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Nuclear Dependence of the Saturation Scale and its Consequences for the Electron-ion Collider

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We study the predictions of CGC physics for electron-ion collisions at high energies. The nucleus at high energies acts as an amplifier of saturation effects. We have investigated some observables, using a generalization for nuclear targets of the Iancu-Itakura-Munier model, and our results indicate that the experimental analysis of these observables in the future electron-ion collider could discriminate between linear and saturation physics, as well as constrain the behavior of the saturation scale.

Keywords: Electron-ion collisions; Saturation physics; Color dipole formalism

I. INTRODUCTION

The search for signatures of parton saturation effects has been subject of an active research in the last years (for recent reviews see, e.g. [1]). It has been observed that HERA data in the small x and low Q^2 region can be successfully described with saturation models [2-4]. Moreover, the experimentally measured total cross sections [5] and charm production cross section [6] present the property of geometric scaling. The recently observed [7] supression of high p_T hadron yields at forward rapidities in dAu collisions at RHIC follows the behavior anticipated on the basis of CGC ideas [8–11]. All these results provide strong evidence for saturation at HERA and RHIC. However, more definite conclusions are not possible due to the small value of the saturation scale in the kinematical range of HERA and due to the complexity of dAu collisions, where we need to consider the substructure of the projectile and the target, as well as the fragmentation of the produced partons. So far, other models (without saturation included) are able to describe the same set of data (see e.g. Refs. [12, 13]). In order to discriminate between these different models and test the CGC physics, it would be very important to consider an alternative search. To this purpose, the future electron-nucleus eRHIC collider is ideal, because it can probably determine whether parton distributions saturate or not and constrain the behavior of the nuclear gluon distribution. After the eRHIC was proposed, it became crucial to have some quantitative estimates of the impact of saturation effects on observables. Some of these estimates can be found in [14-16].

In the following section we present the color dipole formalism. In the next section we introduce the saturation scale and its possible nuclear dependences. In sequence, a comparison of the results of the model with available data on F_2^A is shown, as well as the estimate of saturation effects on the nuclear structure function. Finally, we present our conclusions.

II. DIPOLE FORMALISM

At small *x*, Deep Inelastic Scattering (DIS) is most conveniently computed with the dipole formalism. The virtual photon splits into a quark anti-quark dipole, which interacts with the target [17]. In this formalism the structure function of the target can be expressed as:

$$F_2(x,Q^2) = \frac{Q^2}{4\pi^2 \alpha_{em}} (\sigma_T + \sigma_L) \tag{1}$$

where

$$\sigma_{T,L}(x,Q^2) = \int_0^1 dz \int d^2r |\Psi_{T,L}(z,r,Q^2)|^2 \sigma_{dip}(x,r)$$
 (2)

with

$$|\Psi_T(z, r, Q^2)|^2 = \frac{6\alpha_{\rm em}}{4\pi^2} \sum_f e_f^2 \times [z^2 + (1-z)^2] \varepsilon^2 K_1^2(\varepsilon r) + m_f^2 K_0^2(\varepsilon r)$$
 (3)

and

$$|\Psi_L(z, r, Q^2)|^2 = \frac{6\alpha_{\rm em}}{\pi^2} \sum_f e_f^2 \times \left\{ Q^2 z^2 (1 - z)^2 K_0^2(\varepsilon r) \right\}$$
 (4)

The last two expressions represent the squared photon wave function for transverse (T) and longitudinal (L) photons, respectively. The variable r defines the relative transverse separation of the pair (dipole) and z (1-z) is the longitudinal momentum fraction of the quark (antiquark). The auxiliary variable $\varepsilon^2 = z(1-z)Q^2 + m_f^2$ depends on the quark mass, m_f . The $K_{0,1}$ are the McDonald functions and the summation is performed over the quark flavors.

At high energy [18–20], σ_{dip} can be computed in the eikonal approximation and it is given by:

$$\sigma_{dip}(x,r) = 2 \int d^2b \, \mathcal{N}(x,r,b) \tag{5}$$

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where $\mathcal{N}(x,r,b)$ is the forward scattering amplitude for a dipole with size r and impact parameter b. Here we assume that the impact parameter dependence of \mathcal{N} can be factorized as $\mathcal{N}(x,r,b) = \mathcal{N}(x,r)S(b)$. So, $\sigma_{dip}(x,r) = \sigma_0 \mathcal{N}(x,r)$, with $\sigma_0 = 2\pi R_p^2$ (R_p is the proton radius).

In the IIM parametrization [4] the dipole-target forward scattering amplitude was assumed to have the form:

$$\mathcal{N} = \begin{cases} \mathcal{N}_0 \left(\frac{rQ_s}{2} \right)^{2 \left(\gamma_s + \frac{\ln(2/rQ_s)}{\kappa \lambda Y} \right)} & rQ_s \le 2\\ 1 - \exp^{-a \ln^2(b rQ_s)} & rQ_s > 2 \end{cases}$$
 (6)

where Q_s is the saturation scale discussed in the next section. The expression in the second line of Eq. (6) has the correct functional form for $r \gg 2/Q_s$, as obtained either by solving the BK equation [18, 21] or from the theory of the CGC [1]. This is strictly valid only to LO accuracy, but here it is used merely as a convenient interpolation. The details of this interpolation are unimportant for the calculation of σ_{γ^*p} . The coefficients a and b are determined uniquely from the condition that $\mathcal{N}(rQ_s,Y)$ and its slope be continuous at $rQ_s=2$. The overall factor \mathcal{N}_0 in the first line of Eq. (6) is ambiguous, reflecting an ambiguity in the definition of Q_s . The coefficients γ_s and κ are fixed to their LO BFKL values: $\gamma_s=0.63$ and $\kappa=9.9$.

III. SATURATION SCALE

The saturation momentum, $Q_s(x)$, is the value of the transverse momentum below which saturation effects are expected to be important in the gluon distribution. It can be estimated in a simple geometrical way. Let's assume that the transverse area of one gluon in the target is approximately given by α_s/Q^2 and that the number of gluons (per unit rapidity) "seen" by an external probe is $xG(x,Q^2)$. The area occupied by all these gluons is $\alpha_s/Q^2xG(x,Q^2)$. When this area becomes comparable to the total geometrical area of the target, πR_p^2 , saturation sets on. This matching of areas gives an equation, which can be solved for Q yielding the especial value Q_s :

$$Q_s^2(x) \simeq \alpha_s \frac{xG(x, Q_s^2)}{\pi R_p^2} = Q_0^2 \left(\frac{x_0}{x}\right)^{\lambda}$$
 (7)

where $x_0 = 0.3 \times 10^{-4}$ and $\lambda = 0.29$. For a nuclear target we expect that, in a first approximation, $xG(x, Q^2) \rightarrow AxG(x, Q^2)$, $R_p \rightarrow R_A = R_p A^{1/3}$ and thus, from (7) we have:

$$Q_s^2(x) \to A^{1/3} \times Q_s^2(x) \tag{8}$$

Moreover, we may generalize the IIM model to nuclear collisions assuming the following basic transformation for the parameter σ_0 :

$$\sigma_0 \to \sigma_0^A = A^{2/3} \times \sigma_0 \tag{9}$$

These two transformations define what we call model IIM1. For comparison we also consider another A-dependence of

the saturation momentum, which was suggested in [22]

$$Q_s^2(x) \to Q_{s,A}^2 = [A^{1/3}]^{1/\delta} \times Q_s^2(x)$$
 (10)

where $\delta = 0.79$. Notice that, with this choice for δ the A dependence of Q_s becomes stronger. This feature arises from the inclusion of the impact parameter in all calculations, as done in [22]. The transformations (9) and (10) define the model IIM2. Further studies of the A-dependence of Q_s can be found in Refs. [23, 24].

IV. RESULTS AND DISCUSSION

In this section we calculate the ratio:

$$R \equiv \frac{2F_2^A}{AF_2^D} \tag{11}$$

where D = deuteron, with the models IIM1 and IIM2 and compare the results with the experimental data, taken by the Fermilab E665 collaboration, using inelastically scattered muons of average incident momentum 470 GeV/c [25]. These data, taken over a wide kinematic range, have shown that the proton and neutron structure functions are modified by a nuclear environment. The modifications depends on the parton momentum fraction: for momentum fractions x < 0.1 and 0.3 < x < 0.7, a depletion is observed in the nuclear structure functions. The low x (shadowing region) and the larger x (EMC region) are bridged by an enhancement known as antishadowing for 0.1 < x < 0.3. We refer to the entire phenomena as the nuclear shadowing effect [27]. As shown in Ref. [26] these effects can be described by the DGLAP evolution equation with a suitable set of nonperturbative initial conditions. Another possibility to describe the small-x behavior of the ratio R is to consider multiple scattering of the projectile on several target nucleons using Glauber-Gribov approach [24]. Here we are interested in the low-x region ($x < 10^{-3}$), where it is believed that the behavior of R should be determined by high density QCD and parton saturation effects. In our approach we do not include higher-x corrections and rather try to understand the behavior of R in terms of parton saturation. Strictly speaking, our formalism is valid only in the very low x region, whereas the available data exist only in the intermediate x region. In order to have an idea of how well our results can reproduce the data we have to extrapolate them to intermediate x region. In doing this, we move to the region dominated by the linear regime, where saturation is not important and the dipole scattering amplitude is dominated by the first line of expression (6). In this regime, denoted color transparency regime, the scattering amplitude should behave as $(rQ_s)^2$. However a careful analysis of this expression shows that the parenthesis in the exponent never becomes equal to one (!) and thus the $(rQ_s)^2$ behavior is never really reached. This is a limitation of the IIM parametrization which is only valid in the saturation and extended geometric scaling regimes. In our present exercise we insist on the comparison with data, which are in general outside of these regimes. Therefore we have some freedom to play a bit

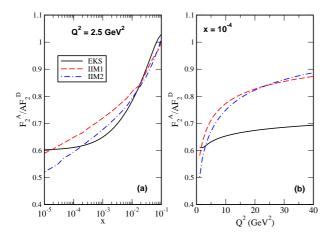


FIG. 1: Ratio $R(x,Q^2) \equiv F_2^A(x,Q^2)/F_2^p(x,Q^2)$ as a function of x (a) and Q^2 (b). The predictions of the EKS parametrization are also shown.

with the parameters of (6). Making use of this freedom, we have multiplied the ratio R by a constant so that, at the point x = 0.1, it coincides with one, in agreement with experimental data. Since F_2 is a function of Q^2 this adjust has to be done for each value of Q^2 .

In Fig. 1, we show the ratio R computed with both models, IIM1 and IIM2, as a function of x [Fig. 1(a)] and Q^2 [Fig. 1(b)] for a lead nucleus (A=208). As expected the IIM2 model has a stronger dependence with A and therefore a larger deviation from R=1. For comparison we also show the ratio R calculated with the EKS parametrization [26] of the ratio of nuclear structure functions. This parametrization comes from a global fit of the nuclear experimental data using DGLAP evolution. Notice that, as mentioned above, at x=0.1 the EKS curve approaches one. Our curves IIM1 and IIM2 were constrained to pass through this point as well.

The main difference between the predictions is the behavior of the ratio R at small x. EKS predicts that the ratio is constant, and the IIM1 and IIM2 predict that the ratio still decreases in this limit (small x). We can see that for R as a function of Q^2 , the predictions differ significantly. This behavior arises because EKS is directly related to DGLAP evolution and the IIM1 and IIM2 models are associated to the saturation and geometric scaling regimes.

The deviation of R from one in the region 0.01 < x < 0.1 comes from the non-trivial A dependence of the dipole cross section [Eqs. (8) and (10)]. In this region our Ansatz, (8) or (10), leads to results similar to those obtained with for with the Glauber-Gribov approach [27], although they are independent from each other.

In Fig. 2 we show the ratio R as a function of x for a lead nucleus A = 208. On the top of the figure we have included the values of Q^2 , which are different for each x. The model IIM1 (IIM2) is represented by the dashed (dash-dotted) line. As it can be seen both models agree reasonably well with the data, especially considering that, apart from a normalization factor there was no free parameter.

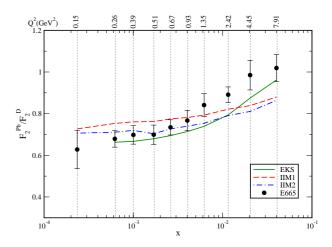


FIG. 2: Comparison of the results of the models IIM1 and IIM2 with experimental data at small *x* for the ratio of Pb (lead) to D (deuteron), from E665 Collaboration [25].

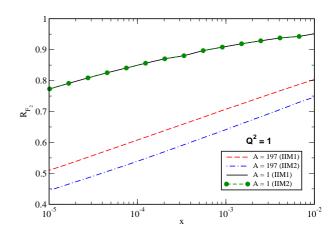


FIG. 3: Ratio of the full to the linear predictions for the nuclear structure function as a function of x.

In order to obtain a more precise estimate of modification in the observables F_2 and F_L by saturation physics, in Fig. 3 and Fig. 4 we present the ratios R_{F_2} and R_{F_L} of full to linear predictions for nuclear structure function F_2^A and F_L^A . We consider two typical values of the atomic number. As expected, the contribution of the saturation physics increases at larger nuclei and smaller values of x. In particular, for values of x around 10^{-5} , we predict a reduction of about 50% in the total and longitudinal structure functions.

V. SUMMARY & CONCLUSIONS

In this work we have studied the predictions of CGC physics for electron-ion collisions at high energies, using a generalization for nuclear targets of Iancu-Itakura-Munier model. We have estimated the ratio of the nuclear to the deuteron (or proton) structure functions. We have compared

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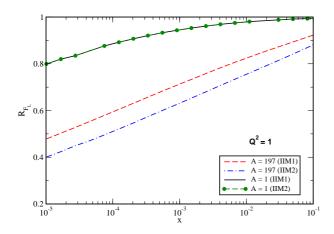


FIG. 4: Ratio of the full to the linear predictions for the longitudinal nuclear structure function as a function of *x*.

our results with experimental data from the E665 collaboration and also with the EKS parametrization. Although the EKS formula does not include saturation physics and although the E665 data are taken at too low energy (for saturation effects to be dominant), the reached values of x and Q^2 fall already in the saturation domain, justifying the comparison. For the sake of a preliminary estimate of saturation efects in an electron-ion collider we have computed, with the existent nuclear dependent saturation scales, the ratio of the F_2 and F_L structure functions, finding a strong reduction ($\simeq 50$ %) of these ratios. The impact of these results encourages us to further study the subject.

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