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# Uplift force and momenta on a slab subjected to hydraulic jump

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## Abstract

As part of the search for safe and economic design criterion to line slabs of stilling basins, the present study is one of the first to calculate the center of pressure, uplift forces, and momenta from a spatiotemporal analysis of the pressures measured above and below instrumented slabs in a physical model. Controlled release of the waterstops, and variation in the dimensions of expansion joints and in the gap between foundation and the lining slab were carried out in order to consider their effects on the magnitudes of uplift forces and momenta. An offset of the center of pressure from the slab's center of gravity was identified. The objective of this work was to consider the failure mechanism induced by momentum in the slab's design. Design criterion to make the lining slab's thickness to length between 6 and 12 times the incident flow depth, is proposed, and this is compared to other design criteria.

**Keywords:** Uplift pressure; hydrodynamics uplift; slabs, physical model; stilling basins; hydraulic jump.

# Fuerza de levantamiento y momentos en una losa sometida a salto hidráulico

## Resumen

Buscando un criterio de diseño seguro y económico para las losas de los tanques de amortiguación, se calcularon fuerzas de levantamiento, centros de presión y momentos a partir de un análisis espacio-temporal de las presiones medidas encima y debajo de losas instrumentadas en un modelo físico. La liberación controlada de los sellos y la variación en las dimensiones de las juntas y de la separación entre la cimentación y la losa, fueron realizadas para considerar sus efectos sobre la fuerza de levantamiento y los momentos. Se identificó desplazamiento del centro de presión respecto al centro de gravedad de la losa. Para considerar el mecanismo de falla inducido por el momento en el diseño de losas, objetivo del trabajo, se propone un criterio de diseño para el espesor equivalente de las losas con longitudes entre 6 y 12 veces la profundidad del flujo incidente y se compara con otros criterios.

**Palabras clave:** Presiones de levantamiento; levantamiento hidrodinámico; losas; modelo físico; tanques de amortiguación; salto hidráulico.

## 1. Introduction

Outlet works conduit typically requires dissipation of excess kinetic energy to prevent downstream channel erosion as this flow often discharges at a high velocity. An energy dissipator, such as a stilling basin, is used to retard the fast moving water by creating a hydraulic jump [1]. The design of an energy dissipating structure need criteria to avoid cavitation, abrasion, internal erosion, hydrodynamic uplift, etc.

Historical reporting of the failure of slabs in flumes and

stilling basins, with an equivalent thickness ranging from 0.3 m to 4 m, has show the hydrodynamic uplift to be a structural design problem [2-5]. Equivalent thickness is the real slab thickness, and anchors are defense against uplift.

Since the early 60s, design criteria for lining slabs to calculate the uplift force and equivalent thickness have been proposed. The most recognized design criteria were based on stochastic analysis of the pressure and force fluctuations at the floor of the hydraulic jump in a physical model [6-10]. A summary of the criteria can be found in references [11-12]. They determine the uplift force taking into account the length

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(L) and width (W) of the slab. Researchers agree with the criteria that the length of the slab in direction of flow has an inverse relation to the uplift force [6,7,9,10,12]. However, there is no complete agreement as to the slab's width influence on the uplift force. Bellin and Fiorotto [10] suggest building the slab with the minimum width technically possible, and other criteria indicate otherwise [8,9,12].

There are differences between design criteria due to simplifications in the physical and conceptual models that were supported. For the same condition, the slab's equivalent thickness that was calculated using existing criteria shows large differences. Thus, it is difficult to choose criteria that guarantee the stability of the slab with the lowest cost and, generally, the designer chooses the more conservative criteria. According to Khatsuria [11], the vast variation between criteria points to the fact that this science is still in an evolutionary stage. While Bollaert [13] expressed that *"despite major advances in measurement technology and data acquisition, a safe and economic design method for any kind of concrete lined stilling basin is still missing today. Especially the dynamic or even transient character of pressure pulsations as a function of their two-dimensional spatial distribution above and underneath the lining is not fully assessed and implemented in existing design methods."* [13].

In addition, the physical models that supported the design criteria were not simulated in their true scale joints, waterstops, slab thickness ( $s$ ), and gap between soil foundation and the concrete slab ( $\delta$ ) since the pressure drop through the joints to the foundation was depreciated. In the prototype, gap  $\delta$  and width joint ( $\varepsilon$ ) can change by sources of natural movement, internal erosion, etc. Furthermore, the position and number of sensors reported by the references [6-10] were not sufficient to be able to accurately estimate both the uplift force and its center of pressure.

To date, the evidence suggests that hydrodynamic uplift is also influenced by the interaction of fluid with joint and detachment of the waterstops [13-19]. However, these factors have not been considered in the design criteria of the slab subjected to a hydraulic jump with horizontal aprons.

Previous work was observed in which joints and waterstops act as pressure filter fluctuations generated in the flume [18]. Also, the joints generate a time delay between the entry of the pressure wave at the joint and its arrival below the slab. It leads to the pressure differential between top and bottom of the slab and, therefore, the uplift force emerges. The interactions between the joints and the main stream alter the amplitude of pressure wave below the slab. Joints and waterstops promote pressure generating pressure gradients below the slab and some instants, the pressure gradients will have positive or negative linear correlation. With only one open transversal joint, the pressure below the slab was uniform. With two or more open joints, pressure gradients below the slab were generated.

No uniformity in pressure over a slab leads to the consideration of the failure mechanism induced by momentum of force. If a slab turns a little due to momentum, offset between slabs occurs and the stagnation point increases the uplift pressure and drag force. Failure or loss of intimate

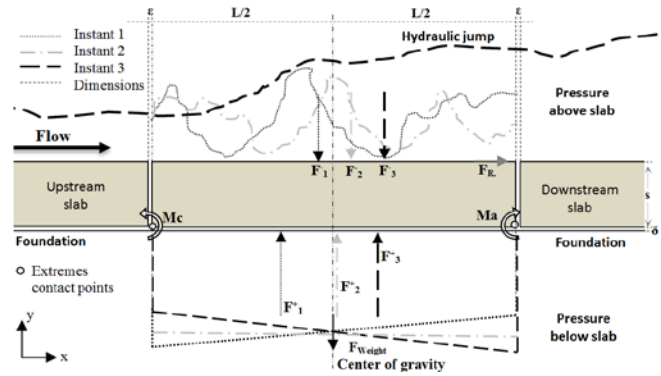


Figure 1. Force and momentum diagram of a slab in three instants.  
Source: The author

contact with the soil is typically the result of a slab overturning its downstream contact point [1]. The forces of interest in a momentum balance are slab weight ( $F_{\text{weight}}$ ), strength of the anchors, the resultant forces  $F^+$  and  $F^-$  of field pressure acting on the surface above and below the slab, and drag force ( $F_R$ ). The net uplift force ( $F_{\text{net}}$ ) is a vector sum of the forces  $F^+$  and  $F^-$ , which could have a center of pressure in a different coordinate to the center of gravity of the slab that changes over time (Fig. 1).

Therefore, in this study the author determined the forces  $F^+$ ,  $F^-$  and  $F_{\text{net}}$  from a spatial integration of pressure fields and balance forces. The author established the pressure fields from measured pressures with multiple sensors above and below a slab that was subject to hydraulic jump. The center of pressure to be able to calculate the momenta of force  $F^+$  and  $F^-$  was also identified, and the momentum  $M_a$  in terms of the downstream contact point of the slab, and the momentum  $M_c$ , in terms of the upstream contact point of the slab (Fig. 1) was calculated. The author also contemplated the variation of magnitude of the force  $F^+$  and its center of pressure by the joints, the damage of the waterstops, and the variation of gap  $\delta$  and  $\varepsilon$ .

Multiple tests including physical and hydrodynamic variations were evaluated. They were analyzed and helped improve the understanding of the uplift hydrodynamic of the lining slabs. The author present the design criterion that has an equivalent thickness of the slabs with lengths between 6 and 12 times the depth of the incident flow. This paper is based on the author's PhD thesis [18].

## 2. Materials and methods

Pressures were measured above and below slabs in a physical model that was made in the Hydraulic Laboratory at the "University of Valle" in Cali, Colombia (Fig. 2). The physical model contains slabs fixed under the horizontal flume floor at different distances from the load tank. The flume was 0.5 m high, 8m long, and 0.35 m wide. The slab and its details such as expansion joints, slab thickness, gaps  $\delta$ , and  $\varepsilon$ , were simulated with several acrylic boxes with dimensions from largest  $((L+2\varepsilon)*(W+2\varepsilon)*(s+\delta))$ , internal dimensions) to smallest  $(L*W*s)$ , external dimensions; Table 1; Figs. 1, 2).

Table 1.

Slab type, dimensions (mm) and sensors distribution (D).

Slab type	L	W	s	$\epsilon$	$\delta$	D	# tests
S1A	280	150	30	2	0.5	D1	58
S1A*	280	150	30	2	0, 0.2, 1	D1	180
S1B	294	156	34	0.5	0.5	D2	70
S2	299	160	37	1	1	D2	56
S3	299	160	38	1.5	1	D2	56

Source: The author

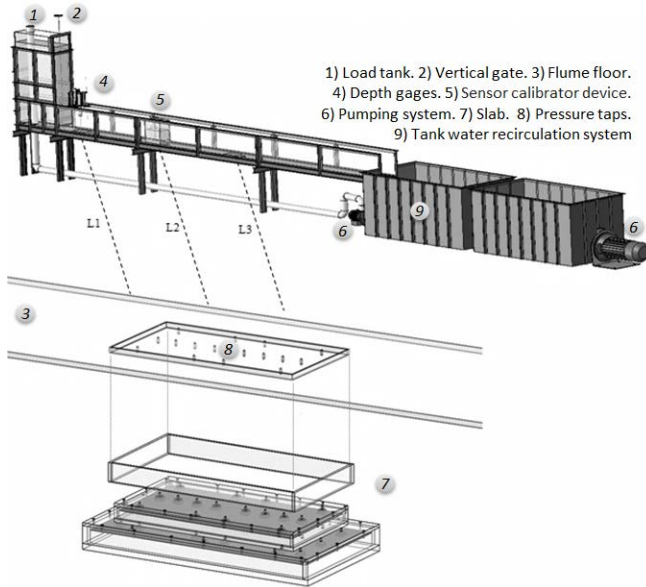


Figure 2. Physical model.

Source: Adapted from [18]

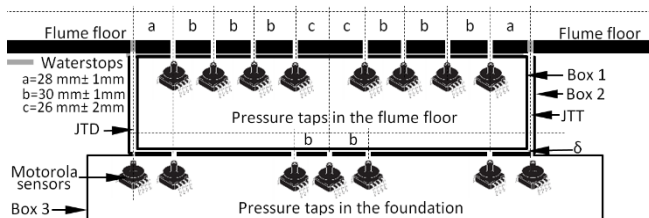


Figure 3. Lateral section of the slab on the x axis

Source: The author

The length ( $L$ ) of individual slabs ranged from 6 to 12 times the incident flow depth ( $y_1$ ), and the slab's width was approximately half its length. The gap  $\delta$  was possible by interposing aluminum sheet rings 1 mm in diameter and thickness that were required to achieve the desired separation.

The flume floor was drilled and slotted to provide continuity to pressure taps and joints (Fig. 3). The model slabs were fixed to the basin to prevent motion. The coupling between elements in the system was monitored to avoid stagnation points by the offset between edges, as was recommended and studied in references [19-20]. The offset was estimated to be  $10^{-5}$ m. This could be the case for the prototype due to imperfections in the finishing of the slabs and their rearrangement by natural movement.

The flow entering the hydraulic jump was full and partially developed with a Reynolds number in the boundary layer ( $Re_x$ ) between 300,000 and 17,380,000. The first slab (S1) was located at a distance at which the  $Re_x$  was between 300,000 and 660,000 (transition), the second slab 2 (S2) was in the area of  $Re_x$  between 4,150,000 and 9,130,000, and the third slab (S3) was the farthest from the load tank with  $Re_x$  between 7,900,000 and 17,380,000. The experimental design varied the state of development of the boundary layer since the magnitude of pressure fluctuation depended on whether the flow is fully developed or undeveloped [11]. However, the flow regime was always turbulent with Reynolds numbers between 90,000 and 200,000. Incident flow velocities ( $V_1$ ) ranged from 1.65 and 5.76 m/s.

The pressure was measured with 32 Motorola sensors (MPXV 4006GC7U, range 0-6 kpa and accuracy  $\pm 5\%$ ) and with circular pressure taps of 2 mm in diameter above and below the slab with two distributions (Fig. 4). The first sensors distribution (D1) selected 16 pressure taps above and below the slab that had an equal distribution (Fig. 4a, sensor symbol "●" and "■"). The second sensors distribution (D2) selected 8 pressure taps that were located above the slab in the central line (Fig. 4a; sensor symbol "●"). When these sensors failed, the pressure taps next to the longitudinal joint were used (Fig. 4a; sensor symbol "■"). Furthermore, 24 pressure taps below the slab and the bottom of the joints were implemented to achieve a higher resolution of the pressure field (Fig. 4b; sensor symbol "◆").

Every five working hours, in accordance with the methodology proposed in the reference [21], the pressure measurement system was dynamically calibrated, and dynamic uncertainty was, on average, 8.82%. The signs that

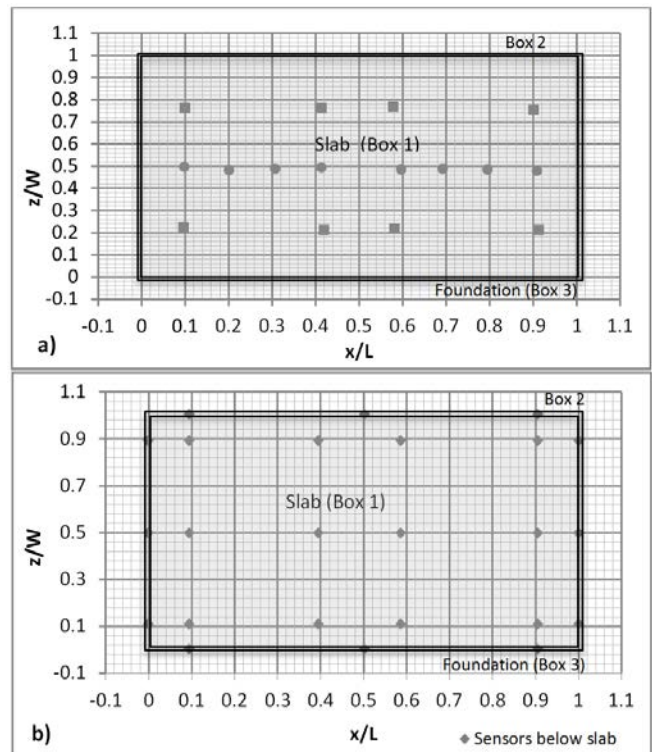


Figure 4. The expansion joints and two sensors distributions

Source: The author

were acquired with a data acquisition system (DAQ National Instruments, NI SCXI: 1000, 1102B, 1600, 1300) were sent to a laptop. The sampling frequency ( $f_s$ ) was 200 Hz and was limited by the data acquisition system available. In addition, it held the sampling theorem (avoiding aliasing) and improved the resolution in the time of the digitized signal (5 ms). In signal processing, a median digital filter was used to remove frequency components that were not part of the phenomenon since it closely recovers the original signal while removing noise [22]. According to the analysis of the frequency signal and the dynamic characteristics of the pressure measurement system, the cutoff frequency of the digital filter was 10.5 Hz (window median filter equal to nineteen). Thus, the typical overshoot of the pressure measurement system in response to a sudden change of pressure (pressure fluctuation) was minimized. "Overshoot is the amount of output measured beyond the final steady output value in response to a step change in the measurand" [23].

In each test, the slab type (S1A, S1A\*, S1B, S2, and S3: Table 1), the open joint(s), and the  $Fr_1$ , were selected. Hydrodynamic variations included a minimum seven different  $Fr_1$  between 2.3 and 10 for each physical variation.

Physical variations include the controlled release of the waterstop(s) in: a) one of the four joints, front transverse joint (FTJ), rear transverse joint (RTJ), or longitudinal joint (LJ); b) two joints simultaneously, longitudinal joints (LJ), or transverse joints (TJ); c) all joints (AJ).

The flow depth was measured on a) FTJ, b) LJ in the middle of the slab, c) RTJ. At each point, the minimum and maximum depth detected in 30 seconds were measured with depth gages that had a 300 mm range and an accuracy of  $\pm 0.2$  mm. The discharge was regulated between 8.15 and 14.1 Gallon/min, as was the vertical gate of the load tank (1.8m high, 1m long and 0.35 m wide) between 2.5 and 5.5 cm. The discharge was measured from an Omega flow meter (FMG-901). The flow rate was measured with a Prandtl tube at a point located 0.05 m upstream of the front transverse joint, and the measurement error was 4%.

The test was run over 15 minutes and the data acquisition was performed during in the last five minutes. Data acquisition time was mainly associated with extensive data and the number of tests explored (420). One test had 60,000 discrete samples in which the pressure fields were analyzed.

The hydraulic jump with rectangular weirs of heights ranging from 5 to 20 cm at the end of the flume was induced. Because, in general, the highest pressure fluctuations are reported in the first third of the length of the free hydraulic jump [8,24-30], the slabs were located under 30% of its length. Some tests in the slab "S1" had a submerged hydraulic jump.

### 3. Data processing and results

This researcher evaluated each sampling instant from the 58 test samples that had an S1A configuration, the forces  $F^+$ ,  $F^-$ ,  $F_{net}$ , their center of pressure over the slab surfaces, and the momenta  $Ma$  and  $Mc$ . Using data processing, the pressure fields from the pressure measured above and below the slab in each sampling instant were adjusted. According to the theory of Riemann integration, to obtain the total force

vectors  $F^+$  and  $F^-$  (eq. 1 and eq. 2), the area of slab was discretized and the sum of the partial pressures was computed.

$$F^- = \iint P^-(x,y) dx dy = \Delta x \Delta y \sum P^-(x,y) \quad (1)$$

$$F^+ = \iint P^+(x,y) dx dy = \Delta x \Delta y \sum P^+(x,y) \quad (2)$$

Where,  $P^-$  and  $P^+$  are the pressures above and below the slab's surfaces.  $\Delta x \Delta y$  ( $L/186 \times B/115$ ) are area elements in which the slab area ( $A_L$ ) was discretized.

The x-coordinate of center of pressure (intersection of the resultant force and the surface's line of action) was obtained with eq. 3.

$$\bar{X} = \frac{\sum P^{\pm}(x,y)x_i}{\sum P^{\pm}(x,y)} \quad (3)$$

Where  $x_i$  is x coordinate of the center of the differential element of area.

The forces  $F^+$  and  $F^-$ 's centers of pressure were different to their centers of gravity, which affect momenta that induce rotation of the slab. The offset percentage of the center of pressure from the center of gravity in x-coordinate was calculated using eq. 4 (Fig. 5).

$$\text{offset}_{xc}(\%)^{+/-} = \frac{(x_c - \bar{X})}{x_c} * 100 \quad (4)$$

Where  $x_c$  is x-coordinate of the slab's center of gravity (or centroid).

The author calculated the momenta balances with respect to the slab's extreme contact points. The clockwise momentum was positive. The  $F_{net}$  and net momenta ( $Ma_{net}$  and  $Mc_{net}$ ) determine the possibility of the slab's uplift or rotation (Fig. 1). Then, the maximum value of  $F_{net}$ ,  $Ma_{net}$ ,  $Mc_{net}$  in each test was selected and expressed in terms of net instability dimensionless coefficients ( $F_{NM}^*$ ,  $Ma_{NM}^*$ ,  $|Mc_{NM}^*|$ ; eq. 5 -7).

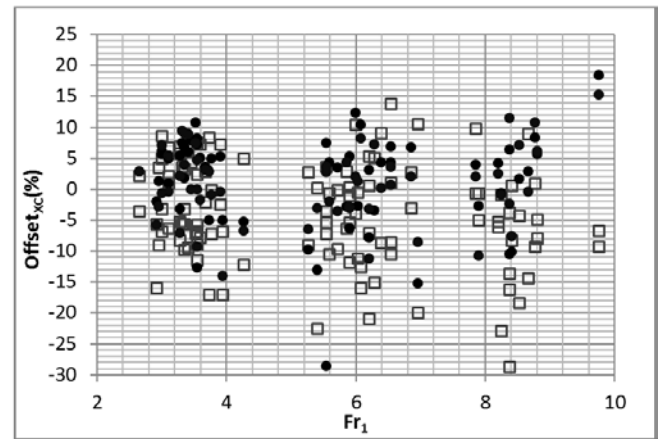


Figure 5. Offset percentage of the center of pressure from the center of gravity above ( $\square$ ) and below ( $\bullet$ ) the slab.

Source: The author



$$F_{NM}^* = \frac{F_{net}}{\gamma A_L V_1^2 / 2g} \quad (5)$$

$$Ma_{NM}^* = \frac{Ma_{net}}{x_c \gamma A_L V_1^2 / 2g} \quad (6)$$

$$Mc_{NM}^* = \frac{Mc_{net}}{x_c \gamma A_L V_1^2 / 2g} \quad (7)$$

Where  $\gamma$  is the specific weight of water and  $g$  is the gravity.

The coefficients  $F_{NM}^*$  were lower than the coefficient  $Ma_{NM}^*$  and  $|Mc_{NM}^*|$  (Fig. 6), which show that the mechanism of initial failure is the slab's rotation. The dotted boundary was called the enveloping curve of instability net coefficients ( $C_{net}$ ) and it will be used to predict the uplift hydrodynamic in the next subsection. Two values of  $|Mc_{NM}^*|$  that fall outside the area of the curve (Fig. 6). These values manifest the combination of a great uplift force with a great center of pressure offset from the center of gravity below the slab (Fig. 6).

To expand upon the above, the author analyzed the impact on uplift force of the variations of  $Re_x$ , the gap  $\delta$ , the gap  $\epsilon$ , and the controlled release of the waterstops. It was considered that these physical variables only affect pressure fields below the slab, i.e. the force  $F^+$ . Thus, in each sampling instant from the 420 tests we calculated the force  $F^+$  (eq. 2) and then expressed it in the form of a dimensionless coefficient, according to eq. 8.

$$F^* = \frac{F^+}{\gamma \bar{h} A_L} \quad (8)$$

Where  $\bar{h}$  was calculated as the average of three minimum depths measured on FTJ, LJ, RTJ with a baseline below the slab.

To avoid the mistake of basing the analyses on a spurious value, ten maximum values identified in each test were plotted (Figs. 7-10). For same Froude number, coefficient  $F^*$  varied as a result of pressure fluctuations of the hydraulic jump and the geometric variations made in each test.

The incidence of the state of development of flow over force  $F^+$  was not clear. The force  $F^+$  is proportional to the Froude number and, generally, it was lower than twice the average hydrostatic force below the slab ( $\bar{h}\gamma A_L$ ; Fig. 7).

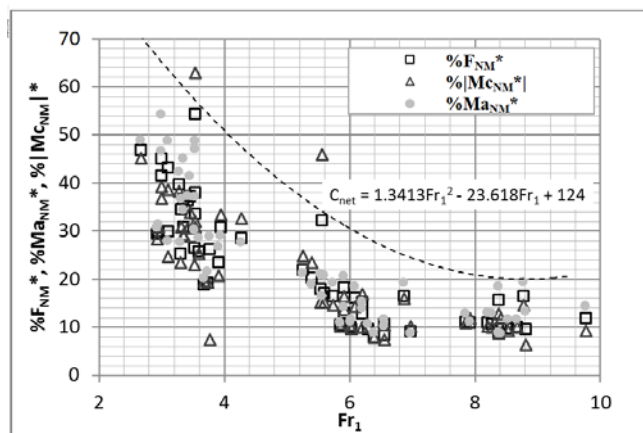


Figure 6. Net instability coefficients and their enveloping curve  
Source: The author

The effect on the force  $F^+$  by detachment of the waterstops, the change of the gaps  $\epsilon$ , and  $\delta$  can be deduced from Figs. 8-10. These showed the maximum  $F^+$  found in the different tests with S1 configuration and open transversal joints (Fig. 8), open longitudinal joints (Fig. 9), and all open joints (Fig. 10). Furthermore, a slab configuration with gap  $\epsilon$  of 0.5 mm and 2 mm; and gap  $\delta$  of 0.2 mm, 0.5 mm, and 1 mm was also considered

As a result of these tests, it is possible to say that the narrowest joint ( $\epsilon=0.5$  mm) induced a greater uplift force  $F^+$  (Fig. 8-10). Tests with open transversal joints induced major uplift forces under the slabs, and these were followed by tests with all open joints.

The incidence of gap  $\delta$  on uplift force was not clear. For the condition of open transverse joints an inverse relationship between the uplift force and the gap  $\delta$  was observed (Fig. 8).

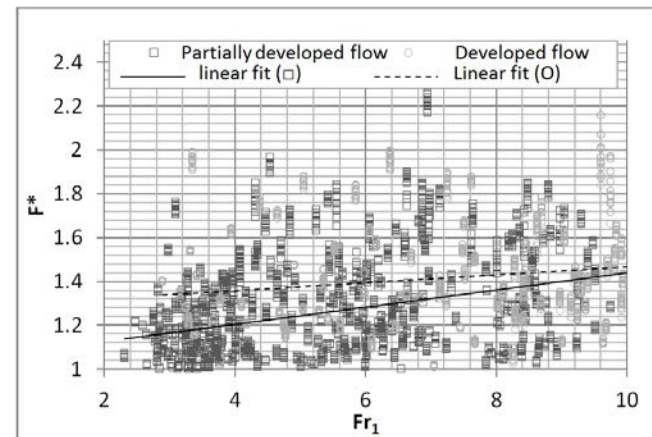


Figure 7. The tests' maximum force  $F^+$ .  
Source: The author

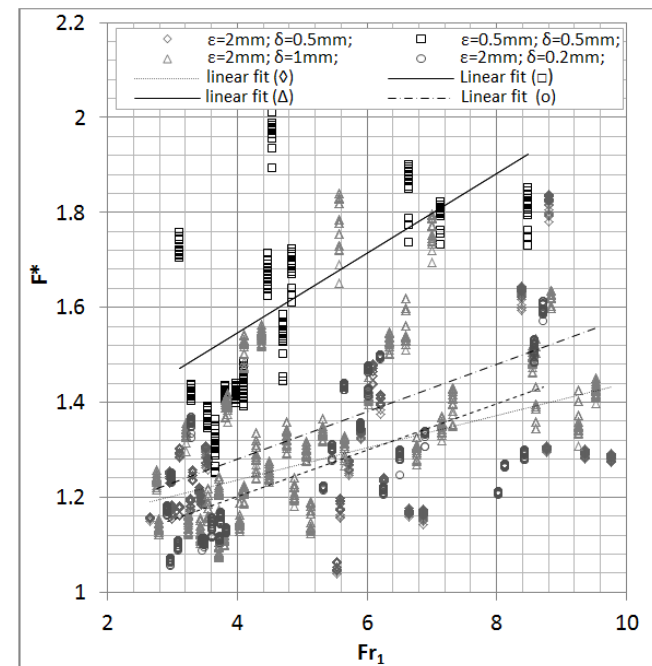


Figure 8. The maximum force  $F^+$  with open transversal joints  
Source: The author

However, occasionally the author identified a proportional relationship between  $F^+$  and gap  $\delta$  in tests with longitudinal joints or all open joints (Figs. 8, 9). The greatest uplift forces obtained from the combination of gap  $\varepsilon$  of 0.5 mm and gap  $\delta$  of 0.5 mm, and the results showed in references [15,16], led to us leaving the hypothesis open (narrower gap  $\delta$  leads to a hydraulic jack).

The study of net uplift force and its point of application showed that it is necessary to consider the equivalent thickness of lining slabs in design criteria as well as the failure mechanism induced by momentum. Also, detachment of the waterstops, the size and the orientation joints that have an effect on the uplift force, and consequently influence its momentum should also be considered.

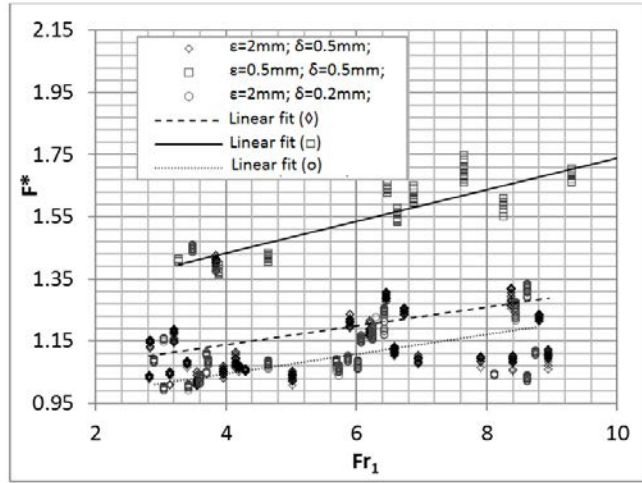


Figure 9. The maximum force  $F^+$  with open longitudinal joints  
Source: The author

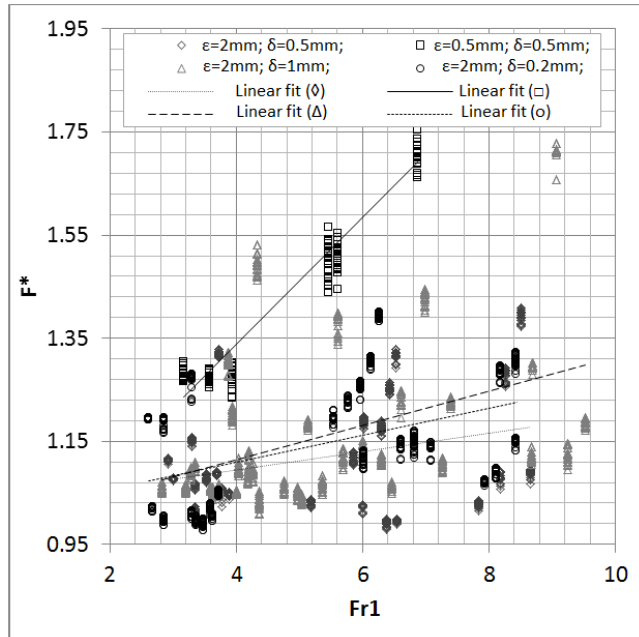


Figure 10. The maximum force  $F^+$  with all joint exposed.  
Source: The author

#### 4. Estimation of hydrodynamic uplift

The author proposes experimental tests and design criterion to estimate the equivalent thickness of a slab with lengths between 6 and 12 times the incident flow depth. The design of concrete slabs for hydrodynamic loading focuses on the determination of the maximum possible destabilizing force and momentum. In this criterion, uplift force and momenta are considered by the dimensionless design coefficient  $C_d$ , calculated by eq. 9.

$$C_d = C_{net} f_1 f_2 \quad (9)$$

Where,  $C_{net}$  is the instability net coefficients, which can be obtained from Fig. 6's envelope curve. " $f_1$ " is a dimensionless experimental coefficient that takes into account the increase of the force  $F^+$  and its momentum from the detachment of the waterstops, and the size and the orientation joints. " $f_2$ " is a dimensionless experimental coefficient that takes into account extreme instabilities.

To obtain the coefficients  $f_1$  and  $f_2$ , the force  $F^+$  found in each sampling instant from 420 tests was used to calculate the momenta  $Ma^+$  and  $Mc^+$ . The largest momenta  $Ma^+$  and  $Mc^+$  in each test were selected and expressed in form of dimensionless coefficients (eq. 10 and eq. 11).

$$Ma^* = \frac{Ma^+}{h\gamma A_L x_c} \quad (10)$$

$$Mc^* = \frac{Mc^+}{h\gamma A_L x_c} \quad (11)$$

The largest absolute value of the coefficients  $Ma^*$  and  $Mc^*$  in each test were identified and called coefficient  $M$  (eq. 12).

$$M = \text{Maximum}(|Mc^*|, |Ma^*|) \quad (12)$$

$M$  coefficients from 58 tests with an S1A configuration were added to the subscript  $r$  ( $M_r$ ). A curves adjustment over the maximum value of  $M_r$  and  $M$  vs.  $Fr_1$  was plotted (Fig. 11). The  $M$  curves that were proposed as lines ensured that the slope is always positive as the uplift force  $F^+$  is proportional to  $Fr_1$ . Furthermore, since the positive and negative maximum pressure

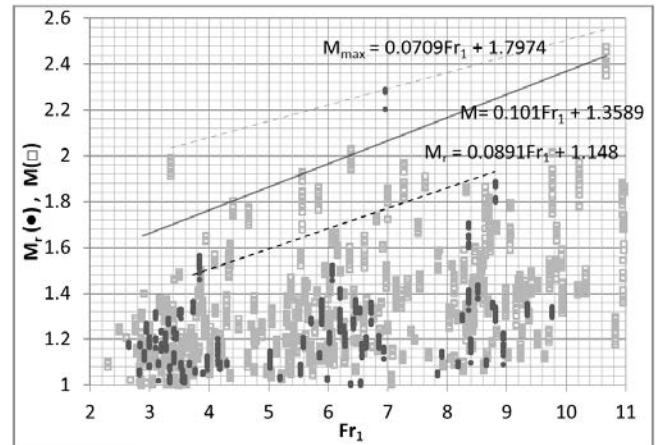


Figure 11. Maximum instability coefficients  $M_r$  and  $M$   
Source: The author

coefficient increases over time [8,27], the line fits the data conservatively to compensate for the short-time data acquisition (5 min).

The amplification factor  $f_1$  that depends on  $Fr_1$  is calculated according to equation 13 (Fig. 11).

$$f_1(Fr_1) = 1 + \frac{(M-M_r)}{M_r} = 1 + \frac{0.012Fr_1 + 0.2109}{0.0891Fr_1 - 1.148} \quad (13)$$

$M_{max}$  were associated with the extreme instabilities and the low probability of occurrence (Fig. 11). To determine the coefficient  $f_2$ , the same methodology used to determine  $f_1$  was implemented, and the M curve was compared with a curve fit to  $M_{max}$  (eq. 14, Fig. 11).

$$f_2(Fr_1) = 1 + \frac{(M_{max}-M)}{M} = 1 + \frac{(-0.0301Fr_1 + 0.2109)}{0.0891Fr_1 - 1.148} \quad (14)$$

The design coefficient in the  $Fr_1$  function is presented in Fig. 12. The buoyancy is considered by the design coefficient if the real thickness used in the prototype is less than the calculated thickness scaling model to prototype (Table 1). If the above are fulfilled, the thickness of the slab can be calculated with equation 15.

$$s = C_d \gamma V^2 / (\gamma_c 2g) \quad (15)$$

Where  $\gamma_c$  is the specific weight of concrete. In a scenario in which the slab could be immersed in a water-sediment mixture (for example, during the flushing of sediments from reservoirs), it is necessary to replace the specific weight of water by mixture ( $\gamma_m$ ). The above equation intends to compensate for the increase in the buoyancy force on the slab by the increased density of the mixture.

The slab thickness is most often selected empirically as achieving stability to resist uplift force alone with this parameter requires a heavy slab, and this is not always possible. In these cases, the methodology of equivalent thickness through the anchor should be used [31]. Slab thickness and the anchor could be calculated with eq. 16

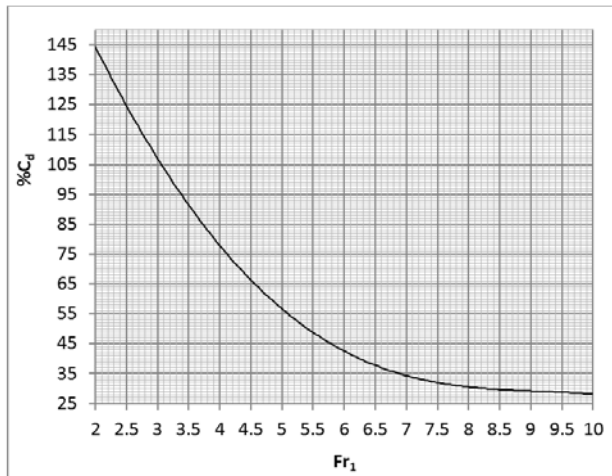


Figure 12. Coefficient  $C_d$  to estimate hydrodynamic uplift  
Source: The author

$$C_d A_L f_d \gamma_m V^2 / 2g = s \gamma_c A_L + 0.5 A_n \sigma_a n_a \quad (16)$$

The left side of eq. 16 is considered the hydrodynamic uplift. " $f_d$ " is the drainage coefficient, and it can be used as a means to theoretically reduce up to 50% of the pressure uplift ( $f_d = 0.5$ ; [32-33]). The right side of eq. 16 represents the forces that counteract the uplift force, including the weight of the concrete slab and the force that provides the anchor. Where, " $\sigma_a$ " is the tensile stress between steel-slab,  $n_a$  is the number of steel bars, and  $A_n$  is the area of the steel bar. For safety purposes, double the area of the anchor steel is assumed to design slabs in stilling basins [31].

Underdrains, anchors, cutoffs, and slab thickness are all provided to stabilize the slabs [32]. A slab that is about 600 mm thick is the minimum recommended [33], and this shall be determined by analyzing hydrostatic uplift and an elastic foundation analysis [32]. Uplift momenta and misalignment between slabs can be prevented by adding steel in the partial contraction deboned joint located the transversal joint (the joint with slip dowels). Thus, the deboned joint allows the expansion or contraction of the slab while the steel counteracts the shear loads void misalignment between slabs [32,34-35]. Also, safety reinforcement counteracts the momentum of force  $F_R$ .

## 5. Analysis

To ensure that the physical model represents the prototype, there must be geometrical, kinematic, and dynamic similarity [36-38]. Therefore, it is necessary to consider the effects of scale before using any lining slabs design criteria.

In hydraulic jump, when the large eddies are well reproduced in a model, the representation of turbulence is nearly achieved since the eddies are the energy carriers [11]. The large eddies in the turbulent flow are proportional to the principal dimension of the flow field, and they ensure correct simulation using a geometrically similar model [11]. The author recommends using a geometric scale more generous than 1:50 [36].

Viscous effects can lead to scale effects, especially in models based on Froude, for which the Reynolds number is always less than the prototype [11]. In tests with an  $Fr_1$  between 2.3 and 7.15, viscous effects and scale effects in terms of void fraction, bubble count rate, and bubble chord time distributions were overcome. Their influence was at least minimized since in the model the flow depth was greater than 30 mm, and there was a turbulent flow with Reynolds numbers greater than 100,000 [39,36-41]. When the physical model does not take into account the concentration of air in the evaluation of the pressures, it may require an additional safety factor. Pinheiro [25] found that increased air concentration decreases the mean pressure value and the standard deviation of force.

According to Lopardo *et al.* [29], the pressure data collected in a physical model with a free vertical gate system and horizontal flume can be extrapolated to sloping channels in hydraulic jump stilling basins. That is as long as the error is on the side of safety. Similarity law of fluctuating pressure spectrum in the strongly rolling area agrees with gravity law [41]. Thus, data from basic research provides pressure values



that are useful for stilling basin predesign, despite the limits in scale similarity.

Viscous and inertial forces dominate physical processes involving flow through small cracks or joints along a channel boundary [19]. The dimensions used to simulate the expansion joints (0.5 mm - 2 mm) lead us to suggest the use of a geometric scale more generous than 1:30. To establish similarity between the roughness implemented in the general contour of the model (coated in acrylic:  $n_{\text{Manning}} = 0.009$ ) and prototype (coated concrete:  $n_{\text{Manning}} = 0.014$ ), the geometric scale should be 1:14. Thus, the Manning roughness scale factor limits the geometric scale [36]. When this parameter has no similarity, the model is rougher than its prototype, and scale effects are generated.

Inside the joints and the  $\delta$  gap, as with the cavities, constrictions, and junctions, the propagation speed of pressure wave ( $c$ ) becomes a function of the variation of fluid density (compressibility), and area (distensibility) increases in pressure [42]. For a given  $Fr_1$ , the effects of the Reynolds number on the two-phase flow properties are particularly notable in the developed shear layer [38]. Thus, aeration in a prototype will be higher than in the model, and a similar or smaller “ $c$ ” can be expected in the prototype. Pressure waves experience diffraction, interference, reflection, and refraction that depend of solid material in the boundary. These can alter the propagation speed, amplitude and the transmitted energy [14,18]. In the prototype, the boundary may be concrete and soil. The boundary was acrylic in the model, in which “ $c$ ” may decrease and energy losses in the reflection of the pressure wave increase. Nevertheless, in a prototype designed with the criterion and a scale more generous than 1:14, the impact of the last variables are less in the resonance phenomena and persistence time of the net uplift pressure due to the length of the slabs [27], the hydraulic jump’s low frequency [27,31,37], and the role of the joints as frequency filters [17,18]. The pressure amplification under the slab for the effects of fluid, joints interaction, and pressure waves at frequencies below 10.5 Hz were considered as part of this criterion.

In these cases that  $Fr_1$  is greater than 7.16, and/or the stilling basin demands a greater geometric scale than 1:15 to be able to establish similarity. The criterion proposed can be used for the predesign of lining slabs. “For a joint length of 18 m and  $c$  of 100 m/s, one obtains a resonance frequency  $< 3$  Hz [13]”. If the resonance is demonstrated, the transient approach needs a quantification of pressure amplification inside the joints, which can be the use of an appropriate pressure amplification coefficient [13]. To verify resonance inside the joints and the gap  $\delta$ , a model scale 1:1, pressure sensors with high natural frequency and with a damping close to 0.6 to prevent overshoot error are required. To check the stability of the slabs in the physical model of the prototype, a scale more generous than 1:14 is recommended. Given the opportunity to try alternatives, analyze different solutions, view operating conditions in extreme situations, and eventually, reduce the risk [43], physical modeling allows details to be refined so to as find a safer and more economical project.

To compare the developed criterion with other traditional criteria to estimate the slab equivalent thickness, some scale effects are ignored and two illustrative examples are shown. The author consider the hydraulic jump stilling basin with the

following details. The first example:  $y_1=2.43\text{m}$ ,  $y_2=31.45\text{m}$  (major conjugate of the hydraulic jump). Size of panel monolith:  $W=11.5\text{ m}$  ( $W=4.4y_1$ ) and  $L=25\text{ m}$  ( $L=9.76y_1$ ).  $V_1=46.1\text{ m/s}$  and  $Fr_1=9.44$ . Second illustrative example:  $y_1=0.45\text{m}$ ,  $y_2=3.54\text{ m}$ ,  $W=4.5\text{ m}$  ( $W=4.4y_1$ ),  $L=2\text{ m}$  ( $L=10y_1$ ),  $V_1=16.5\text{ m/s}$  and  $Fr_1=5.5$ . In the computation, the submerged specific weight is  $1.6\text{ ton/m}^3$ , and a safety factor and an operating drainage system are not considered.

Hydrostatic uplift is evaluated using three conditions: spillway design flood, stilling basin empty, and sudden drawdown following design flood [11,33]. Usually, the first condition gives the maximum uplift force in the slab close to the hydraulic jump [11]. The latter is due to the pressure of tail water level ( $T_w$ ), which is transmitted by a saturated foundation that has greater fluid pressure on the slab. The criteria belonging to Hajdin [7] and Toso *et al.* [8] was used, which are based on the measurement of fluctuating pressures, and the criteria of Farhoudi *et al.* [9] and Bellin *et al.* [10], which are based on direct measurement of fluctuating force. In all these studies, except Bellin *et al.* [10], propagation of fluctuating pressures below the apron was not considered. For the criteria to be applied, the influence of the length and width of the slab are taken into account by using the coefficient of spatial correlation ( $\phi_1, \phi_2$ ), the force coefficient ( $C_{fl}, C_{fw}$ ), or the uplift coefficient ( $\Omega$ ). This paper also considers the dimensionless pressure coefficient ( $C_p$ ), which is based on the maximum positive ( $C_p^+$ ) and negative pressure ( $C_p^-$ ) deviation from the mean pressure, and the coefficient based on root-mean-square pressure fluctuations ( $C_p'$ ) that is reported in the references [7-10, 27, 30].

In each example, two computations to evaluate Bellin *et al.* [10] and Toso’s [8] criteria with two  $C_p$  were used as it is important acknowledge the importance of a correct selection pressure coefficient when estimating the equivalent thickness. The slab equivalent thickness computation using various relationships is presented in Table 2.

The first computation of the two illustrative  $C_p$  examples was based on  $C_p^+$  and  $C_p^-$  experimental data. In this case, the equivalent thickness estimated by criteria from Bellin *et al.* [10], Hajdin [7], and Farhoudi *et al.* [9] were similar. The equivalent thickness that was estimated by the criterion proposed in this paper (last row, table 2) is greater than those mentioned above while Toso *et al.*’s criterion [8] was most conservative.

In the second computation in the two illustrative examples,  $C_p$  was based on the suggestions from each group of researchers. Bellin *et al.* [10] suggest assuming the pressure coefficients  $C_p^+$ ,  $C_p^- = 1$  in case of a lack of experimental data while Toso *et al.* [10] suggest  $C_p$  0.9 for the incident Froude number between 7.7 and 10. In this case, the criteria were very conservative.

The Toso [8] criteria may be safely assumed, but it is conservative for a large slab that presents the compensation of the pressure pulses on its upper face. In the hydraulic jump, the pressure pulses on big slabs are uncorrelated since the slab length is larger than the integral scale of the pressure fluctuations. The integral scale is thereby defined as the distance on which, on average, two pressure pulses become fully uncorrelated. In other words, it defines the maximum possible area in which a pulse may reasonably act [13,17].

Table 2.

Comparison of equivalent thickness of concrete lining that are calculated using various criteria

Method	Conditions/assumption	Fr <sub>1</sub>	s(m)
Hydrostatic uplift $s = (T_w - \bar{h})\gamma / (\gamma_c - \gamma)$	$\bar{h}/y_1 = 2.95$	9.44	15.17
	$\bar{h}/y_1 = 3.8$	5.55	1.14
Hajdin [7]	$\phi_1 = 0.68; \phi_2 = 0.93$	9.44	7.68
$s = \frac{C_p K \phi_1 \phi_2 V_1^2 \gamma}{2g(\gamma_c - \gamma)}$	$K = 3.09, C_p = 0.058$		
	$\phi_1 = 0.55; \phi_2 = 0.88$	5.55	0.93
	$K = 3.09, C_p = 0.072$		
Toso [8]; $C_p = C_p^+ + C_p^-$	$C_p = 0.43 + 0.28$ [8]	9.44	16.03
	$C_p = 0.9$ [8]	9.44	20.33
$s = \frac{C_p V_1^2 \gamma}{6g(\gamma_c - \gamma)}$	$C_p = 0.5 + 0.38$	5.55	2.55
	$C_p = 1$	5.55	2.89
Farhoudi [9]; $C_f'^2 = C_{fl} C_{fw}'$	$C_f'^2 = C_{fl} C_{fw}' = 0.022 * 0.044$	9.44	7.37
$s = \frac{V_1^2 \gamma 3.5 C_f'}{2g(\gamma_c - \gamma)}$	$C_f'^2 = C_{fl} C_{fw}' = 0.022 * 0.055$	5.55	1.05
Bellin [10]	$\Omega = 0.16$	9.44	7.15
$s = \frac{V_1^2 \gamma \Omega (C_p^+ + C_p^-)}{2g(\gamma_c - \gamma)}$	$C_p^+ = 0.40; C_p^- = 0.26$		
	$\Omega = 0.16, C_p^+ = 1, C_p^- = 1$	9.44	21.68
	$C_p^+ = 0.51, C_p^- = 0.32, \Omega = 0.12$	5.55	0.86
	$\Omega = 0.12, C_p^+ = 1, C_p^- = 1$	5.55	2.08
Author. Eq. 15	$C_d = 0.29$	9.44	12.01
	$C_d = 0.49$	5.55	2.61

Source: The author

Thus, extreme pulses recorded by a single sensor in the large slab are not a representative sample of the pressure fields above and below the slab to accurately calculate the uplift force [13,18]. Above the large slab, a positive or negative pulse is a local effect.

In the first illustrative example, for the first computation and the discarded Toso criterion, hydrostatic uplift was the most critical condition for the slab's stability. This clearly shows that the release of waterstops at two different points in the floor stilling basin leads to critical situations that deserve to be paid more attention from engineers.

In this study, a slab was located in the highest pressure fluctuations zone of the hydraulic jump as the study of Farhoudi *et al.* [9] and Bellin *et al.* [10] indicated. Differential heads resulting from the sloping water surface of the jump can cause a circulating flow under the slab if leakage is allowed to enter the joint at the downstream end of the basin and to flow out of the joint at the upstream end [32]. Therefore, it is necessary in future research to mount several slabs along the hydraulic jump and to vary the number of waterstops detached on two different slabs: one at the area of maximum pressure fluctuation in the toe jump and the other at the area of maximum depth.

The criterion proposed contributed to the search for a safe and economic design method for a concrete lined stilling basin because it considers uplift force and momenta. It was computed from a spatiotemporal analysis of the pressure fields that was measured above and below the instrumented slabs in a physical model. Furthermore, the criterion was supported by a large amount of experimental information, for which details that had previously been poorly studied such as joints, waterstops, and gaps between foundations and the concrete slab were considered. The design coefficient that is supplied by a curve in an  $Fr_1$  function facilitates the designer's application of the criterion.

## 6. Conclusions

The waterstops, the size, and the orientation joints have an effect on the uplift pressures, and consequently, influence the magnitude of uplift forces and momenta. The narrower joints and open traversal joints generated major uplift forces below the slabs. An offset of the center of pressure from the center of gravity in the flow direction increased the momenta  $Ma$  and  $Mc$  by up to 30%. Thus, it was necessary to consider the failure mechanism induced by momentum in the design criteria.

Considering the maximum force and momenta in each test, a design coefficient was found that defines the equivalent thickness depending on the incident Froude number between 3 and 10. It considers the effects of the offset on the center of pressure from the slab's center of gravity. This is generated by the influence of waterstops, joints, and hydraulic jump macroturbulence with full and partially developed inflow. According to changes in the hydrodynamic conditions and the physical model's characteristics, the study involves slabs with lengths between 6 and 12 times the incident flow depth.

The author discusses the scale effect that is inherent to the physical model and concludes that the experimental results are useful for: a) Designing the lining slabs in hydraulics structures that are similar to the model using scale more generous than 1:14, and an  $Fr_1$  between 2.3 and 7.15; b) Predesigning the lining slabs in stilling basins that require a geometric scale greater than 1:15 in order to establish similarity and/or an  $Fr_1$  between 7.16 and 10.

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