



CERNE

ISSN: 0104-7760

cerne@dcf.ufla.br

Universidade Federal de Lavras

Brasil

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CERNE, vol. 18, núm. 3, julio-septiembre, 2012, pp. 507-514

Universidade Federal de Lavras

Lavras, Brasil

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# BEHAVIOR OF ULTRASONIC WAVES IN WOOD WITH PRESENCE OF HOLES

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(received: September 17, 2010; accepted: March 30, 2012)

**ABSTRACT:** This work aimed to analyze the pattern of variation in wave lengths in presence of wood holes and to develop a model capable of describing the process. To attain that end, wood pieces were used from species pequiá (*Aspidosperma desmanthum*), on which circular and linear artificial holes were made and gradually enlarged. Ultrasonic tests were performed using USLab equipment and 45 kHz transducers. Measurements were taken first on the intact piece and then after each stage of artificial hole enlargement. Results demonstrated that propagation velocities of ultrasonic waves are affected by presence of holes and also that reduction in velocity is caused by changes in wave path, since waves tend to deviate from empty space and travel through matter. The circular hole type had a slightly stronger influence on velocity reduction than the linear hole type. Variation in velocity as a function of increasing percentage of hollow space relative to the intact piece can be represented by a linear model.

Key words: Pequiá (*Aspidosperma desmanthum*), wave length, acoustic method, forest sector.

## COMPORTAMENTO DE ONDAS DE ULTRASSOM NA PRESENÇA DE OCOS NA MADEIRA

**RESUMO:** Neste trabalho, objetivou-se estudar o comportamento da variação do percurso da onda em presença de oco na madeira bem como elaborar um modelo que o descrevesse. Para atingir esse objetivo, foram utilizadas peças de madeira da espécie pequiá (*Aspidosperma desmanthum*) nos quais foram confeccionados orifícios artificiais (circular e linear). Esses orifícios foram sendo aumentados gradualmente. Os ensaios de ultrassom foram realizados utilizando equipamento da marca USLab e transdutores de 45 kHz. As medições foram realizadas na peça íntegra e após cada fase de confecção do oco artificial. Os resultados permitiram confirmar que as velocidades de propagação de ondas de ultrassom são afetadas pela presença de ocos e que a redução da velocidade é provocada pela mudança de percurso da onda, que tende a se desviar do vazio e percorrer o material. O oco do tipo circular teve influência levemente superior na redução da velocidade do que o oco do tipo linear. A variação da velocidade com o aumento da porcentagem de oco em relação à peça íntegra pode ser representada por um modelo linear.

*Palavras-chave:* Pequiá (*Aspidosperma desmanthum*), percurso da onda, método acústico, setor florestal.

## 1 INTRODUCTION

One major problem entrepreneurs are faced with in sustainable forest management is the losses that come with tree selection, whether related to low quality or to low yield of wood. Where trees are rated as having low commercial value for one of the above reasons, they should still be preserved. Preserving unwanted trees would prevent waste, as trees in such condition are often abandoned in forests or in log yards for having no commercial value. Furthermore, if preserved, unwanted trees are important sources of food and shelter for animals, becoming part

of the group of remnant trees. One of the reasons for low yield is presence of holes in wood. Some species with commercial or strategic value are naturally hollowed, yet holes can also be provoked, in any species, by action of fungi and bacteria or else by natural causes. Where holes are large, use of the relevant trunk by the lumber industry may become economically unfeasible.

In Brazil, three methods are currently in use to evaluate presence of holes in tree trunks. One method consists in introducing the bar of a chainsaw into the trunk in the vertical direction and, based on resistance found, then infer about the presence and size of hollow spaces.

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This process is very invasive and may cause permanent damage to trees. Another technique is to hit the trunk with a hammer and assess the sound produced. This type of assessment is very subjective and conditional on operator's experience, being thus susceptible to major inaccuracies. A third technique is to evaluate any symptoms indicative of hole presence, including traces of termite presence or dark secretions along the trunk. Apolinário and Martius (2004) analyzed 110 trees from the experimental station of tropical silviculture (INPA), situated around 90 km away from Manaus, and found that 37.7% had large cavities along the center portion of the trunk. Out of the total of 110 trees, 21% were internally infested with termites, accounting for 57.5% of hollowed trees found.

Acoustic methods have been used successfully throughout the world in forest assessments and are even replacing or complementing visual assessments, given that in many cases tree pathologies are not visible to the naked eye, as is the case with the large majority of hollow spaces in trees. Wang et al. (2004) argue that different arrangements in measurements of wave propagation enable detection of different minimum sizes of internal defects. These authors concluded that measuring wave propagation time along the stem in the radial direction allows accurate determination of the internal condition of a tree. According to these authors, the velocity of wave propagation in defective solids will decrease because waves surround the defect, increasing the length traveled and, consequently, the propagation time. Deflorio, Fink and Schwarze (2007) used wave propagation to detect deterioration by six types of fungus in wood from Douglas Fir (*Pseudotsuga manziessi*), Beech (*Fagus grandifolia*), Oak (*Quercus robur*) and Sycamore (*Populus tremuloides*) following artificial inoculation, and observed data for 2, 16 and 27 months. Besides variation in velocity, the authors also evaluated weight loss and density reduction in order to compare results. They concluded that wave propagation was capable of detecting deterioration by fungi from the start. Weight loss, density reduction and velocity reduction were detected for all fungus-host combinations. Najafi, Shalbafan and Ebrahimi (2009) performed tests using ultrasonic waves in order to detect hollow spaces in Beech (*Fagus orientalis*). To obtain improved contrasts, disks were removed from different sections of the trunk of sound trees, then holes (representing internal decay) were manually created and progressively enlarged. These artificial holes included two types, circular and linear. Velocities of ultrasonic waves

were measured on intact disks and on the disks with linear and circular holes, in different positions. Results revealed that ultrasonic velocities significantly decreased with increased hole size. The relative position of holes did not influence the magnitude nor the tendency to reduction in velocity. A comparison between linear and circular holes showed that linear holes had less effect on the decrease in ultrasound velocities. Najafi, Shalbafan and Ebrahimi (2009) concluded that the propagation velocity decreases because waves surround holes, similarly to the conclusion drawn by Wang et al. (2007).

To evaluate ultrasonic wave behavior in presence of hollow spaces, Lin et al. (2008) artificially made circular holes, centralized and decentralized, in wood disks from species Japanese cedar (*Cryptomeria japonica*) measuring 300 mm and 350 mm in diameter and 100 mm in thickness. For the study, the authors used Sylvest equipment with 22 kHz frequency transducers. They established correlations between the propagation velocity of ultrasonic waves and the relative residual diameter, using initial diameter and hole diameter as factors.

In this context, this work was developed to evaluate variation in the propagation velocity of ultrasonic waves in presence of holes of known size, looking to determine a representative model of this type of variation for circular and linear holes in wood from pequiá (*Aspidosperma desmanthum*).

## 2 MATERIAL AND METHODS

### 2.1 Material and equipment

To perform tests, two massive wood pieces from pequiá (*Aspidosperma desmanthum*) were used, 390 mm x 390 mm x 50 mm in nominal size. This particular species was selected due to its susceptibility to formation of holes and due to its great commercial interest. The wood pieces were donated by TORA BRASIL.

The ultrasound equipment used was USLab, developed by staff at the nondestructive testing laboratory (LabEND) of the Agricultural Engineering College (FEAGRI) of Campinas state university (UNICAMP), in partnership with AGRICEF Soluções Tecnológicas, a technology-based company. The tests were performed using flat-face transducers and 45 kHz frequencies.

In order to make artificial holes, a CNC (Computer Numeric Control) machine was used, from a SENAI unit located in Itatiba. The reason for selecting this type of equipment is it allows precision in hole cutting, which makes it possible to develop a regression study for

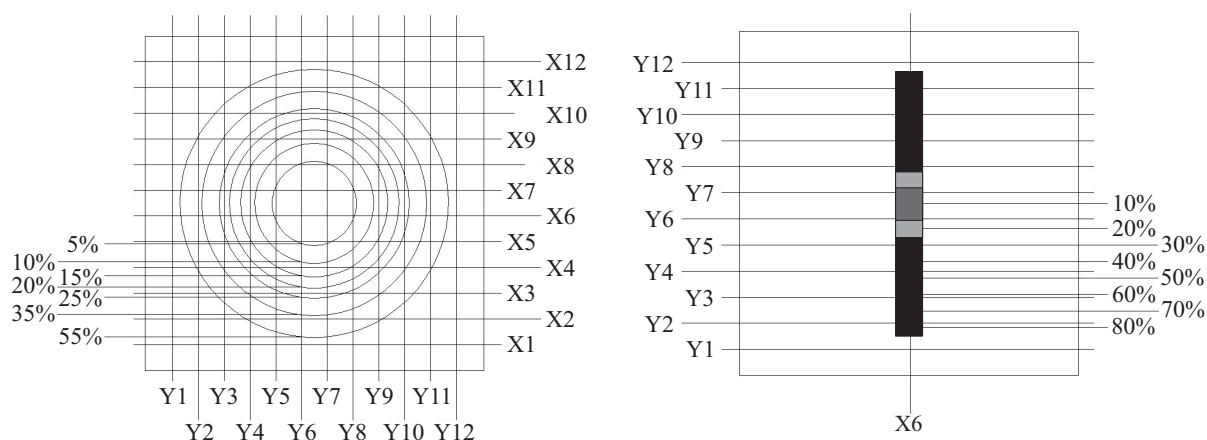
determination of a variation model of wave propagation as a function of increased hollow size.

## 2.2 Measurement methodology

Two types of artificial hole were created in each wood piece, namely linear and circular, which were gradually enlarged (Figure 1). Figure 1 also depicts the measurement grid with a 30 mm x 30 mm line pattern drawn in perpendicular directions and labeled X and Y. In each grid band (X1, X2, ... etc. , Y1, Y2, ... etc.), measurements were taken of the times of ultrasonic wave propagation (t). Initially, the intact pieces (no holes) were subjected to ultrasonic measurement to determine times of

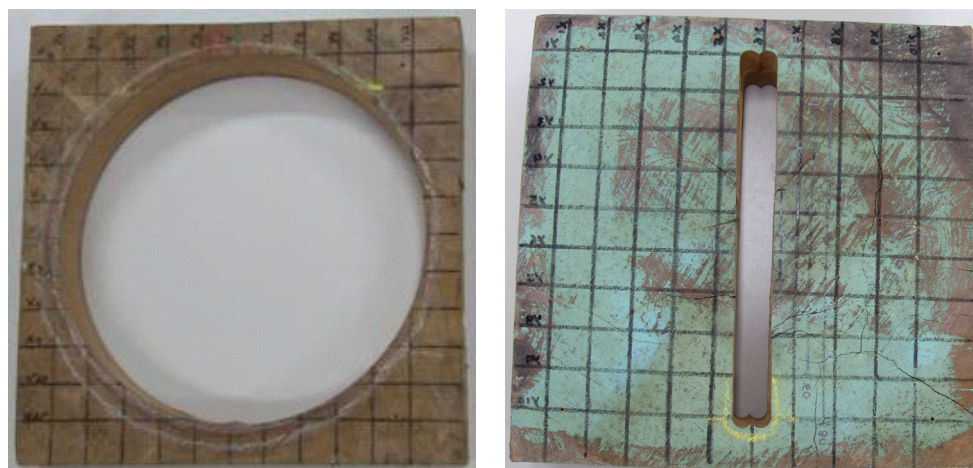
wave propagation (t). The piece with a circular hole was termed P1 and the piece with a linear hole was termed P2. To assess variations in travel time as a function of hole size, the pieces were progressively enlarged at the following rates: 5%, 10%, 15%, 20%, 25%, 35% and 55% in the case of the circular hole and 10%, 20%, 30%, 40%, 50%, 60%, 70% and 80% in the case of the linear hole. After each incision, the pieces were again subjected to measurements using the ultrasonic wave grid. Figure 2 illustrates the hollowed pieces up to the maximum percentages.

Results of wave propagation velocity for each hole size were statistically analyzed using software Statgraphics Centurion.



**Figure 1** – Illustration of artificially cut circular and linear holes, increasingly enlarged in percentage relative to the sound piece.

**Figura 1** – Esquema da produção de ocos artificiais - circular e linear - com aumento percentual da dimensão em relação à parte sã.



**Figure 2** – Artificially hollowed pieces of pequiá up to maximum percentages (55% for the circular hole and 80% for the linear hole).

**Figura 2** – Peças de pequiá com oco artificial circular máximo (55%) e com oco artificial linear máximo (80%).

### 3 RESULTS AND DISCUSSION

Table 1 provides mean results and variability in velocity of wave propagation as obtained in both measurement directions (X and Y), for the two intact pieces (P1 – circular hole and P2 – linear hole). Results are given as velocity because the two pieces differ slightly in size, preventing direct comparison of wave propagation times. For each point of the measurement grid, velocity was calculated as the ratio of length traveled to propagation time.

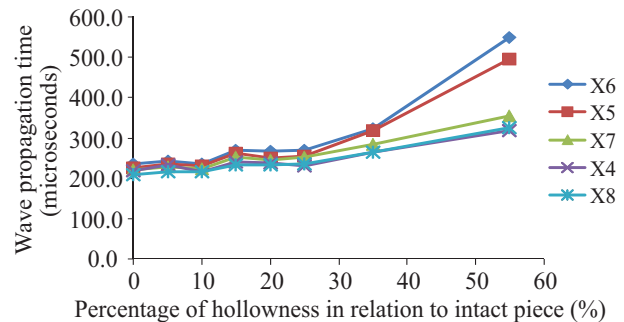
**Table 1** – Mean results for propagation velocities of ultrasonic waves in yet intact pieces of pequiá.

**Tabela 1** – Resultados de médias das velocidades de propagação de ondas de ultrassom nas peças de Pequiá ainda integras.

Grid direction	Mean velocity (m.s <sup>-1</sup> )	CV (%)
Piece P1 (on which a circular hole was cut)		
X	1841	3.7
Y	1803	6.3
Mean	1822	5.1
Piece P2 (on which a linear hole was cut)		
X	1708	5.18
Y	1760	6.07
Mean	1734	5.7
Overall mean	1778	3.5

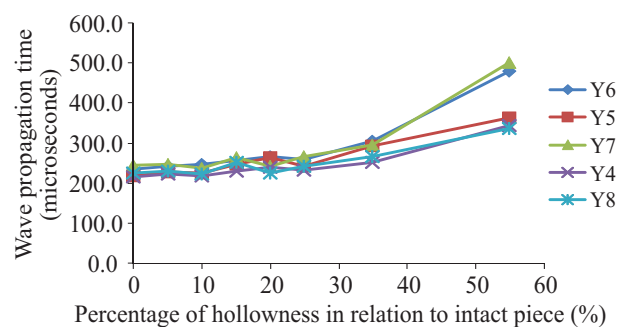
The mean velocity in piece P1 was 5% higher than in piece P2. After using all X and Y measurements on the grid of each piece, it was demonstrated that the means were statistically similar. This result suggests that, independently, the pieces show little variation in velocity, which indicates absence of defects or less resistant areas affected for instance by small cracks etc. Despite being both from the same species, the coefficient of variation for velocities in pieces P1 and P2 was low (3.5%), considering the inherent variability of wood. According to NBR 7190 (ASSOCIAÇÃO BRASILEIRA DE NORMAS TÉCNICAS - ABNT, 1997), coefficients of variation for wood properties in one lot of the same species are considered normal if up to 18%. For propagation velocity of ultrasonic waves in a single species, Bucur (2006) reported coefficients of variation ranging from 3.69% to 7.51%. Lin et al. (2008) obtained velocities in the order of 1600 m.s<sup>-1</sup> while studying yet intact pieces from species *Cryptomeria japonica*.

Figures 3, 4, 5 and 6 provide graphs illustrating the behavior of wave propagation times at different points of the grid, for different hole sizes, circular and linear respectively.



**Figure 3** – Behavior of wave propagation time as a function of position in the measurement grid for the piece with a circular hole, X direction.

**Figura 3** – Comportamento do tempo de propagação da onda em função da posição na malha de medição na direção X para a peça com oco circular.

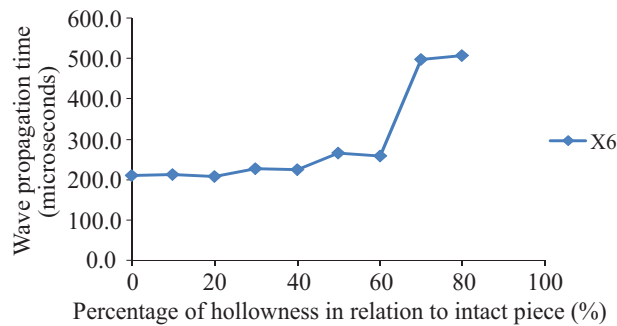


**Figure 4** – Behavior of wave propagation time as a function of position in the measurement grid for the piece with a circular hole, Y direction.

**Figura 4** – Comportamento do tempo de propagação da onda em função da posição na malha de medição na direção Y para a peça com oco circular.

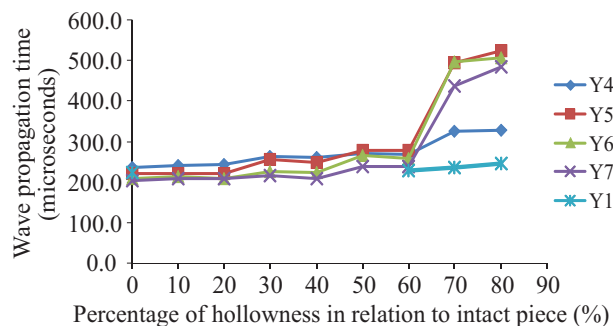
In both pieces, measurements were taken in hole-affected positions only. In the case of the linear hole, X direction, there is indication of one measuring point only (X6) as the others are inapplicable. The reason for adopting propagation time rather than propagation velocity was that, if velocity had been used, the length traveled by the wave would have been automatically established, yet the aim in this study was more exactly to study the length traveled by the wave in presence of empty space.





**Figure 5** – Behavior of wave propagation time as a function of position in the measurement grid for the piece with a linear hole, X direction.

**Figura 5** – Comportamento do tempo de propagação da onda em função da posição na malha de medição na direção X para a peça com oco linear.



**Figure 6** – Behavior of wave propagation time as a function of position in the measurement grid for the piece with a linear hole, Y direction.

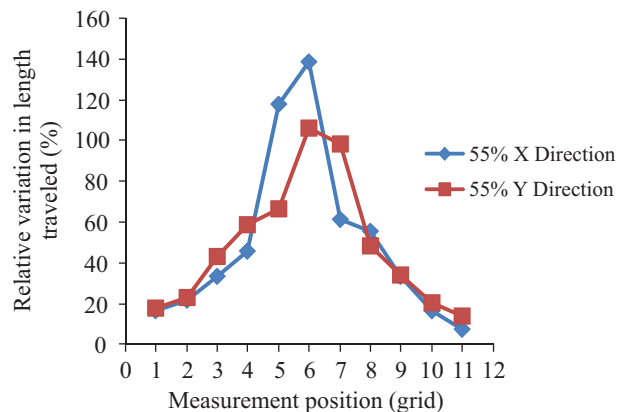
**Figura 6** – Comportamento do tempo de propagação da onda em função da posição na malha de medição na direção Y para a peça com oco linear.

In both types of hole, greater variations in propagation time were found in positions closer to center portion of the hole, against minor variations in positions away from the center. The graphs also reveal two levels of time variation. Regarding the circular hole, one level of time variation is noted up until 35% of hollowness, followed by another with greater variations from that point onward. For the linear hole, time variations are greater for hollowness values above 60%. These greater variations in more central positions seem to corroborate conclusions drawn by Najafi, Shalbafan and Ebrahimi (2009) and Wang et al. (2004), in that a wave diverts from empty space and, in doing so, the length traveled will increase and so will time consequently.

Figures 7 and 8 provide graphs of relative variation in the length traveled ( $\Delta LR$ ) obtained by Equation 1, as a function of the measurement position, considering the highest proportion of hollowness being analyzed (55% for the circular hole and 80% for the linear hole).

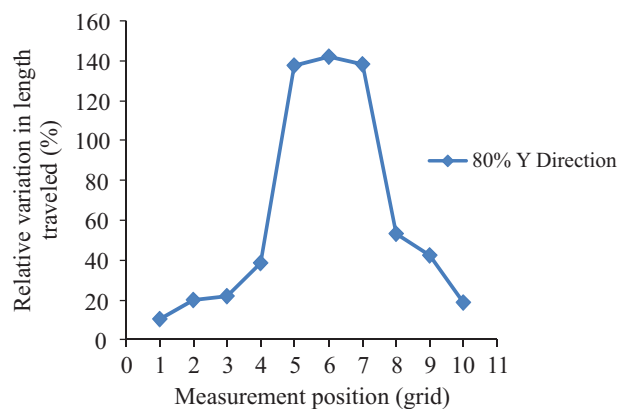
$$\Delta LR = [(L_{\text{Reference}} - L_{\text{length}}) / (L_{\text{Reference}})] * 100 \quad (1)$$

Where:  $L_{\text{Reference}}$  is the length traveled by the wave on the intact piece and  $L_{\text{length}}$  is the length obtained using the velocity on the intact piece and the time measured on the hollowed piece.



**Figure 7** – Relative variation in length traveled as a function of measurement position. Circular hole.

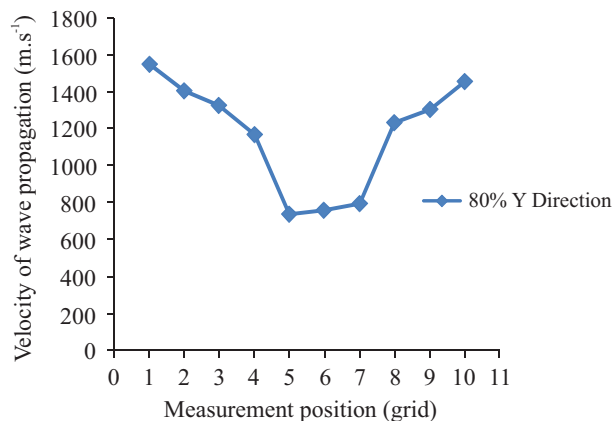
**Figura 7** – Variação relativa do comprimento de percurso em função da posição de medição. Oco circular.



**Figure 8** – Relative variation in length traveled as a function of measurement position. Linear hole.

**Figura 8** – Variação relativa do comprimento de percurso em função da posição de medição. Oco linear.

These graphs reveal longer lengths in reading position 6, the reason being that in this case propagation is closer to the center portion of the hole, in both hole types. The more removed propagation is from the center portion of the hole, the smaller the increase in the length traveled, as the path traveled in order to deviate from the hole is shorter. Another way to explain variation in the propagation velocity of ultrasonic waves in wood as a function of hollowness is to consider that velocity decreases because waves pass through two different mediums, wood matter (intact piece) and air (hollow space). Considering that in intact wood velocity is about  $1800 \text{ m.s}^{-1}$  whereas in air velocity is about  $300 \text{ m.s}^{-1}$ , a reduction in this velocity could be a function of the proportion between the propagation mediums. Yet, in the case of the linear hole, with propagation in the Y direction (perpendicular to the hole), the proportions of wood and air would be the same in any measurement point passing through the hole. Consequently, one would expect velocities to be virtually the same, regardless of the measurement position in the Y direction, although not the case (Figure 9).



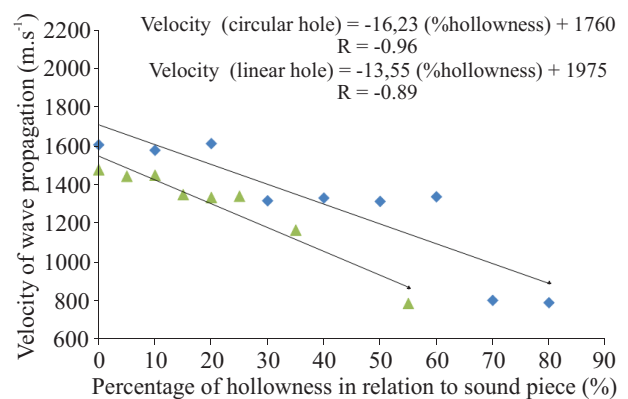
**Figure 9** – Variation in propagation velocity as a function of measurement position Y. Linear hole at a proportion of 80% relative to the piece.

**Figura 9** – Variação da velocidade de propagação em função da posição de medição Y. Oco linear com proporção de 80% em relação à peça.

Additionally, if propagation did occur through hollowness, the obtained mean velocity, considering the length traveled in wood (355 mm) and the length traveled in air (30 mm), would be approximately  $1600 \text{ m.s}^{-1}$ , yet this value was only observed in edge positions (1 and 10). In the remaining cases, velocity was always lower, reaching

around  $700 \text{ m.s}^{-1}$  in the center position, which confirms the hypothesis that a wave seeks matter to propagate as opposed to empty space, diverting its path. This variation in velocities was very close to values found by Lin et al. (2008), whose results ranged from  $1600 \text{ m.s}^{-1}$  to  $600 \text{ m.s}^{-1}$ .

In order to evaluate the materiality of a correlation model between variation in propagation velocity and increased proportion of hollowness, in the case of species pequiá, mean velocities (X and Y) were used as obtained in measurement position 6, the reason being that position 6 was the centermost portion of the hole and consequently the most suitable, as far as rates of hollowness to intact piece are concerned. In the remaining positions, such correlations could be obtained by considering the linear size of the hole through which the wave propagated rather than its proportion relative to the intact piece. Figure 10 provides a graph to illustrate the behavior of velocity variation with increased percentage of hollowness and the regression equation for circular and linear hole.



**Figure 10** – Variation of velocity as a function of rate of hollowness to intact piece (circular and linear holes), considering measurement position 6 (centermost portion).

**Figura 10** – Variação entre velocidade e porcentagem de oco em relação à parte sã das peças com oco (circular e linear) considerando a posição de medição 6 (mais centralizada em relação ao oco).

Tables 2 and 3 provide results of the analysis of variance of the regression for circular and linear holes respectively. With the P-values found in the ANOVA tables being less than 0.05, for both the circular hole (Table 2) and the linear hole (Table 3), the correlation between propagation velocity and variation in hollowness percentage is indeed statistically significant at the 95% confidence level.

**Table 2** – Analysis of Variance (ANOVA table) of the regression between velocity and hollowness percentage, for the piece with a circular hole.

**Tabela 2** – Análise de Variância (Tabela de ANOVA) da regressão entre velocidade e porcentagem de oco para a peça com oco circular.

Source	Sum of squares	Df	Mean squares	F-Ratio	P-Value
Model	585379.	1	585379.		
Residual	49437.8	6	8239.63	71.04	0.0002
Total (Corr.)	634817.	7			

**Table 3** – Analysis of Variance (ANOVA table) of the regression between velocity and hollowness percentage, for the piece with a linear hole.

**Tabela 3** – Análise de Variância (Tabela de ANOVA) da regressão entre velocidade e porcentagem de oco para a peça com oco linear.

Source	Sum of squares	Df	Mean squares	F-Ratio	P-Value
Model	1.10107E6	1	1.10107E-6		
Residual	263069	7	37581.3	29.30	0.0010
Total (Corr.)	1.36414E6	8			

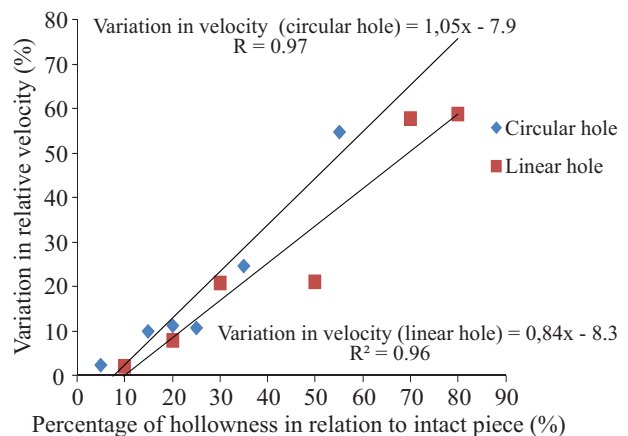
In the case of the circular hole, the model explains 92.2% of variability in velocity and there is a strong correlation between the variables velocity and hollowness percentage ( $R = 0.96$ ). As regards the linear hole, the model explains 80.7% of variability in velocity and the correlation, despite weaker, can also be considered significant ( $R = 0.89$ ). The slope coefficients of the regression models indicate that the velocity with which waves propagate is more influenced by the circular hole than by the linear hole. For every 10% increase in hollowness, the variation in velocity is about  $160 \text{ m.s}^{-1}$  for the circular hole and about  $130 \text{ m.s}^{-1}$  for the linear hole. A similar result was obtained by Najafi, Shalbafan and Ebrahimi (2009), despite less, as for every 10% increase in hollowness these authors found a velocity variation of about  $110 \text{ m.s}^{-1}$  for the circular hole and  $70 \text{ m.s}^{-1}$  for the linear hole.

Another method to evaluate which type of hole has greater influence on velocity is to use the relative variation in velocity (RVC) as adopted by Najafi, Shalbafan and Ebrahimi (2009) which is represented by Equation 2.

$$\text{RVC} = [(V_{\text{reference}} - V_{\text{measured}})/(V_{\text{reference}})] * 100 \quad (2)$$

Where  $V_{\text{reference}}$  is the velocity through the intact piece and  $V_{\text{measured}}$  is the measured velocity in the hollowed piece.

Figure 11 provides a graph to illustrate the behavior of RVC variation for both types of hole being analyzed. Results were similar to those found by Najafi, Shalbafan and Ebrahimi (2009), who found greater variations for the circular hole and a tendency toward increasing differences the greater the percentage of hollowness.



**Figure 11** – Variation in relative velocity (RVC) for circular hole and linear hole.

**Figura 11** – Variação da velocidade relativa (RVC) para peças com oco circular e linear.

## 4 CONCLUSIONS

The propagation velocities of ultrasonic waves are affected by presence of holes, whether linear or circular, and the reduction in velocity is caused by a diversion in the wave path, as waves tend to divert from empty space and travel through matter. The circular hole type had greater influence on reduction in velocity than the linear hole type. Variation in velocity as a function of increased percentage of hollowness can be represented by a linear model. The model will be used by the team on a later occasion in order to construct imagery using ultrasonic tomography.

## 5 ACKNOWLEDGEMENTS

The authors wish to thank CNPq and FAPESP for providing financial support, TORA BRASIL for providing wood samples, SENAI-Itatiba's technician Antônio Paulo



for helping with wood cutting, and SENAI-Itatiba for providing the CNC machine.

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