



Journal of Applied Research and Technology

ISSN: 1665-6423

jart@aleph.cinstrum.unam.mx

Centro de Ciencias Aplicadas y Desarrollo

Tecnológico

México

Baharodimehr, A.; Abolfazl Suratgar, A.; Sadeghi, H.
Capacitive MEMS accelerometer wide range modeling using artificial neural network
Journal of Applied Research and Technology, vol. 7, núm. 2, agosto, 2009, pp. 185-192
Centro de Ciencias Aplicadas y Desarrollo Tecnológico
Distrito Federal, México

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Capacitive MEMS accelerometer wide range modeling using artificial neural network

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ABSTRACT

This paper presents a nonlinear model for a capacitive microelectromechanical accelerometer (MEMA). System parameters of the accelerometer are developed using the effect of cubic term of the folded-flexure spring. To solve this equation, we use the FEA method. The neural network (NN) uses the Levenberg-Marquardt (LM) method for training the system to have a more accurate response. The designed NN can identify and predict the displacement of the movable mass of accelerometer. The simulation results are very promising.

Keywords: Accelerometer, MEMS, cubic stiffness, neural network.

RESUMEN

Este trabajo presenta un modelo no lineal para un acelerómetro microelectromecánico de tipo capacitivo (MEMA). Asimismo, en él se desarrollan parámetros de sistema de el acelerómetro utilizando el efecto del término cúbico del resorte de flexión plegado. Para resolver esta ecuación, usamos el método FEA. La red neuronal (RN) usa el método Levenberg-Marquardt (LM) para entrenar al sistema a fin de que tenga una respuesta más exacta. La RN diseñada puede identificar y predecir el desplazamiento de la masa móvil del acelerómetro. Los resultados de la simulación son muy prometedores.

Palabras clave: Acelerómetro, MEMS, rigidez cúbica, red neuronal.

1. Introduction

Nonlinearities in Micro Electro Mechanical System (MEMS) can arise from various sources such as spring and damping mechanisms [1-4], capacitive circuit elements [5], nonlinear coupling between the electrostatic force and displacement on the MEM structure [6], therefore, electrostatic MEMS have nonlinear regions[7].

Several researchers have developed various capacitive MEMS accelerometers [8-11], however, the circuitry design behind the sensing plate of all those accelerometers is based on buffers and demodulators (with low frequency sampling), which is not a suitable response for high accuracy applications. This paper presents a new method to sense the motion of movable plates to have a high

accuracy and prevent the device from damage at high accelerations using an artificial neural network [17]. First, a nonlinear dynamic equation with mechanical nonlinearities is obtained. Solving this nonlinear equation can help to determine the displacement of a movable plate with high accuracy, then the applied acceleration at the specific time is sent to the NN to identify and predict the displacement of the movable plate. For training the neural network, the Levenberg-Marquardt algorithm is selected.

The accelerometer sensor is a combination of springs, masses and motion sensing and actuation cells as shown in Fig.1 (a). It consists of a variable differential air capacitor whose plates are etched into the suspended polysilicon layer. The moving plate of the capacitor is formed by a large number

of fingers extending from the beam, a proof mass supported by tethers anchored to the substrate. When responding to an applied acceleration (Fig.1 (b)), the proof mass's inertia causes it to move along a predetermined axis. As the fingers extending from the beam move between the fixed fingers, capacitance change is being sensed and used to measure the amplitude of the force that led to the displacement of the beam.

In Section 2, the analytical model of the MEM accelerometer (MEMA) is obtained. In Section 3, a nonlinear model using the neural network is proposed. Simulation results are given in Section 4. Finally, Section 5 includes the conclusions.

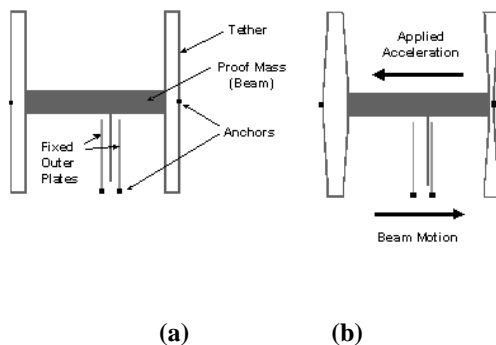


Figure 1. Schematic diagram of the accelerometer model.

2. Analytical Modeling of MEMA

An accelerometer can be modeled as a spring-mass-damper system in the x-direction. Physics-based models for the effective spring stiffness of the folded-flexure suspensions, the effective masses of the proof mass and viscous air damping are used in the synthesis tool [12].

Approximations to the nonlinear rod theory provide formulas for the coefficients of linear and cubic stiffening, which enable predictions of spring hardening behavior [1]. Considering the folded-

flexure spring and lumped element modeling, the following expression for the spring is obtained:

$$F_{spring} = k_1 \cdot x + k_3 \cdot x^3 \quad (1)$$

Where k_1 and k_3 are the linear and cubic stiffness of the folded-flexure spring respectively, they are obtained as follows [1]:

$$k_1 = \frac{12EI}{L^3} \quad (2)$$

$$k_3 = \frac{252EA}{175L^3} \quad (3)$$

Where E is Young's modulus of polysilicon, I is the moment of inertia of the beam, L is the effective length of the folded-flexure spring and A is the cross section area of the folded-flexure spring.

Therefore, the first linear resonance frequency is given by

$$\omega_0 = \sqrt{\frac{k_1}{m}} \quad (4)$$

Where, m is the equivalent lumped mass of the movable plate.

Damping caused by air flow between the rotor and the stator fingers, and at the edge of the proof mass, is the major damping mechanism. For the lateral accelerometer, squeeze-film damping, which occurs when the air gap between two closely placed parallel surface changes, is not critical. The damping coefficient between a single comb finger gap is given as [13]

$$b = 7.2\mu l \left(\frac{t}{d}\right)^3 \quad (5)$$

Where, μ is the effective viscosity of air, t is the finger's thickness, d is the finger's gap and l is the finger's length. Table 1 and 2 summarize some properties of the accelerometer's fingers. Table 3

shows the calculated theoretical lumped parameters for the accelerometer under study.

	L_f (μ m)	W_f (μ m)	t_f (μ m)	d (μ m)	m (μ g)
Reference [14]	180	2	3	1.3	0.27
Reference [15]	55	3.9	5	1.5	0.57
Reference [13]	50	3.9	5	2	0.36
Reference [13]	55	3.9	5	2	0.45
Reference [9]	200	2	2	1	0.126

Table 1. Specification of some accelerometers.

Where L_f, W_f, t_f are length, width and thickness of the fingers respectively, f_r is the resonant frequency, d is the finger gap and m is the mass of the proof mass.

E (Young's modulus)	160GPa
ρ_m (Density)	2331kg/m ³
ν (Poisson Ratio)	≈ 0.2

Table 2. Properties of the fingers (Material: polysilicon).

k_1	0.71 [N/m]
k_3	1.136e11 [N/m ³]
m	2.7e-10 [kg]
b	11.9e-6[kg/s]

Table 3. Analytical lumped parameters of the accelerometer.

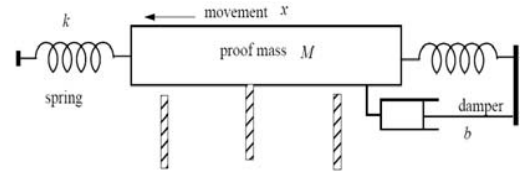


Figure 2. Schematic of a capacitive accelerometer.

In general, considering the equations above and Fig.2, the open-loop nonlinear equation of motion can be written as

$$m \frac{d^2 x}{dt^2} + b \frac{dx}{dt} + k_1 x + k_3 x^3 = m a_{ext} \quad (6)$$

Where, a_{ext} is the applied acceleration from environment, x is the center displacement of proof mass. The response of this equation is calculated using the Runge-Kutta method and shown in Fig.4.

3. Nonlinear Model of MEMA Using an Artificial Neural Network

Figure 1 shows the vertical section at constant 12wt.% (5.3at.%) Zn of the Al-Zn-Mg phase diagram [13], where the vertical lines indicate the Mg content added to the Al-12wt. %Zn master alloy. The microstructures are constituted mainly by columnar dendrites of α -Al with small τ ($Al_2Mg_3Zn_3$) precipitates and eutectic ($\alpha+\tau$) in interdendritic regions, as is shown in Figure 2 and in agreement with the work of Alvarez et al. [14].

The ANN's inputs are applied accelerations and time of actuating of the specific acceleration applied to the device. The output of the ANN is the displacement of the movable plate; here, a three layer feed-forward network is created (Fig.3). The first layer has 22 linear transfer functions, the second layer has 10 hyperbolic tangent sigmoid transfer functions and the last layer has one linear transfer function.

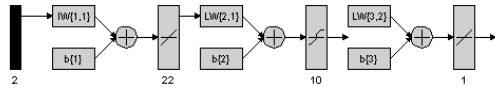


Figure 3. Neural Network Design.

For training the network, we suggest the Levenberg-Marquardt (LM) algorithm. In the following, the Levenberg-Marquardt method is reviewed [16]. In the EBP algorithm, the performance index $F(w)$ to be minimized is defined as the sum of squared errors between the target outputs and the network's simulated outputs, namely:

$$F(w) = e^T e \quad (7)$$

Where, $w = [w_1, w_2, \dots, w_N]$ consists of all weights of the network, e is the error vector comprising the error for all the training examples.

When training with the LM method, the increment of weights Δw can be obtained as follows:

$$\Delta w = [J^T J + \mu I]^{-1} J^T e \quad (8)$$

Where, J is the Jacobian matrix, μ is the learning rate which is to be updated using the β depending on the outcome. In particular, μ is multiplied by the decay rate β ($0 < \beta < 1$) whenever $F(w)$ decreases, whereas μ is divided by β whenever $F(w)$ increases in a new step.

The standard LM training process can be illustrated in the following pseudo-codes:

1. Initialize the weights and parameter μ ($\mu = 0.01$ is appropriate).
2. Compute the sum of the squared errors over all inputs $F(w)$.
3. Solve (8) to obtain the increment of weights Δw
4. Recompute the sum of squared errors $F(w)$

Using $w + \Delta w$ as the trial w , and judge
IF trial in step 2 THEN

$$w = w + \Delta w$$

$$\mu = \mu \cdot \beta \quad (\beta = .1)$$

Go back to step 2

ELSE

$$\mu = \mu / \beta$$

go back to step 4

END

Considering the performance index is $F(w) = e^T e$ using the Newton method we have:

$$W_{K+1} = W_K - A_K^{-1} \cdot g_K \quad (9)$$

$$A_k = \nabla^2 F(w) \Big|_{w=w_k} \quad (10)$$

$$g_k = \nabla F(w) \Big|_{w=w_k} \quad (11)$$

$$\begin{aligned} [\nabla F(w)]_j &= \frac{\partial F(w)}{\partial w_j} \\ &= 2 \sum_{i=1}^N e_i(w) \cdot \frac{\partial e_i(w)}{\partial w_j} \end{aligned} \quad (12)$$

The gradient can be written as

$$\nabla F(x) = 2J^T e(w) \quad (13)$$

Where,

$$J(w) = \begin{bmatrix} \frac{\partial e_{11}}{\partial w_1} & \frac{\partial e_{11}}{\partial w_2} & \dots & \frac{\partial e_{11}}{\partial w_N} \\ \frac{\partial e_{21}}{\partial w_1} & \frac{\partial e_{21}}{\partial w_2} & \dots & \frac{\partial e_{21}}{\partial w_N} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial e_{KP}}{\partial w_1} & \frac{\partial e_{KP}}{\partial w_2} & \dots & \frac{\partial e_{KP}}{\partial w_N} \end{bmatrix} \quad (14)$$

$J(w)$ is called the Jacobian matrix.

Next, we want to find the Hessian matrix. The k, j elements of the Hessian matrix yields as

$$\begin{aligned} \left[\nabla^2 F(w) \right]_{k,j} &= \frac{\partial^2 F(w)}{\partial w_k \partial w_j} \\ &= 2 \sum_{i=1}^N \left\{ \frac{\partial e_i(w)}{\partial w_k} \frac{\partial e_i(w)}{\partial w_j} \right. \\ &\quad \left. + e_i(w) \cdot \frac{\partial^2 e_i(w)}{\partial w_k \partial w_j} \right\} \end{aligned} \quad (15)$$

The Hessian matrix can then be expressed as follows:

$$\nabla^2 F(W) = 2J^T(W) \cdot J(W) + S(W) \quad (16)$$

Where,

$$S(w) = \sum_{i=1}^N e_i(w) \cdot \nabla^2 e_i(w) \quad (17)$$

If we assume that $S(w)$ is small, we can approximate the Hessian matrix as

$$\nabla^2 F(w) \cong 2J^T(w)J(w) \quad (18)$$

Using (12) and (4), we obtain the Gauss-Newton method:

$$\begin{aligned} W_{k+1} &= \\ W_k - \left[2J^T(w_k) \cdot J(w_k) \right]^{-1} 2J^T(w_k)e(w_k) \\ &\cong W_k - \left[J^T(w_k) \cdot J(w_k) \right]^{-1} J^T(w_k)e(w_k) \end{aligned} \quad (19)$$

The advantage of the Gauss-Newton method is that it does not require calculation of second derivatives.

There is a problem with the Gauss-Newton method: the matrix $H=J^TJ$ may not be invertible. This can be overcome by using the following modification:

The Hessian matrix can be written as

$$G = H + \mu I \quad (20)$$

Let us suppose that the eigenvalues and eigenvectors of H are $\{\lambda_1, \lambda_2, \dots, \lambda_n\}$ and $\{z_1, z_2, \dots, z_n\}$. Then

$$\begin{aligned} Gz_i &= [H + \mu I]z_i \\ &= Hz_i + \mu z_i \\ &= \lambda_i z_i + \mu z_i \\ &= (\lambda_i + \mu) z_i \end{aligned} \quad (21)$$

Therefore, the eigenvectors of G are the same as the eigenvectors of H , and the eigenvalues of G are $(\lambda_i + \mu)$. Matrix G is positive definite by increasing μ until $(\lambda_i + \mu) > 0$ for all i , therefore, the matrix will be invertible.

This leads to the Levenberg-Marquardt algorithm:

$$w_{k+1} = w_k - \left[J^T(w_k)J(w_k) + \mu I \right]^{-1} J^T(w_k)e(w_k) \quad (22)$$

$$\Delta w_k = \left[J^T(w_k)J(w_k) + \mu I \right]^{-1} J^T(w_k)e(w_k) \quad (23)$$

As it is known, the learning parameter μ illustrates the steps of the actual output movement to the desired output. In the standard LM method, μ is a constant number.

In this paper, the input matrix for training the NN has 2×6000 dimensions and the output matrix has 1×6000 dimensions. After training the NN, for testing it, a 2×120 matrix is given to the input of the NN and the results are evaluated.

4. Simulation Results

By using Eq. (6), the displacement response of a movable plate with $10g$ ($\approx 100m/s^2$) acceleration is calculated and shown in Fig.4.

To validate Fig.4, we use the FEA analysis for modeling this accelerometer. The results are shown in Fig.5.

With regard to the cubic stiffness of the spring, the results are more accurate (Fig.6), therefore, when the ANN is trained, its output can be fit with the diagram that regards the cubic stiffness (Fig.7).

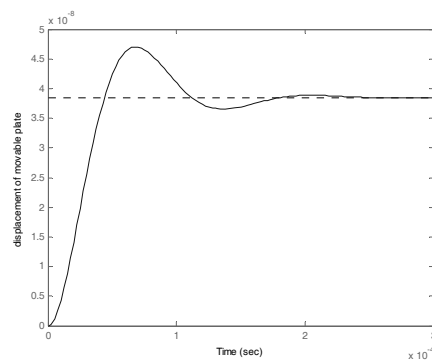


Figure 4. Calculated displacement response.

One of the advantages of this method is that we can predict the damage to the fingers of the device because of the high acceleration, so an electrical feedback to the movable plate can prevent the damage.

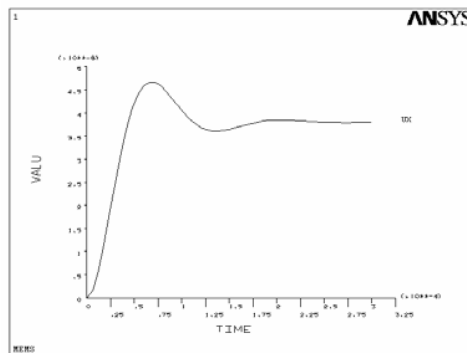


Figure 5. Displacement of the movable plate with the FEA method.

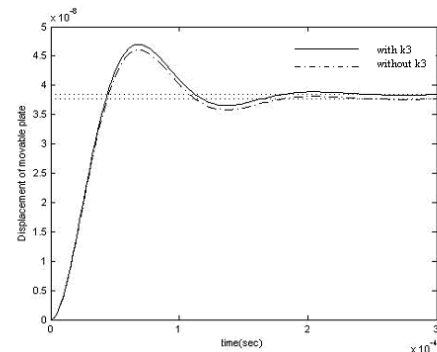


Figure 6. Comparison between the calculated displacement response with k3 and without k3.

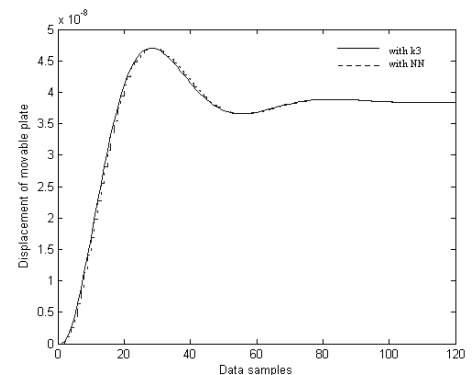


Figure 7. Output of the NN with a test data with 10g acceleration.

5. Conclusions

This paper presented a nonlinear model for a capacitive MEMA. System parameters of the accelerometer were developed using the effect of cubic term of the folded-flexure spring. To solve this equation, the FEA method was used. The artificial neural network (ANN) used the Levenberg-Marquardt (LM) method for training the system to have a more accurate response. The designed ANN identified and predicted the displacement of the movable mass of the accelerometer. The simulation results were very promising.

The neural network is a good method to predict the response with very high accuracy. The response of the device using cubic stiffness is more accurate, therefore, the ANN acts better than the linear model.

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