the compression ratio [1].

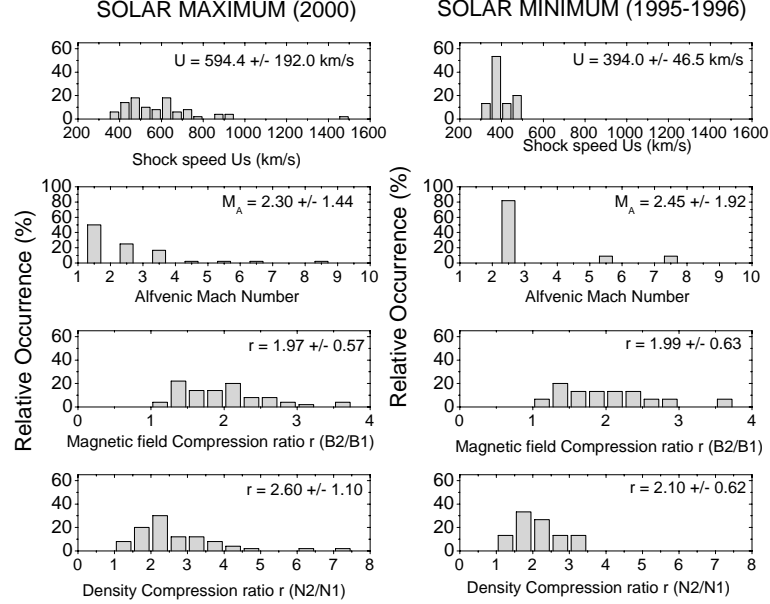


Figure 5. Upper panels, calculated shock speeds for solar maximum (left) and solar minimum (right). Intermediate panels, Alfvenic Mach number in solar maximum (left) and in solar minimum (right). Lower intermediate panels, magnetic field compression ratio in solar maximum (left) and in solar minimum (right). Bottom panels, density compression ratio in solar maximum (left) and in solar minimum (right).

### Pressure calculations

In the fluid description of a plasma, the definition of ideal gas pressure can be applied, and the momentum conservation can be expressed as a pressure balance. The thermal pressure of plasma is calculated in eq.(4):

$$p_T = N_p k T_p \quad (4)$$

In eq. (4)  $N_p$  and  $T_p$  are the proton density and temperature, and  $k$  is the Boltzmann constant. The magnetic pressure is also defined in terms of the total magnetic field, in eq. (5) [1,4].

$$p_B = \frac{B^2}{2\mu_0} \quad (5)$$

The thermal and magnetic pressures are called static pressures of plasma. The momentum flux of plasma is also called dynamic pressure and it is expressed in eq. (6):

$$p_{dyn} = N_p m^+ V_p^2 \quad (6)$$

Figure 6 shows the calculation of the thermal, magnetic and dynamic pressures variations through the shocks, as a step-variation between upstream and downstream sides. The

pressures are given in units of nPa and the time is in arbitrary units. It is seen that pressure values both at upstream and downstream sides are higher in solar maximum than in solar minimum. Also the step-like variations are higher for solar maximum. Another interesting point to observe is that the dynamic pressure is higher by almost 2 magnitude orders than magnetic and thermal pressures. These results indicate that the majority of energy/momentum flux is in kinetic form instead of thermal or magnetic energy. Actually, in the solar wind, about 99% of the pressure is in form of dynamic pressure [1].

## IV Conclusions

Interplanetary shock parameter variations were studied in this work in solar maximum (2000) and solar minimum (1995-1996) activity. It was observed that the majority of interplanetary shocks are of the fast forward type, about 88% of the identified shocks in solar maximum and 66% in solar minimum. Fast reverse shocks were observed to have a higher relative occurrence in solar minimum (24%) than in solar maximum (9%), because of the larger number of corotating streams in the descending and minimum phases of solar cycle.

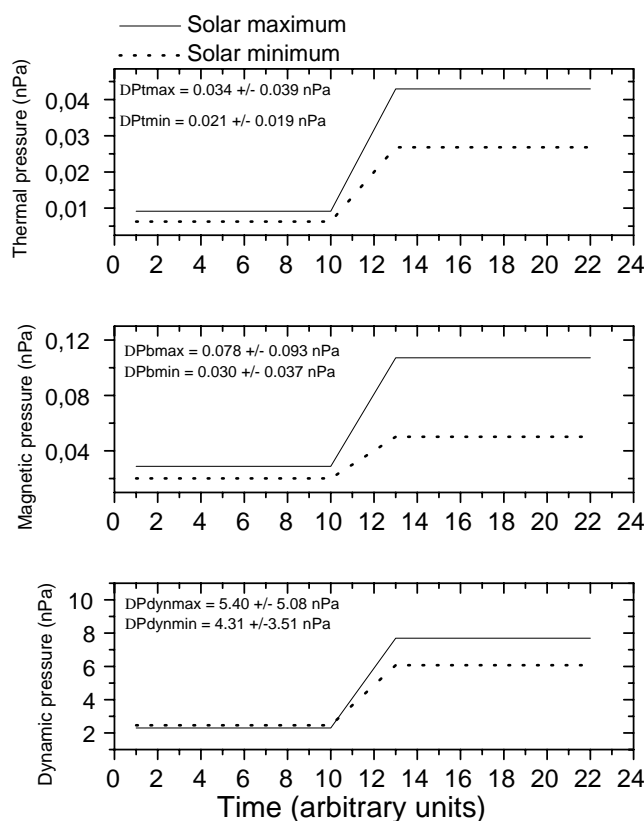


Figure 6. Upper panel, step-like calculated thermal pressure variations (in nPa) for solar maximum(continuous line) and solar minimum (dotted line). Intermediate and lower panels, magnetic and dynamical pressures variations.

Plasma and magnetic fields parameters have higher upstream-downstream averages and variations in solar maximum than in solar minimum, with exception of the proton density. Proton density is higher in solar minimum probably because of the heliospheric current sheet, which has a higher density than the background environment, and is more stable during solar minimum conditions. Shock speed variation is much higher in solar maximum (average speed variation of 83 km/s) than in solar minimum (33.1 km/s). The shock speed is also larger in solar maximum (594 km/s against 394 km/s in minimum), because in solar maximum the solar ejecta have higher speeds.

Alfvenic Mach number and magnetic field compression ratio are very similar for both solar maximum and solar minimum. Shocks strength, quantified by Mach Alfvenic number, is similar in solar maximum and solar minimum, because higher shock speeds in solar maximum are being compensated by higher Alfvenic speeds.

Thermal, magnetic and dynamic pressure variations through the shocks are larger in solar maximum than in solar minimum, as expected because the majority of parameters have a stronger variation in solar maximum. Moreover, it was observed that dynamic pressure values are about two orders of magnitude higher than thermal and magnetic pressure, which confirms that a large fraction of solar wind energy is in form of kinetic energy.

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