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# White-Dwarfs in the thin-disk: physical properties and luminosity functions

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In this article, we present an investigation of a sample of 1072 stars extracted from the *Villanova Catalog of Spectroscopically Identified White Dwarfs* (2005 on-line version), studying their distribution in the Galaxy, their physical properties and their luminosity functions. The distances and physical properties of the white dwarfs are determined through interpolation of their (B-V) or (b-y) colors in model grids. The solar position relative to the Galactic plane, luminosity function, as well as separate functions for each white dwarf spectral type are derived and discussed. We show that the binary fraction does not vary significantly as a function of distance from the Galactic disk out to 100 pc. We propose that the formation rates of DA and non-DAs have changed over time and/or that DAs evolve into non-DA types. The luminosity functions for DAs and DBs have peaks possibly related to a star burst event.

**Key words:** White dwarfs. Binaries ages. Statistics.  
Stellar populations.



## 1 Introduction

Stars with masses lower than 8 comprise the majority of objects in the Galaxy, and will eventually evolve into electron-degenerate white dwarfs (WDs), making them the most common end product of stellar evolution. WDs are essentially degenerate plasmas, governed by well understood physical processes, and are one of the most useful classes of objects in the Galaxy because they are well-behaved cosmochronometers – for a detailed discussion, see Fontaine et al. (2001). Consequently, WDs have been used to understand degenerate physical processes, stellar evolution, and Galactic formation and evolution.

White dwarfs have been commonly used as tracers of old Galactic populations. For example, in Sion et al. (1988), the authors analyzed a sample of stars from the McCook & Sion (1977) catalog. Based on published observational data and on the derived effective temperatures, radii, masses, and kinematics of hundreds of WDs of various spectral types, the authors found that there is no kinematic difference between DA and DB stars of similar color and magnitude, and that magnetic degenerate stars are a kinematically distinct group of young disk objects. Based on the general kinematic similarity of DA stars and their non-DA counterparts, the authors also inferred that neither evolved from more massive WD progenitors.

Because WDs cool predictably with age, they provide a means to estimate important timescales, such as the timing of early star formation events in the Galaxy. Luyten (1958), Sion and Liebert (1977), Greenstein (1979), and Sion et al. (1988) all estimated the WD local density and luminosity function. All efforts were successes to some extent, but were ultimately limited by statistically incomplete and small samples. Green (1980) constructed the WD luminosity function for a statistically complete sample, but was limit-

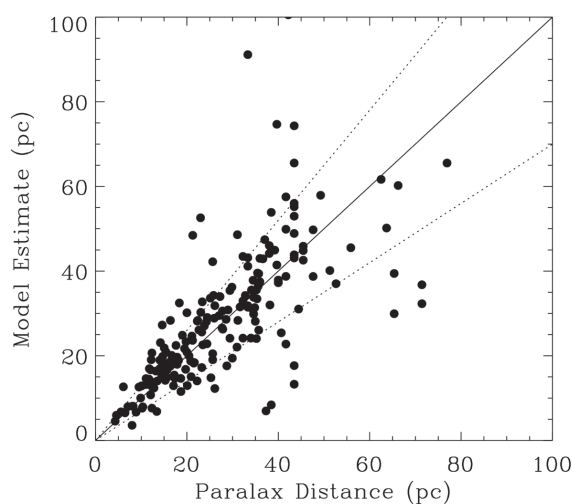
ed by small number of objects (89) and low quality spectra, which led to poorly estimated physical properties.

One of the luminosity function's most important features, the evident drop-off found at, was recognized not to be a simple effect of observational completeness but to be a consequence of the cooling processes in WDs. To put it simply, WDs have not had enough time to cool to fainter magnitudes. The possibility of linking this feature to the first burst of star formation has prompted researchers to attempt to use the luminosity function to obtain constraints for the age of the Galaxy (e.g. IBEN; LAUGHLIN, 1989; OSWALT et al., 1996; SALARIS et al., 1997, and references therein). In Liebert et al. (1988), the authors presented arguably the benchmark study of the WD luminosity function. With careful attention to the sample used, as well as the most up-to-date models to determine WD physical properties, they estimated an age of 7 to 10 Gyr for the Galactic disk.

Based on the observational results of Liebert et al. (1988), Wood (1992) presented the first comprehensive theoretical study of the parameter space that defines the luminosity function, including more realistic treatments of cooling, star formation rates and bursts, as well as scale-height inflation. The author shows the luminosity function as particularly sensitive to star formation rates and bursts, as well as WD core composition. The author finds that the luminosity function is insensitive to the assumed initial mass function, scale height, and WD progenitor mass upper limit.

After these efforts, many others have followed with improved samples and variations in the theoretical procedure of obtaining a fit to an observed luminosity function. Wood & Oswalt (1998) present a good summary of these papers, as well as a very thorough discussion of uncertainties inherent to the commonly used method of obtaining the





ed the catalog’s spectral classification of individual WDs to assign each WD to DA or non-DA model grid. Thus, stars were separated into DA and non-DA samples for the application of H or He model grids, respectively, as described in Bergeron et al. (2001). As shown in table 1, a total of 184 WDs and 888 WDs with estimated distances comprise the final sample.

### 3 Distribution of WDs in the galaxy

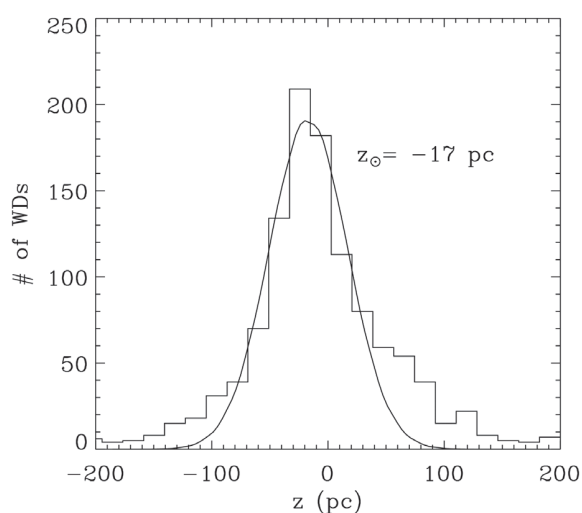
### 3.1 The binary fraction

One of our objectives in this work was to investigate how the properties of the objects in our sample relate to their positions in the Galaxy and more precisely, to their distances to the Galactic disk. Figure 2 shows the distribution of the sample in the sky, as well as the distances to the disk as a function of the Galactic longitude. The reasonably uniform distribution of objects in the sky and the decreasing gradient away from the disk

are evident. Visual inspection of this figure shows that there is no significant difference between the specified distributions of DA (open circles) and non-DA (filled circles) stars.

Our sample allows us to investigate whether any correlation exists between distance to the Galactic disk and binary fraction. To examine the potential correlation between disk distance  $z$  and binary fraction, we first corrected  $z$  for the solar offset. The correction was performed using the offset value determined by performing a Gaussian fit to the histogram of uncorrected  $z$  values and determining the offset of the Gaussian peak (figure 3). In this fit we used Poisson weighting for the points, which gives higher importance for higher star counts, therefore leading to a poorer fit for the wings of the distribution. We found the solar distance to the disk to be above the plane defined by the WDs. This value is in general agreement

with the ones published by Humphreys & Larsen (1995), in which a thorough discussion of the solar distance to the plane is made. Using the corrected values, we plotted the number of single and binary WD systems (as defined in the *Villanova Catalog*) out to 100 pc in bins of 10 pc (figure 4, upper left panel), and then divided the two distributions to obtain the binary fraction (figure 4, upper right). In the lower panels of figure 4, we show the results of applying the same procedure as before, but plotting counts as a function of distance to the Sun. In this procedure stars such as Sirius A and B were considered as one system to be consistent with the unresolved binaries in the sample.



**Figure 3: Determination of the solar distance to the Galactic disk. We constructed a histogram with the uncorrected  $z$  values for the WDs and then fit a Gaussian to the distribution. The offset of the Gaussian peak relative to the position  $z=0$  was then adopted as the solar offset**

Source: The authors.

The flat nature (within the errors) of the binary fraction (figure 4, lower right panel) indicates that both single and binary WD systems have similar detection biases as a function of distance, when considering the volume limited to 100 pc. We limited the distance to the value of 100 pc due to detection biases that can be present at higher dis-

tances. In particular, we needed to ensure that the efficiency for the detection of objects is basically the same for single WDs as well as for the binary WDs, before investigating their relative behavior. This is clearly demonstrated by the histogram of counts as a function of solar distance for single and binary WDs and the binary fraction derived from them. If there were systematic differences in the detection efficiency for the two types of objects, a change in the slope of the binary fraction would be evident. Inspecting the histogram of the binary fraction of WDs as a function of distance to the disk  $z$  (figure 4 upper right), a slope in the binary fraction is not detected, at least within the errors. It is clear that this technique can provide some interesting results, but much larger samples with reliable binary classification are still needed.

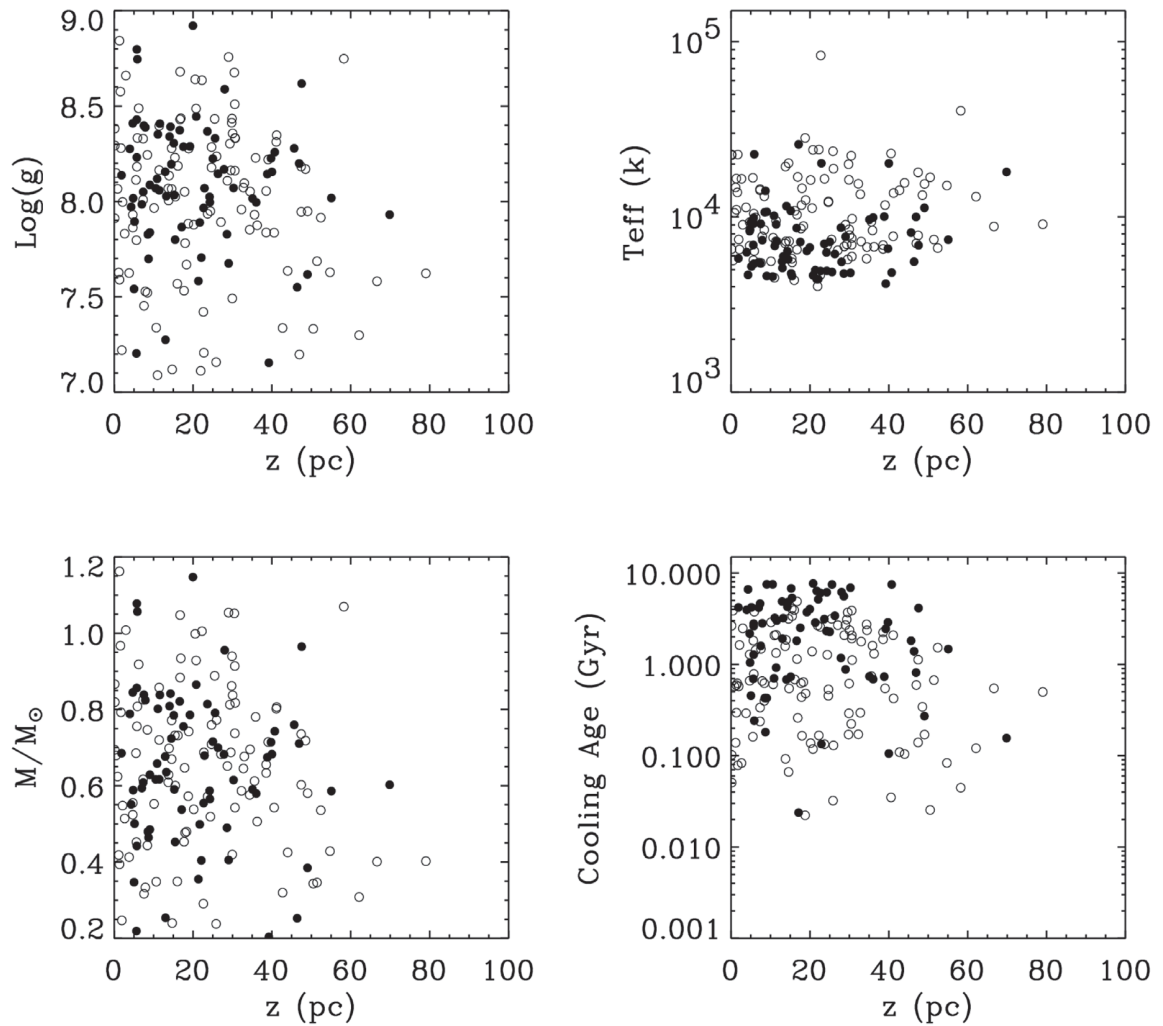
## 2.2 The physical properties

We also investigated the relationship between the physical properties of the WDs that had reliable parallaxes and their positions in the Galaxy, using the procedure developed in Monteiro et al. (2006), which combines the absolute magnitude with the  $(B-V)$  color and model grids to determine the physical properties of the WDs. To determine the errors in our procedure, we compared results from our method to those of Bergeron et al. (2001), who modeled WD physical properties using precise trigonometric parallaxes. It is clear from the results shown in figure 5 that the  $\log(g)$ ,  $T_{eff}$  and cooling age are reasonably well-determined, with average errors under 20%, approximately. However, mass is less well-determined, with about 30% average errors. The objects found outside of the 20% regions typically fall outside the model grids available, and therefore, are subject to large extrapolation errors.

We proceeded with the determination of  $\log(g)$ ,  $T_{eff}$  mass and cooling age for our sample using the method discussed above. With these







**Figure 5: Comparison of our model interpolation results to those of Bergeron et al.(2001) with DA (open circles) and non-DA (filled circles). The dotted lines indicate the 20% difference regions**

Source: The authors.

ences between DA and non-DAs. The histogram for  $\log(g)$ ,  $T_{eff}$  with median around  $\log(g) \sim 8.1$ , is slightly skewed to higher values, likely due to contamination by unresolved binaries. The histograms for the cooling ages of DAs and non-DAs show that DAs are on average younger than non-DAs, and are not likely to be found with cooling ages greater than  $\sim 5$  Gyr. On the other hand, we found cooling ages up to  $\sim 8$  Gyr for non-DAs.

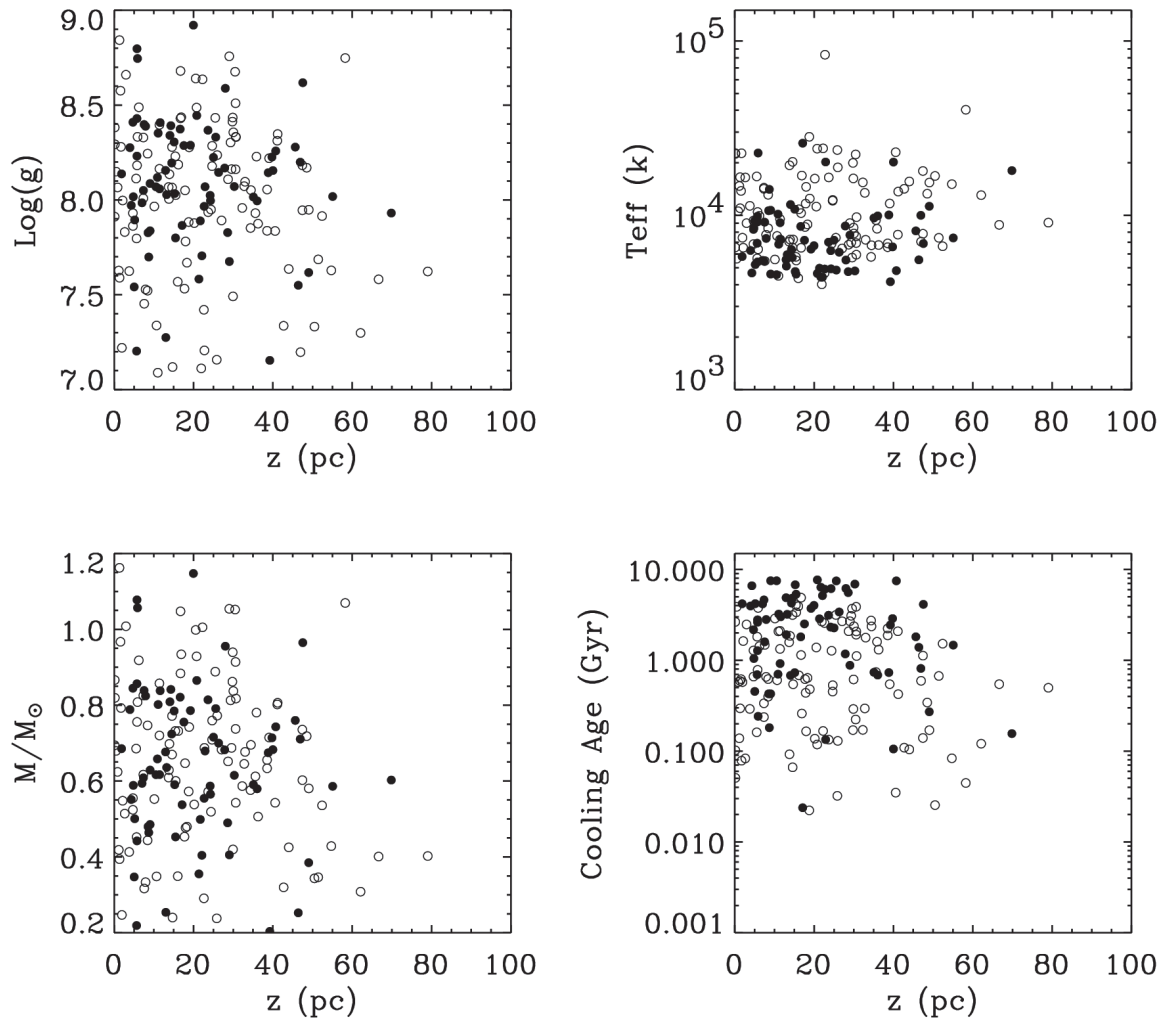
We also investigated the distribution of total ages for each WD spectral type. To accomplish

this, we first adopted the initial to final mass relation (IFMR) of Weidemann (2000) to determine the progenitor masses for the WDs fitting the tabulated values using a third order polynomial:

$$M = 0.009 + (6.6M_{WD}) + (20.8M_{WD}^2) + (7.6M_{WD}^3) \quad (1)$$

in which  $M$  is the progenitor mass and  $M_{WD}$  is the mass of the white dwarf in solar masses. Finally, we used this polynomial in conjunction with the





**Figure 6: Physical parameters determined for the WDs with parallax distances using the model grid interpolation method described in Monteiro et al. (2005)**

Source: The authors.

following equation for the time spent on the Main Sequence to obtain the total ages FBB01:

$$t_{MS} = 10 \cdot M^{-2.5} \text{ Gyr} \quad (2)$$

in which  $M$  is the mass of the progenitor (in solar units), and  $t_{MS}$  is the main sequence lifetime in Gyr.

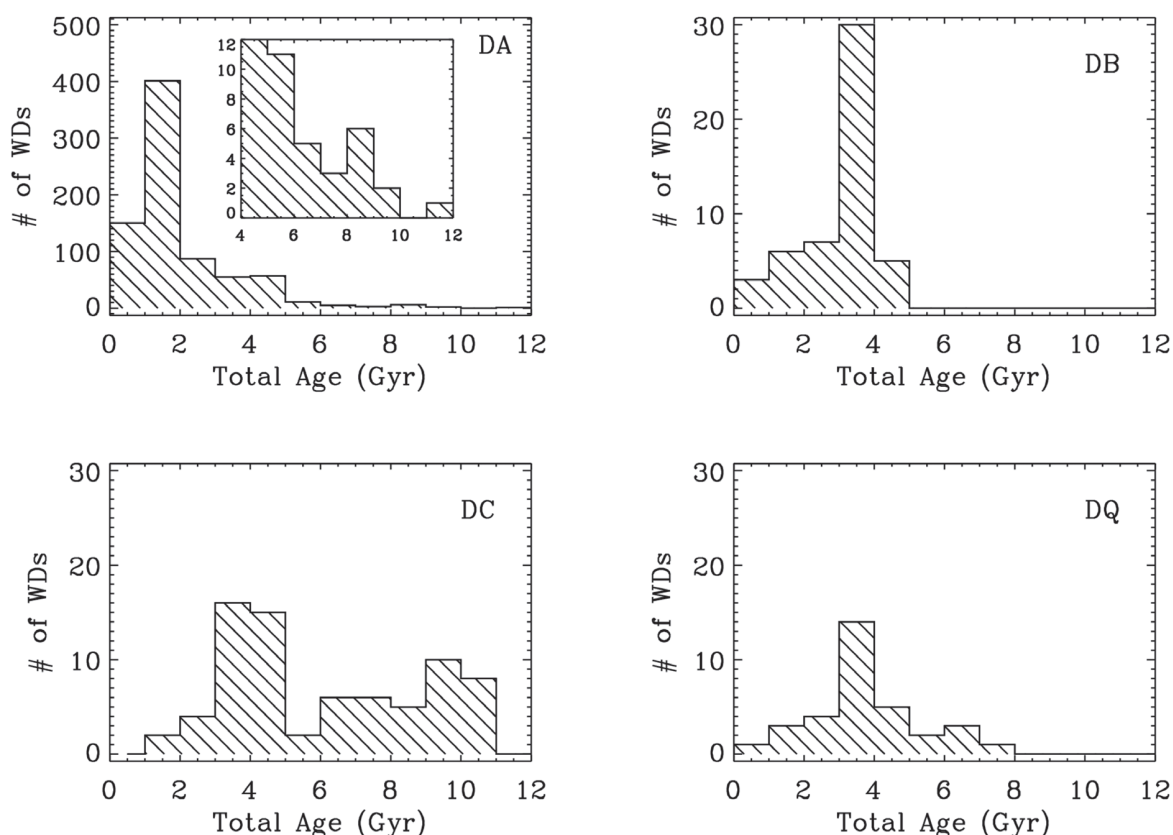
In figure 9, we show the total age histograms for the various WD spectral types studied here (DA, DB, DC and DQ). Due to small number of

objects, the DZ histogram was not constructed. For these histograms, we used the entire sample (including the WDs with distance estimates). It is important to point out that these distances were determined using a fixed  $\log(g) = 8.0$  and will, therefore, lead to uncertainties in cooling age and Main Sequence Lifetime, although this error should be small given the narrow distribution of  $\log(g)$  and masses of WDs as seen in figure 7.

Source: The authors.

The main cause for the behavior discussed previously is the evolution of the spectral types due to the cooling of the WDs, for example, the evolution to DCs from DBs caused by the lowering of the atmospheric temperature and reduction of

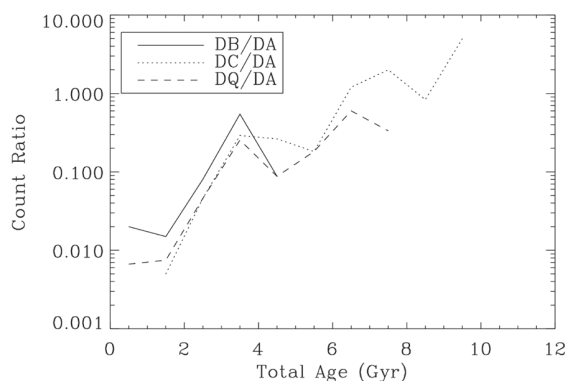




**Figure 9: Histograms of WD total ages for the different spectral types studied. The bin size used was 1 Gyr**

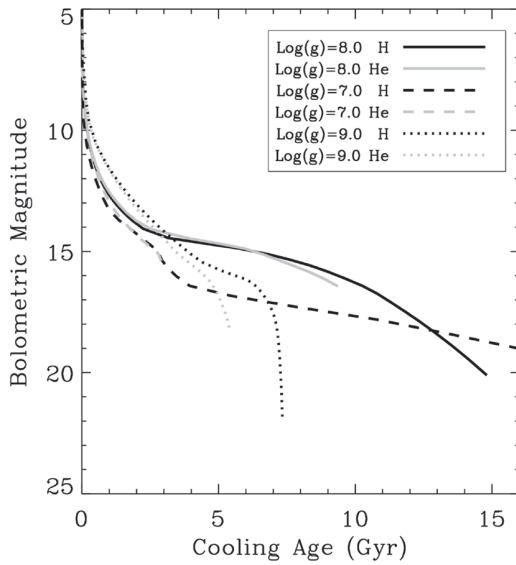
Source: The authors.

3 Gyr, especially considering that for a given age and  $\text{Log}(g) \sim 8.0$  there is very little difference in luminosity between both types. One could also argue that there is some uncertainty in the spectral types assigned to the stars given poor signal to noise spectra, but this is also unlikely to be relevant for the large factor observed at later ages. We are then left with the possibility of changing star formation properties as the Galaxy evolves and the possibility that there might be some evolution of the spectral types, with a portion of DAs evolving eventually to DCs. With this data set, it is impossible to separate between these two effects, or how important one is relative to the other with certainty.



**Figure 10: Ratio of the number counts of DB, DC and DQ relative to the DA counts as a function of total age. The bin size used was 1 Gyr**

Source: The authors.



**Figure 11: Cooling curves for H models (black lines) and He models (gray lines) for different  $\text{Log}(g)$  values**

Source: The authors.

### 3 Luminosity function

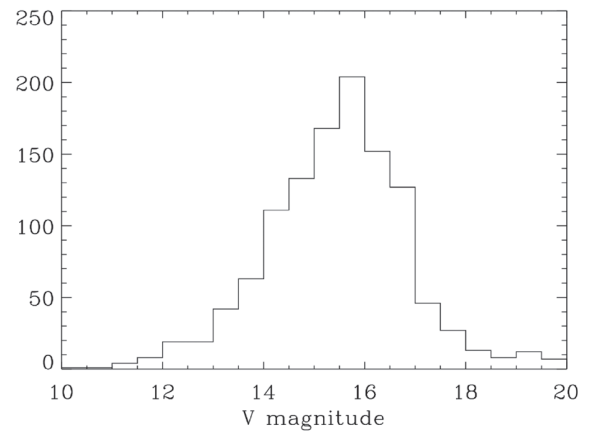
The sample assembled in this work also provides us with an excellent data set to investigate the WD luminosity function. To construct luminosity functions, we use the method developed by Schmidt (1968). In this method, each star is assigned to a volume defined by the maximum distance at which the star can be detected, given sample limitations such as a magnitude limit. In our sample, we define the maximum distance at which any star can be detected as:

$$d_{\max} = d \cdot 10^{\frac{V_{\lim} - V}{5}} \quad (3)$$

in which  $V$  is the observed  $V$  magnitude,  $V_{\lim}$  is the magnitude limit of the sample and  $d$  is the distance.

When constructing the luminosity function, the choice of the limiting magnitude is important. In figure 12, we show the histogram of  $V$  mag-

nitudes for our sample. The figure clearly shows that the sample no longer counts objects efficiently above  $V = 16.0$ , which we adopt as our magnitude limit. One must consider that our sample was drawn from a catalog comprised of many different surveys using various selection criteria, so our sample is the product of many different limiting magnitudes. Adopting a limiting magnitude of  $V = 16.0$  means some stars in our sample had  $d_{\max} < d$ , in which case we adopted  $d_{\max} = d$ .



**Figure 12: Histogram of  $V$  magnitudes for the full WD sample (parallax and model estimated distances) used in this work**

Source: The authors.

Because the distances in our sample are comparable to the scale height of the disk [(obtained by Boyle (1989))], corrections for a non-uniform density of WDs should be applied. From  $d_{\max}$ , we obtained  $V_{\max}$  for each star by using the following expression from Tinney et al. (1993):

$$V_{\max} = \Omega \left( \frac{h_0}{\sin b} \right)^3 [2 - (y^2 + 2y + 2) e^{-y}] \quad (4)$$

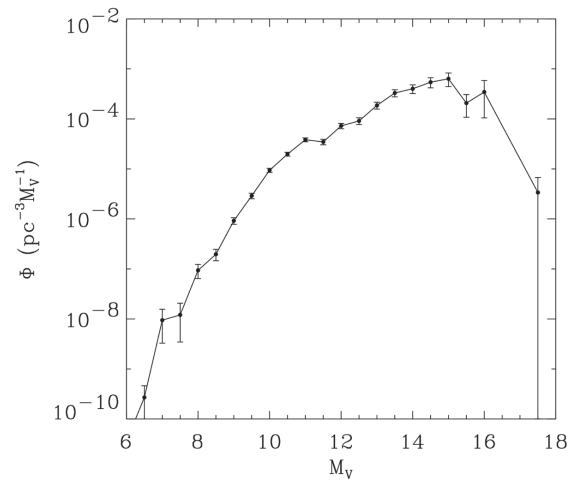
in which  $\Omega$  is the solid angle covered by the sample,  $h_0$  is the scale height and  $b$  is the Galactic latitude. For the value of  $\Omega$ , we adopted  $4\pi$  given the reasonably uniform coverage of the sky in our sample

(figure 2). We adopted the value of  $pc$  obtained by Boyle (1989) as the scale height, although we note that many authors have shown the weak dependence of the luminosity function on its value – see Wood (1992) for a complete discussion on the various dependencies of the luminosity function.

We calculated the luminosity function assuming that each star contributes to its particular luminosity or absolute magnitude bin. The error of each bin was determined following the prescription of Liebert et al. (1988):

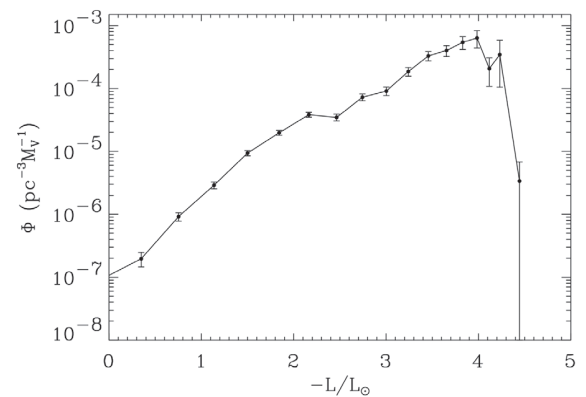
$$\delta = \sum \frac{1}{V_{\max}^2} \quad (5)$$

The luminosity function for the total sample studied in this work is presented in figure 13 as a function of absolute magnitude. In figure 14, we show the total luminosity function with absolute magnitudes converted to luminosities using the relation given in Liebert et al. (1988). The most important feature visible in the luminosity function is the turn-off at the faint end. In this region of the figure, two peaks were identified, one at and another at; however, due to the large error in the magnitude bin, we expect the latter to be not significant. Comparison of the turn-off to theoretical luminosity functions from other authors – for example, Wood (1992) shows that this is consistent with a disk age interval of 6 to 8 Gyr approximately. The peak at is consistent with the expected delay in cooling introduced by the onset of convective coupling and crystallization mentioned in Fontaine et al. (2001). According to Noh & Scalo (1990), it is possible that this peak could be partly due to a star formation burst and other pieces of evidence for such an event around 5 to 6 Gyr do exist [see figure 8 of Noh & Scalo (1990)]. One minor peak is visible at and could also be related to a star burst event at 0.3 Gyr, as mentioned in Noh & Scalo (1990), and references therein.



**Figure 13: Luminosity function of the full WD sample (parallax and model estimated distances) studied in this work including all spectral types (0.5 mag bin size)**

Source: The authors.



**Figure 14: Luminosity function of the full WD sample (parallax and model estimated distances) studied in this work with absolute magnitudes converted to luminosities**

Source: The authors.

The luminosity function for our sample is quite similar to the many efforts published previously – see Wood (1992), for example –, displaying the basic shape and structure. Some differences as to the actual density of WDs may appear and are likely due to our adoption of covering factor and scale height, which might not be the same in other efforts. The most important part however, the

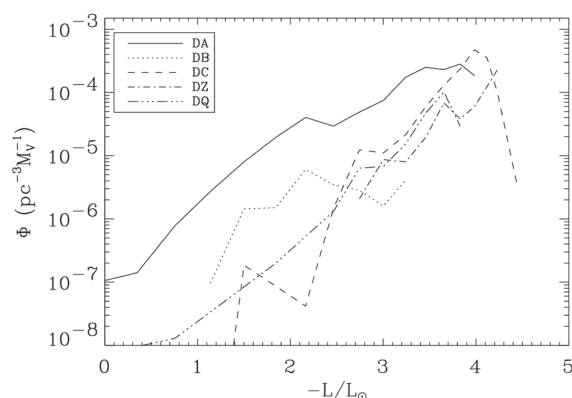


turn-off at the faint end of the luminosity function, is in agreement with all other studies.

One important limitation in our construction of the luminosity function is that we derived it from a sample comprised of many surveys, with many different selection criteria. We, therefore, cannot apply the usual test to ascertain its completeness, meaning that the shape of the function should be correct, but actual density values will be incorrect. This should have no implication on the results discussed below, as our focus is not to determine actual spatial densities of WDs, but rather to try to identify particular events such as star formation bursts and structure relevant to the cooling theory.

To reveal differences among the various WD types, we also constructed luminosity functions for the different spectral types of WDs in our sample. In figure 15, we show the luminosity functions for each type as a function of  $-L/L_{\odot}$ . In figure 16, we break out each luminosity function and show error bars for each magnitude bin. There is remarkable structure in these luminosity functions. We re-identify the peak at approximately  $M_V = 11.0$  ( $-\log(L/L_{\odot}) \approx 2.3$ ) in the DA and DB luminosity functions, as pointed out by Harris et al. (2006) and Noh & Scalo (1990). We also identify a clear concentration of DB WDs in a narrow magnitude range, between  $M_V = 9.0$  and  $M_V = 13.0$ , indicating a very narrow age interval for this particular class of WDs.

The turn off at the faint end is even more interesting when the different types of WDs are considered. The sample of DBs, DQs, DAs and DCs shows a turn-off point at increasingly faint magnitude values respectively. DZs do not appear to turn off at any point. A secondary peak is also apparent in the DC luminosity function at  $M_V \sim 12$ . We have investigated how robust these structural differences are by examining WDs within given distance constraints because



**Figure 15: Luminosity functions of the subsample studied in this work with spectral types discriminated. The bin size used was 0.5 mag**

Source: The authors.

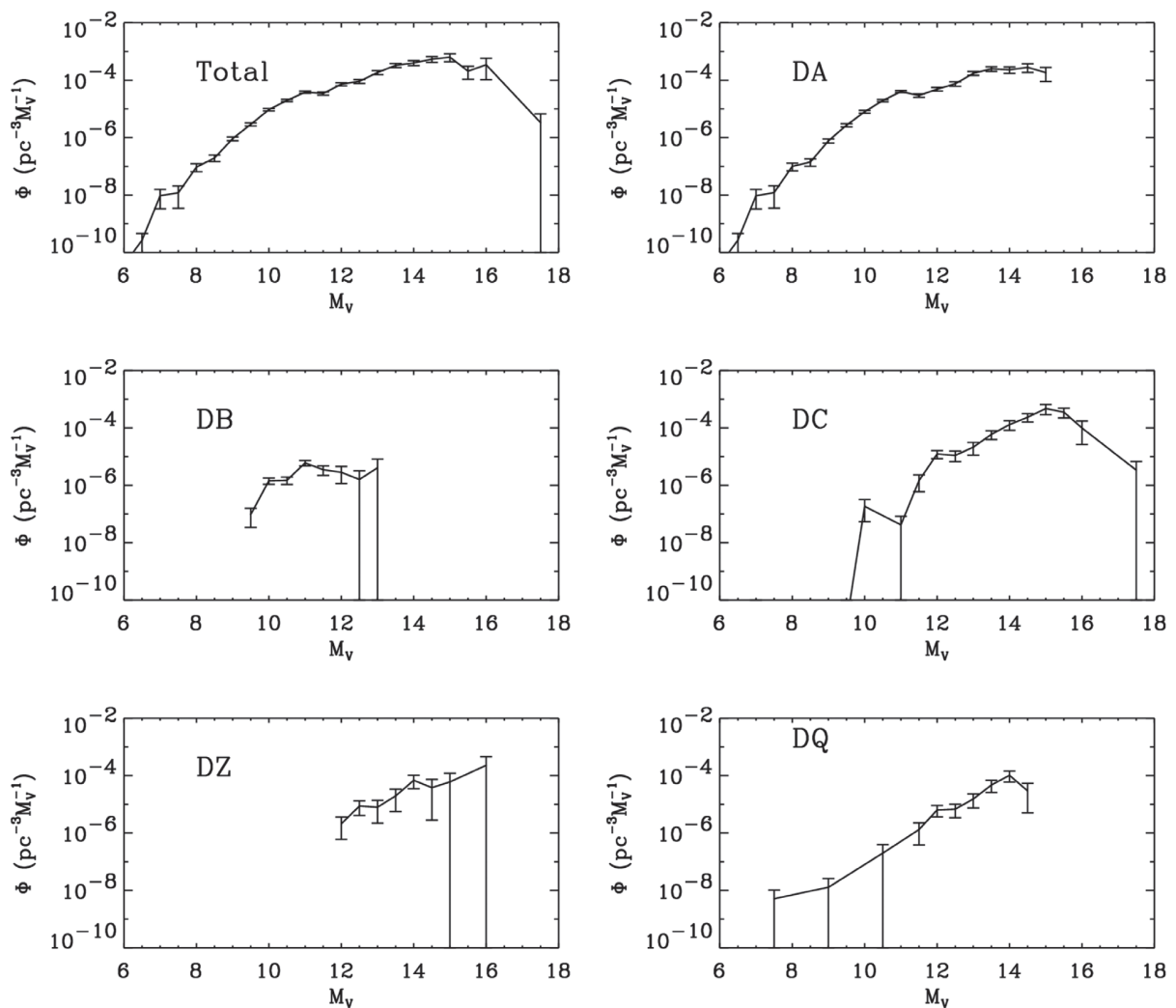
for volume limited samples of small distances we are less affected by selection and detection biases. The luminosity functions presented here are consistent down to 25 pc albeit with smaller numbers.

## 4 Conclusions

We presented here a study of a sample of *Villanova Catalog of Spectroscopically Identified White Dwarfs* using model techniques to obtain their physical characteristics and Galactic distribution. For stars with reliable parallaxes we determined their full physical properties ( $\log(g)$ , mass, cooling age). Examining the distribution of these properties with respect to the WD distances to the disk, we have not found any obvious relation. The histograms for the masses of the DA and non-DA WDs showed narrow distributions with peaks at approximately  $\log(g) \sim 8.1$ , in agreement with results found by other authors.

For the WDs that had  $(B-V)$  or  $(b-y)$  colors we have estimated distances, based on the assumption that  $\log(g) = 8.0$  for all objects, and shown that they are relatively reliable (errors of about





**Figure 16:** Luminosity functions of the sample studied in this work, including the error bars, for all spectral types. The bin size used was 0.5 mag

Source: The authors.

26% as discussed previously) given the minimal information required for their determination. With this sample of 1072 stars with parallax and estimated distances we have determined the solar distance to the Galactic disk and found that to be above the plane. This value is found to be in general agreement with other determinations given by Humphreys & Larsen (1995).

We have also inspected the binary fraction of the sample of WDs. In particular, we investigated the binary fraction and how it varied as a

function of disk distance  $z$ . Our sample did not present any noticeable gradient in the binary fraction out to 100 pc. Even though our sample did not encompass a large volume, the lack of a gradient could indicate that there is no reduction of the concentration of binaries at larger distances to the disk and more complete samples to greater distances are crucial to further test this result.

Using the precise parallax distances as well as the model estimated distances, we have con-



structed the luminosity function for our sample as well as for each individual spectral type as specified in the original catalog. The luminosity function for the whole sample does not present any new feature, but corroborates many previous results. The few differences related to the actual density for a given magnitude bin are likely due to our adopted value for the scale height of the WD distribution relative to the Galactic disk, as well as different distance estimates. However, we have focused on the relative shape of the luminosity function for the whole sample as well as the luminosity functions for individual spectral types. We have shown that each individual type has its own characteristic shape, likely related to the star formation history and physical processes relevant to each one. The luminosity function for DA white dwarfs agrees well with all previous results and shows some structure likely related to previously identified star formation bursts and details of the cooling processes involved. The luminosity function for DB WDs showed a very localized distribution indicating that this particular spectral type is short lived. The other spectral types showed more or less similar slopes with distinct turn-off points. The DC WDs seem to be representative either of the last stage of evolution for WDs or a favored formation scenario for DCs in early times in the Galaxy, given that they represent a large fraction of the older WDs, in contrast with DAs, which clearly dominate on the younger side. However, precise theoretical studies, similar to the one performed by Wood (1992) now should focus on each individual spectral type and the relevant physical processes. With the advances in large survey projects and theoretical models for WDs this could prove to be a powerful tool to further our understanding of fundamental stellar and Galactic evolution.

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