



Dyna

ISSN: 0012-7353

dyna@unalmed.edu.co

Universidad Nacional de Colombia
Colombia

Rueda-Parada, Jorge Enrique
Encryption using circular harmonic key
Dyna, vol. 82, núm. 190, abril, 2015, pp. 70-73
Universidad Nacional de Colombia
Medellín, Colombia

Available in: <http://www.redalyc.org/articulo.oa?id=49637154009>

- How to cite
- Complete issue
- More information about this article
- Journal's homepage in redalyc.org

redalyc.org

Scientific Information System
Network of Scientific Journals from Latin America, the Caribbean, Spain and Portugal
Non-profit academic project, developed under the open access initiative

Encryption using circular harmonic key

Jorge Enrique Rueda-Parada

Grupo Óptica Moderna, Facultad de Ciencias Básicas, Universidad de Pamplona, Pamplona, Colombia. jorgeenriquierueda@gmail.com

Received: April 2th, 2014. Received in revised form: February 2 th, 2015. Accepted: February 20th, 2015

Abstract

This work presents a study of variance to rotation key encryption processors based on the Fourier transform. It was determined that the key in rectangular coordinates allows a tolerance level of less than 0.2 degrees of rotation of the key in the decryption process. Thus, the solution is to build the key in polar coordinates, by means of circular harmonics expansion; in this way, the tolerance threshold rises to about 40 degrees of rotation of the key in the decryption process. This solution is an added value for optical encryption processors. I have developed a computational tool for simulations and results obtained in this study.

Keywords: Cryptography, Circular harmonics, Fourier optics.

Encriptación usando una llave en armónicos circulares

Resumen

En este trabajo presento un estudio sobre la varianza a la rotación de la llave del procesador de encriptación basado en la transformada de Fourier. Determiné que la llave en coordenadas rectangulares permite un nivel de tolerancia inferior a 0.2 grados de rotación de la llave en el proceso de decriptación. Entonces la solución es construir la llave en coordenadas polares, por medio de una expansión en armónicos circulares. De esta manera, el umbral de tolerancia aumenta aproximadamente hasta 40 grados de rotación de la llave en el proceso de decriptación. Esta solución es un valor agregado para el procesador de encriptación óptico. He desarrollado una herramienta computacional para las simulaciones y resultados obtenidos en este estudio.

Palabras clave: Criptografía, Armónicos Circulares, Óptica de Fourier.

1. Introduction

Using optical processor encryption based on the Vander Lugt Correlator (VLC) [1], the image is encrypted due to the encryption key located on Fourier plane [2,4,5,6,9,10]. This processor uses a phase only key with random spatial distribution of the phase. Fig. 1 shows the optical arrangement encryption-decryption based on the VLC.

Encryption techniques should have two equally important features: 1) resistance to attacks on the encrypted information, and 2) they should allow recipient to decrypt the information without difficulty. In previous works [6], we implemented this type of encryption arrangement using the encryption-keys in rectangular coordinates $K(u, v)$. Then, we observed that the decryption is a variant operation with the rotation of the key. In practice, this variance is a problem that needs to be solved. I propose a solution to the problem using a decomposition of the key in circular harmonics.

Fig. 2 shows a result of variance of the decryption operation with the rotation of a key in rectangular

coordinates. A rotational variance encryption processor, due to rotation of the key may be measured in terms of the IOR parameter given by eq.(1):

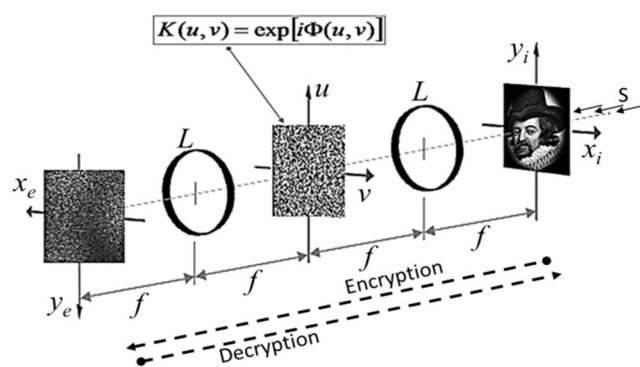


Figure 1. Experimental arrangement VLC to encryption-decryption. L are the convergent lenses of focal length f . Input plane (y_i, x_i) ; encryption plane (y_e, x_e) . S is a plane wave.
Source: The author.

$$IOR = 10 \times \log_{10} \left[\frac{\langle f(x,y) \rangle}{\langle f_d(x,y) \rangle} \right], \quad (1)$$

$$f_d(x,y) \approx f(x,y) * \{K_e(x,y) \otimes K_d(x,y)\}, \quad (2)$$

Where, $f(x,y)$ is the input image and $f_d(x,y)$ is the decrypted image, $K_e(x,y)$ is the encryption key, and $K_d(x,y)$ is the decryption key. $*$ is the convolution operator and \otimes is the correlation operator. If $IOR = 0$ dB, meaning that the output image $f_d(x,y)$ is approximately equal to the input image. Analyzing eq.(2), the system will decrypt only if $K_e(x,y) = K_d(x,y)$, then the operation $K_e(x,y) \otimes K_d(x,y)$ generates an autocorrelation peak that does not distort the image $f_d(x,y)$. But if we rotate the key $K_d(x,y)$, then the result of the $K_e(x,y) \otimes K_d(x,y)$ correlation will be a noise, which is convolved with the image $f(x,y)$, and therefore the result is a distorted image. In this work, it was determined that the level of this distortion depends on the angle of rotation of the decryption key $K_d(x,y)$. This occurs because the correlation product is variant with rotation functions.

The results shown in Fig. 2 correspond to a key in rectangular coordinates, and Fig. 3 is the corresponding calculation of IOR vs the rotation angle of the same key. Note that rotation of 0.2 degrees, corresponds to a value of $IOR = 1.25$ dB, which corresponds to the image in Fig. 2(e), and here it is observed that $f(x,y)$ is highly distorted. Now,

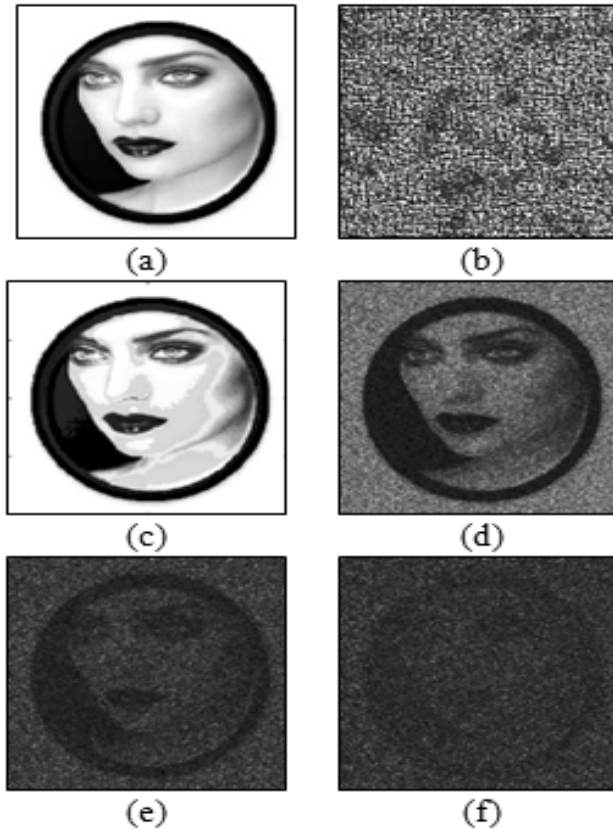


Figure 2. Encryption-Decryption using a key $K(u,v)$. (a) Input image; (b) Encrypted image; (c) Decrypted image with $K(u,v)$ rotated 0° ; (d) Decrypted image with $K(u,v)$ rotated 0.1° ; (e) Decrypted image with $K(u,v)$ rotated 0.2° ; (f) Decrypted image with $K(u,v)$ rotated 0.3° . Source: The author.

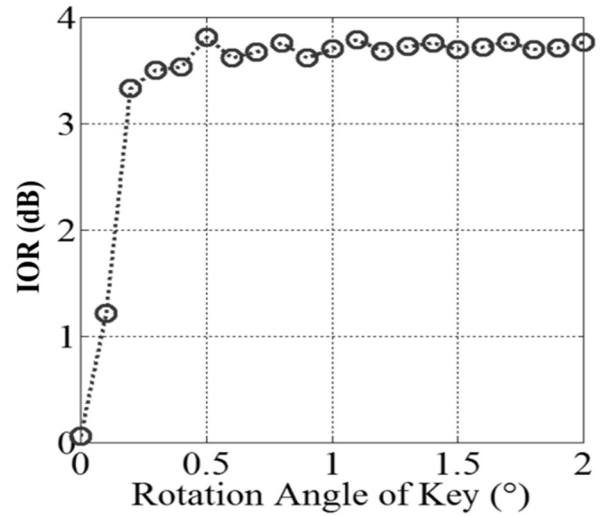


Figure 3. IOR of the decrypted image with the rotation of the key $K(u,v)$. Source: The author.

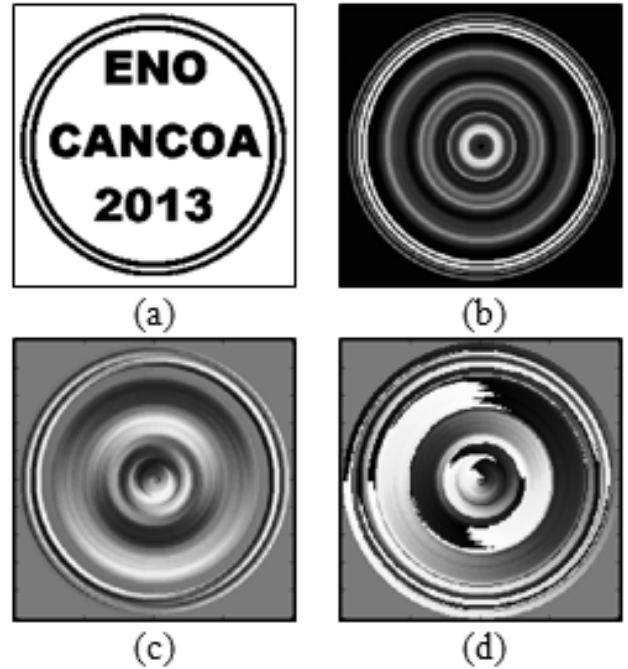


Figure 4. Circular harmonic expansion $m = 1$ of (a) image. (a) $f(x,y)$ image in rectangular coordinates; (b), (c) and (d) are amplitude, real part and phase, respectively, of the circular harmonic component of $f(x,y)$. Source: The author.

for angles greater than 0.2 degrees, the level of distortion is such that there is no decrypted image, as with the result in Fig. 2(f). The solution is then decomposed into harmonic circular key, and thus the operation of decryption increases tolerance to rotation of the key $K_d(x,y)$. Furthermore, we can use IOR as a relative measure of the level of distortion of the decrypted image. Thus, we can see in Fig. 3 that as we increase the angle of rotation of the $K_d(x,y)$ key, the value of IOR increases.

2. Encryption with circular harmonic key

An image can be expressed in polar coordinates for circular harmonic components [7,8]. Then we can consider the key in polar coordinates, so the key takes the form $K(\rho, \phi) = \exp[i\Phi(\rho, \phi)]$, where Φ must contain a distribution of random values. Thus, the key can be decomposed into harmonic circular, as follows:

$$\Phi(\rho, \phi) = \sum_{m=-\infty}^{\infty} \Phi_m(\rho) \exp[im\phi], \quad (3)$$

With,

$$\Phi_m(\rho) = \frac{1}{2\pi} \int_0^{2\pi} \Phi(\rho, \phi) \exp[-im\phi] d\phi, \quad (4)$$

Then, the key is defined as:

$$K_m(\rho, \phi) = \exp[i\Re\{\Phi_m(\rho, \phi)\}]. \quad (5)$$

Where $\Re\{-\}$ is the real part of Φ_m . Fig. 4 is an example of decomposition into circular harmonics of $m=1$ order. Fig. 5 shows the decomposition of $m=1$ order, of an encryption key given in rectangular coordinates in Fig. 5(a).

2.1. Encryption-Decryption results with circular harmonics key

The block diagram of the cryptography system (Fig. 6) was implemented in Matlab(R2012b). Fig. 7 is a result of encryption-decryption using a key $K_m(\rho, \phi)$ (Fig. 5). These results indicate that the decryption operation increased the level of tolerance with respect to the case of the key in rectangular coordinates.

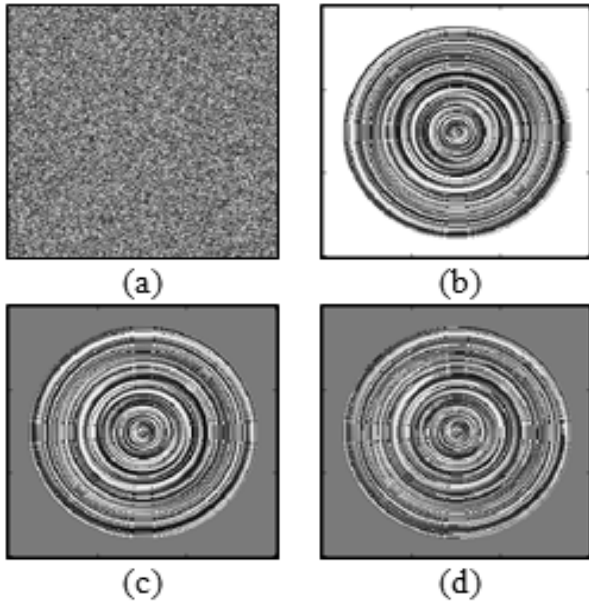


Figure 5. Circular Harmonic Expansion $K_m(\rho, \phi)$ of (a) with $m=1$. (a) Phase of $K(u, v)$; (b) Real part of $K_l(\rho, \phi)$; (c) Imaginary part of $K_l(\rho, \phi)$; (d) Phase of $K_l(\rho, \phi)$.

Source: The author.

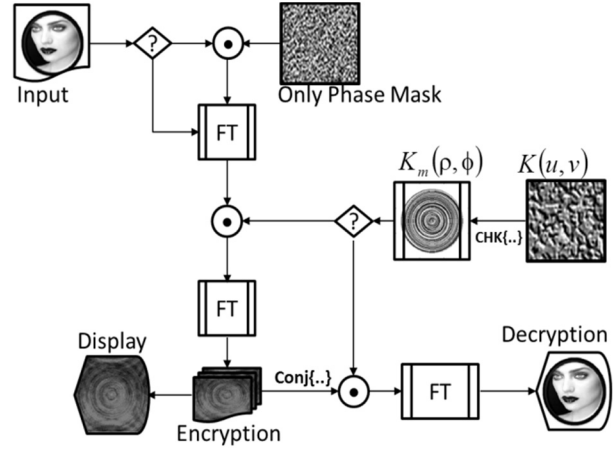


Figure 6. System block diagram, encryption-decryption, using the Fourier Transform and harmonic decomposition. • is the multiplication operator. FT is the Fourier Transform operator. Source: The author.

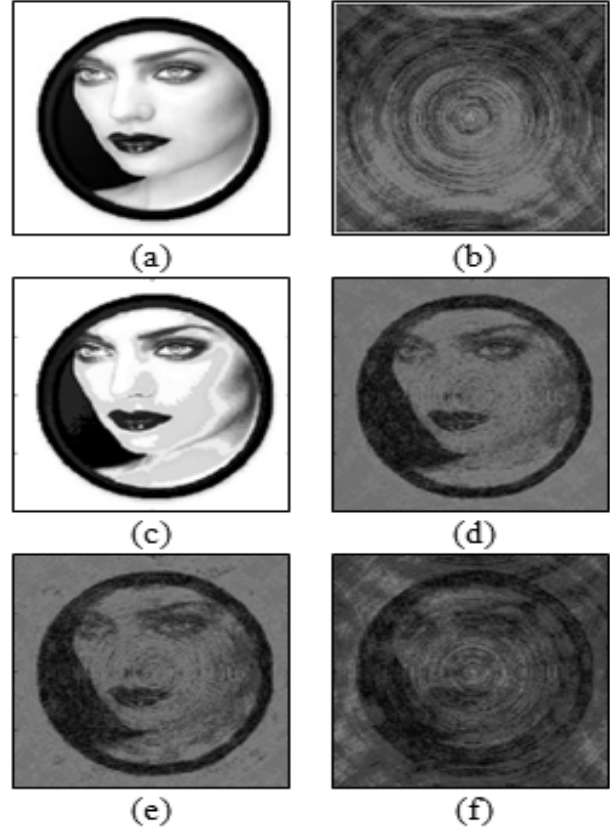


Figure 7. Encryption-Decryption using a key $K_l(\rho, \phi)$. (a) input image; (b) Intensity of the encrypted image; (c) decrypted image with $K_l(\rho, \phi)$ rotated 0°; (d) decrypted image with $K_l(\rho, \phi)$ rotated 5°; (e) decrypted image with $K_l(\rho, \phi)$ rotated 10°; (f) decrypted image with $K_l(\rho, \phi)$ rotated 50°.

Source: The author.

Fig. 7(b) shows the intensity of the encrypted image. Note that the intensity of the encrypted image has the appearance of a deterministic image. However, the values are totally random (see Fig. 8). The output of the processor

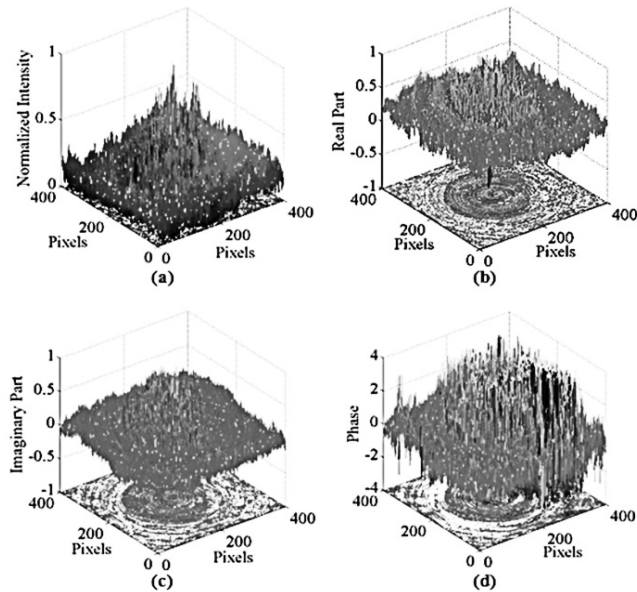


Figure 8. Distribution of values of the encrypted image: (a) $|f_e(x,y)|^2$ (Figure 7(b)), (b) Real $\{f_e(x,y)\}$, (c) Imag $\{f_e(x,y)\}$, and (d) Phase distribution. Source: The author.

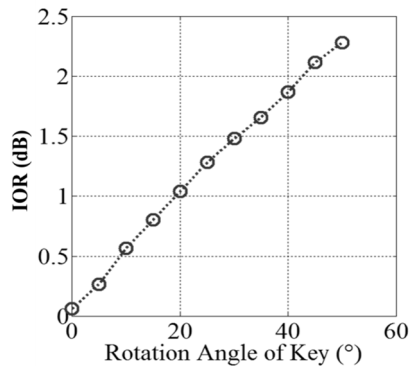


Figure 9. IOR of the decrypted image with the rotation of the key $K_I(\rho, \phi)$. Source: The author.

delivers an array of complex values. So the encrypted image is composed of three parts: a real values matrix, an imaginary values matrix and a phase matrix.

Fig. 9 is the relationship IOR between rotation angles of the decryption key. This analysis corresponds to Figs. 7(c)-(f). Note that for an output of IOR = 2dB, a rotation of the key ≈ 41 degrees is necessary. Thus, tolerance decryption operation is much higher with respect to the key in case of rectangular coordinates. So then encryption with keys in polar coordinates is a solution to the problem of variance in the decryption of the optical arrangements, and is also useful for fully digital encryption.

The order of the harmonic decomposition can be handled as an additional variable that increases the difficulty of breaking the encryption information.

3. Conclusions

In sum, this study show that the encryption processor based on the Fourier transform is a variant with key

rotation. It was demonstrated that a solution to this variance is to expand the key into circular harmonics. The proposed technique increases the tolerance of the processor with the rotation of the key. The key in rectangular coordinates allows a tolerance to rotation of about 0.2 degrees, while with the key in circular harmonics, tolerance increases to about 40 degrees. Thus, the decomposition of the key circular harmonics solves the particular problem of optical encryption processor based on the phenomenon of diffraction, because the decryption key must be physically positioned with high accuracy, as can be concluded from the simulation results presented in this report.

Furthermore, the proposed technique can also be used in digital encryption algorithms, considering that the encrypted image is not deterministic, as it appears to be if only the appearance of the encrypted image is observe. If we analyze the distribution of values of the amplitude and phase of the encrypted image, we find that these are really random. Failing that, the quality of the image encrypted with the key in circular harmonics can be an element of distraction to break the code attacks.

References

- [1] Vanderlugt, A., Signal detection by complex spatial filter, IEEE IT-10, pp.139-146, 1964.
- [2] Refregier, P. and Javidi, B., Optical image encryption based on input plane and Fourier plane random encoding, Opt. Lett. 20 (7), pp.767-769, 1995. <http://dx.doi.org/10.1364/OL.20.000767>
- [3] Matoba, O. and Javidi, B., Encrypted optical storage with angular multiplexing, Appl. Opt. 38 (35), pp.7288-7293, 1999. <http://dx.doi.org/10.1364/AO.38.007288>.
- [4] Lin, C., Shen, X., Tang, R. and Zou, X., Multiple images encryption based on Fourier transform hologram, Opt. Commun. 285 (6), pp.1023-1028, 2012. Doi: 10.1016/j.optcom.2011.10.046
- [5] Tebaldi, M., Furlan W.D., Torroba, R. and Bolognini, N., Optical-data storage-readout technique based on fractal encrypting masks, Opt. Lett. 34 (3), pp. 316-318, 2009. <http://dx.doi.org/10.1364/OL.34.000316>
- [6] Rueda, J.E. and Romero, A.L., Optical cryptography using Fresnel diffraction and phase conjugation, Revista DYNA. Facultad de Minas, Universidad Nacional de Colombia, Sede Medellin, Colombia, 80 (181), pp. 25-30, 2013.
- [7] Hsu, Y.N., Arsenault, H.H. and April, G., Rotation-invariant digital patten recognition using circular harmonic expansion, Appl. Opt. 21(22), pp. 4012-4015, 1982. <http://dx.doi.org/10.1364/AO.21.004012>
- [8] Gualdrón O. and Arsenault H.H., Phase derived circular harmonic filter, Opt. Commun. 104(1-3), pp.32-34, 1993. doi:10.1016/0030-4018(93)90100-J
- [9] Hennelly, B. and Sheridan, J.T. Optical image encryption by random shifting in fractional Fourier domains. Optics Letters 28(4), pp.269-271, 2003. <http://dx.doi.org/10.1364/OL.28.000269>
- [10] Salazar, A., Rueda, J.E. and Lasprilla, M., Encriptación por conjugación de fase en un BSO utilizando señales ópticas de baja potencia, Revista Colombiana de Física 34 (2), pp.636-640, 2002.

J.E. Rueda-Parada, completed his BSc in Physics in 1993, an MSc Physics in 1996, and a PhD Physics in 2002, all of them from the Universidad Industrial de Santander, Colombia. He finished his postdoctoral studies in February 2015, at the Institute of Physics of São Carlos, University of São Paulo, Brazil. Currently, he is a full Professor at the Physics Department, Faculty of Basic Sciences, Universidad de Pamplona, Colombia. His research interests include: growth of mono-crystalline fibers, photorefractive optics, holography, wave mixing, and optical encryption and digital image processing.