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Event-by-Event Fluctuations of Transverse Momentum and Multiparticle Clusters in Relativistic Heavy-Ion Collisions *

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We analyze the event-by-event fluctuations of mean transverse momentum measured recently by the PHENIX and STAR Collaborations at RHIC. We argue that the observed scaling of strength of dynamical fluctuations with the inverse number of particles can be naturally explained by formation of multiparticle clusters.

Keywords: Relativistic heavy-ion collisions; Event-by-event fluctuations; Particle correlations

I. INTRODUCTION

This paper is based on our recent analysis [1] of the event-by-event fluctuations of the mean transverse-momentum measured by PHENIX [2] and STAR [3, 4] Collaborations at RHIC. The discussed new data has extended our knowledge of the phenomena studied intensely in recent years [5–20]. One of the central issues in this field is whether the p_T fluctuations at intermediate momenta result from jets [21, 22]. In this paper we argue that the observed scaling of strength of dynamical fluctuations may be naturally explained by formation of multiparticle clusters. From our point of view, the explanation of the data in terms of quenched jets represents only one possible option, other physical mechanisms leading to clustering also explain the data.

Our reasoning is based on the following three observations: *i*) the mean and the variance of the inclusive momentum distribution are practically constant at low centrality parameters ($c = 0 - 30\%$),

$$\langle M \rangle = \text{const.}, \quad \sigma_p = \text{const.}, \quad (1)$$

ii) the variance of the average momenta for the mixed events is practically equal to the variance of the inclusive distribution divided by the average multiplicity,

$$\sigma_M^{\text{mix}} \simeq \frac{\sigma_p}{\langle n \rangle}, \quad (2)$$

finally, *iii*) the difference of the experimental and mixed-event variances of mean p_T , denoted as σ_{dyn}^2 , scales as inverse multiplicity

$$\sigma_{\text{dyn}}^2 \equiv \sigma_M^2 - \sigma_M^{2,\text{mix}} \sim \frac{1}{\langle n \rangle}. \quad (3)$$

As mentioned above, an explanation of this scaling can be provided by clustering in the expansion velocity. Moreover, the extracted value of σ_{dyn} is large at the expected scale provided by the variance of p_T , which indicates that the clusters should contain at least several particles in order to combinatorically enhance the magnitude to the observed level. This point is supported by the numerical calculations of the values of σ_{dyn}^2 coming from the resonance decays and from thermal clusters in statistical models of heavy-ion collisions, which show that these values are very small [1, 23].

II. SIMPLE WAY OF DOING STATISTICAL ANALYSIS

In this Section we present elementary statistical considerations which form the basis of our treatment of the fluctua-

TABLE I: Analysis of the event-by-event fluctuations in the transverse momentum. Upper rows: the PHENIX experimental data at $\sqrt{s_{NN}} = 130$ GeV [2]; middle rows: the mixed-event results; bottom rows: our way of looking at the data. One observes that to a good approximation $\sigma_M^{2,\text{mix}} \simeq \sigma_p^2 / \langle n \rangle$ and $\sigma_{\text{dyn}}^2 = (\sigma_M^2 - \sigma_M^{2,\text{mix}}) \sim 1 / \langle n \rangle$. Except for the first two rows, all values are given in MeV. The errors in the last row reflect the unknown round-off errors in the data of the upper and middle parts.

centrality	0-5%	0-10%	10-20%	20-30%
$\langle n \rangle$	59.6	53.9	36.6	25.0
σ_n	10.8	12.2	10.2	7.8
$\langle M \rangle$	523	523	523	520
σ_p	290	290	290	289
σ_M	38.6	41.1	49.8	61.1
$\langle M \rangle^{\text{mix}}$	523	523	523	520
σ_M^{mix}	37.8	40.3	48.8	60.0
$\sigma_p \sqrt{\frac{1}{\langle n \rangle} + \frac{\sigma_n^2}{\langle n \rangle^3}}$	38.2	40.5	49.8	60.8
$\sigma_{\text{dyn}} \sqrt{\langle n \rangle}$	60.3 ± 1.6	59.2 ± 1.5	59.8 ± 1.2	57.7 ± 1.1

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tions. We use the notation where the letter p denotes $|\vec{p}_T|$, p_i is the value of p for the i th particle, and $M = \sum_{i=1}^n p_i/n$ is the mean transverse momentum in an event of multiplicity n . Consider events of multiplicity n and transverse momenta p_1, p_2, \dots, p_n . The multiplicity n and the momenta are varying randomly from event to event. The probability density of occurrence of a given momentum configuration is $P(n)\rho_n(p_1, \dots, p_n)$, where $P(n)$ is the multiplicity distribution and $\rho_n(p_1, \dots, p_n)$ is the conditional probability distribution of occurrence of p_1, \dots, p_n in accepted events, provided we have the multiplicity n . Note that in general ρ depends functionally on n , as indicated by the subscript. The normalization is

$$\sum_n P(n) = 1, \quad \int dp_1 \dots dp_n \rho_n(p_1, \dots, p_n) = 1. \quad (4)$$

The marginal probability densities are defined as

$$\rho_n^{(n-k)}(p_1, \dots, p_{n-k}) \equiv \int dp_{n-k+1} \dots dp_n \rho_n(p_1, \dots, p_n), \quad (5)$$

with $k = 1, \dots, n-1$. These are also normalized to unity, as follows from Eq. (4). Since the number of arguments distinguishes the marginal distributions $\rho_n^{(n-k)}$, in the following we drop the superscript $(n-k)$. Further, we introduce the following definitions

$$\langle p \rangle_n \equiv \int dp \rho_n(p) p, \quad (6)$$

$$\text{var}_n(p) \equiv \int dp \rho_n(p) (p - \langle p \rangle_n)^2,$$

$$\text{cov}_n(p_1, p_2) \equiv \int dp_1 dp_2 (p_1 - \langle p \rangle_n)(p_2 - \langle p \rangle_n) \rho_n(p_1, p_2).$$

The subscript n indicates that the averaging is taken in samples of multiplicity n . We note in passing that the commonly used *inclusive* distributions are related to the marginal probability distributions in the following way:

$$\begin{aligned} \rho_{\text{in}}(x) &\equiv \sum_n P(n) \int dp_1 \dots dp_n \sum_{i=1}^n \delta(x - p_i) \rho_n(p_1, \dots, p_n) \\ &= \sum_n n P(n) \rho_n(x), \end{aligned} \quad (7)$$

$$\begin{aligned} \rho_{\text{in}}(x, y) &\equiv \sum_n P(n) \int dp_1 \dots dp_n \sum_{i,j=1, i \neq j}^n \delta(x - p_i) \delta(y - p_j) \rho_n(p_1, \dots, p_n) \\ &= \sum_n n(n-1) P(n) \rho_n(x, y), \end{aligned} \quad (8)$$

which are normalized to $\langle n \rangle$ and $\langle n(n-1) \rangle$, respectively. For the variable $M = \sum_{i=1}^n p_i/n$ we find immediately

$$\begin{aligned} \langle M \rangle &= \sum_n P(n) \int dp_1 \dots dp_n M \rho_n(p_1, \dots, p_n) \\ &= \sum_n P(n) \langle p \rangle_n, \end{aligned} \quad (9)$$

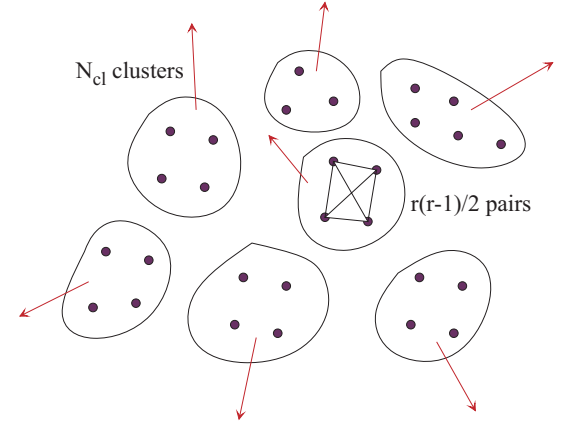


FIG. 1: The cluster picture of correlations. Particles are grouped in N_{cl} clusters, containing on the average r particles. The particles within a cluster move at very similar collective velocities, indicated by arrows.

$$\begin{aligned} \langle M^2 \rangle &= \sum_n P(n) \int dp_1 \dots dp_n M^2 \rho_n(p_1, \dots, p_n) \\ &= \sum_n \frac{P(n)}{n} \langle p^2 \rangle_n \\ &\quad + \sum_n \frac{P(n)}{n^2} \left[\sum_{i,j=1, i \neq j}^n \text{cov}_n(p_i, p_j) + n(n-1) \langle p \rangle_n^2 \right]. \end{aligned} \quad (10)$$

III. ANALYSIS OF THE PHENIX DATA

At first we discuss the PHENIX measurement [2] of the event-by-event fluctuations of the mean transverse momentum at $\sqrt{s_{NN}} = 130$ GeV. We use the experimental fact that the variance of the momentum distribution and its mean are independent of centrality (in the considered range), which allows us to replace the quantities $\langle p \rangle_n$ by $\langle M \rangle$ and $\langle p^2 \rangle_n - \langle p \rangle_n^2$ by σ_p^2 at the average multiplicity, denoted as $\sigma_{p, \langle n \rangle}^2$. In this way we get

$$\sigma_M^2 = \sigma_{p, \langle n \rangle}^2 \sum_n \frac{P(n)}{n} + \sum_n \frac{P(n)}{n^2} \left[\sum_{i,j=1, i \neq j}^n \text{cov}_n(p_i, p_j) \right]. \quad (11)$$

In the mixed events, by construction, particles are not correlated, hence the covariance term in Eq. (11) vanishes and

$$\sigma_M^{2, \text{mix}} = \sigma_{p, \langle n \rangle}^2 \sum_n \frac{P(n)}{n} \simeq \sigma_{p, \langle n \rangle}^2 \left(\frac{1}{\langle n \rangle} + \frac{\sigma_n^2}{\langle n \rangle^3} + \dots \right), \quad (12)$$

where in the last equality we have used the fact that the distribution $P(n)$ is narrow and expanded $1/n = 1/[\langle n \rangle + (n - \langle n \rangle)]$ to second order in $(n - \langle n \rangle)$. Comparison made in Table I, see the 8th and 9th rows, shows that formula (12) works at the 1-2% level. In addition, since $\sigma_{p, \langle n \rangle}^2$ is not altered by the event

mixing procedure, subtracting (12) from (11) yields

$$\begin{aligned}\sigma_{\text{dyn}}^2 &= \sum_n \frac{P(n)}{n^2} \sum_{i,j=1, j \neq i}^n \text{cov}_n(p_i, p_j) \\ &\simeq \frac{1}{\langle n \rangle^2} \sum_{i,j=1, j \neq i}^{\langle n \rangle} \text{cov}_{\langle n \rangle}(p_i, p_j).\end{aligned}\quad (13)$$

IV. CLUSTER EXPLANATION

The scaling of the dynamical fluctuations with $\langle n \rangle$, see the last row of Table I and Eq. (3), may be regarded as a constraint restricting the behavior of the covariance term. For instance, one can immediately conclude that if all particles were correlated to each other, $\sum_{i,j=1, j \neq i}^n \text{cov}_{\langle n \rangle}(p_i, p_j)$ would be proportional to the number of pairs, and σ_{dyn} would not depend on $\langle n \rangle$ at large multiplicities. A natural explanation of the scaling (3) comes from the cluster model, depicted in Fig. 1. The system is assumed to have N_{cl} clusters, each containing (on the average) r particles. Below we keep $r = \text{const.}$ for simplicity (a more general case is discussed in Ref. [1]). The particles are correlated if and only if they belong to the same cluster, where the covariance per pair is 2cov^* . The number of correlated pairs within a cluster is $r(r-1)/2$. Some particles may be unclustered, hence the ratio of clustered to all particles is $\langle N_{\text{cl}} \rangle r / \langle n \rangle = \alpha$. If all particles are clustered then $\alpha = 1$. With these assumptions Eq. (13) becomes

$$\sigma_{\text{dyn}}^2 = \frac{\alpha(r-1)}{\langle n \rangle} \text{cov}^*, \quad (14)$$

which complies to the scaling (3). An immediate conclusion here is that the ratio α cannot depend on $\langle n \rangle$ (in the considered centrality range, $c = 0 - 30\%$) in order for the scaling to hold.

The question now is whether we can use the above results to draw conclusions on effects of jets (minijets), which have been proposed as a possible explanation of the experimental

data even at the considered soft momenta [21]. Jets, when fragmenting, lead to clusters in the momentum space. The resulting full covariance from jets is then $N_{\text{cl,jet}} j(j-1) \frac{\text{cov}^j}{\langle n \rangle^2}$, where $N_{\text{cl,jet}}$ is the number of clusters originating from jets, j is the average number of particles in the cluster, and 2cov^j is the average covariance per pair. The total number of particles produced from jets is $N_{\text{cl,jet}} j$. On the other hand, the commonly accepted estimate of the dependence of $N_{\text{cl,jet}} j$ on centrality is accounted for by the nuclear modification factor R_{AA} multiplied by the number of binary nucleon-nucleon collisions N_{bin} . Since R_{AA} depends on the ratio $\langle n \rangle / \langle n \rangle_{pp}$, where $\langle n \rangle_{pp}$ is the multiplicity in the proton-proton collisions, in a given p_T bin one finds

$$N_{\text{cl,jet}} j \sim R_{\text{AA}} N_{\text{bin}} = \frac{\langle n \rangle}{N_{\text{bin}} \langle n \rangle_{pp}} N_{\text{bin}} \sim \langle n \rangle, \quad (15)$$

which complies to the scaling of Eq. (14).

V. CONCLUSIONS

The observed scaling of the dynamical fluctuations of mean transverse-momentum may be naturally explained by the cluster model. We emphasize that the scaling follows from the presence of clusters only, and is insensitive to the nature of their physical origin as long as one imposes the condition $N_{\text{cl}} \sim \langle n \rangle$.

The explanation of the observed data in terms of quenched jets agrees with the cluster picture. However, the explanation of the centrality dependence of the p_T fluctuations in terms of jets based solely on Eq. (15) is not decisive: any mechanism leading to clusters would do, for instance the thermal clusters discussed in Ref. [1] or mechanisms of Ref. [24]. Microscopic realistic estimates of the magnitude of cov^j and j are necessary in that regard, including the interplay of the jets and medium. In short, the nature of clusters remains an open issue. For the current status of this program the reader is referred to [22, 25].

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