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Seismic Data Compression Using 2D Lifting-Wavelet Algorithms

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Abstract

Different seismic data compression algorithms have been developed in order to make the storage more efficient, and to reduce both the transmission time and cost. In general, those algorithms have three stages: transformation, quantization and coding. The Wavelet transform is highly used to compress seismic data, due to the capabilities of the Wavelets on representing geophysical events in seismic data. We selected the lifting scheme to implement the Wavelet transform because it reduces both computational and storage resources. This work aims to determine how the transformation and the coding stages affect the data compression ratio. Several 2D lifting-based algorithms were implemented to compress three different seismic data sets. Experimental results obtained for different filter type, filter length, number of decomposition levels and coding scheme, are presented in this work.

Key words: seismic data compression; wavelet transform; lifting

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Compresión de datos sísmicos usando algoritmos lifting-wavelet 2D

Resumen

Diferentes algoritmos para compresión de datos sísmicos han sido desarrollados con el objetivo de hacer más eficiente el uso de capacidad de almacenamiento, y para reducir los tiempos y costos de la transmisión de datos. En general, estos algoritmos tienen tres etapas: transformación, cuantización y codificación. La transformada *Wavelet* ha sido ampliamente usada para comprimir datos sísmicos debido a la capacidad de las ondículas para representar eventos geofísicos presentes en los datos sísmicos. En este trabajo se usa el esquema *Lifting* para la implementación de la transformada *Wavelet*, debido a que este método reduce los recursos computacionales y de almacenamiento necesarios. Este trabajo estudia la influencia de las etapas de transformación y codificación en la relación de compresión de los datos. Además se muestran los resultados de la implementación de diferentes esquemas lifting 2D para la compresión de tres diferentes conjuntos de datos sísmicos. Los resultados obtenidos para diferentes tipos de filtros, longitud de filtros, número de niveles de descomposición y esquemas de compresión son presentados en este trabajo.

Palabras clave: compresión de datos sísmicos; transformada wavelet; lifting

1 Introduction

The main strategy used by companies during the oil and gas exploration process is the construction of subsurface images which are used both to identify the reservoirs and also to plan the hydrocarbons extraction. The construction of those images starts with a seismic survey that generates a huge amount of seismic data. Then, the acquired data is transmitted to the processing center to be processed in order to generate the subsurface image.

A typical seismic survey can produce hundreds of terabytes of data. Compression algorithms are then desirable to make the storage more efficient, and to reduce time and costs related to network and satellite transmission. The seismic data compression algorithms usually require three stages: first a transformation, then a uniform or quasi-uniform quantization and finally a coding scheme. On the other hand, decompression

algorithms perform the inverse process of each one of these steps. Figure 1 shows the compression and decompression schemes.

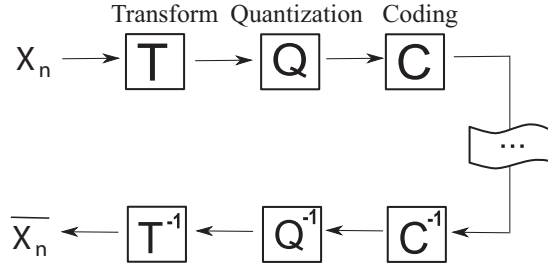


Figure 1: Data compression algorithm

The transformation stage allows de-correlating the seismic data, *i.e.*, the representation in terms of its coefficients (in the transformed domain) must be more compact than the original data. The wavelet transform offers well recognized advantages over other conventional transforms (*e.g.*, cosine and Fourier) because of its multi-resolution analysis with localization both in time and frequency. Hence this family of transformations has been widely used for seismic data compression [1],[2],[3],[4].

There is no compression after the transformation stage when the number of coefficients is the same as the number of samples in the original data. In lossy compression algorithms the stage that follows the transformation is an approximation of the floating-point transform coefficients in a set of integers. This stage is called *quantization* [5]. As will be seen in section 4, a uniform quantizer is generally used in seismic compression [2],[6],[7],[3].

Finally, a coding scheme is applied to the quantized coefficients. The coding scheme is a lossless compression strategy. It seeks a data representation with a small number of bits. In seismic data compression, the most used coding schemes have been Huffman [8],[9],[10],[11] and Arithmetic Coding [3],[12],[13],[7]. Sometimes a Run Length Encoding (RLE) [14] has been used prior to the entropy coding stage [8],[11],[7].

Different methods have been proposed to compress seismic data. The goal has been to achieve higher compression ratios at a quality above 40

dB in terms of the signal to noise ratio (SNR). Since each one of those algorithms uses different data sets, the comparison among them becomes difficult. This paper presents a comparative study for a specific set of seismic data compression algorithms.

We analyzed the wavelet-based algorithms using the *lifting* scheme, followed by a uniform quantization stage and then by a coding scheme. We have selected the *lifting* scheme since it requires less computation and storages resources than the traditional discrete wavelet transform (DWT) [15].

In this comparative study, we examined how the variation of some parameters affects the compression ratio for the same level of SNR. The parameters of interest in this paper are the type and length of the wavelet filter, the number of levels in the wavelet decomposition, and the type of coding scheme used. Our results are presented using graphics of compression ratio (CR) versus SNR. The implemented algorithms were tested on three different seismic datasets from Oz Yilmaz's book [16], which can be downloaded from *Center for Wave Phenomena* (ozdata.2, ozdata.10 and ozdata.28 respectively)¹. Those datasets are shot gathers, *i.e.*, seismic data method traditionally used to store the data in the field. Figure 2 shows a section of each dataset.

This article is organized as follows. Section 2 gives a brief overview of data compression. Sections 3 to 5 examine how the compression ratio is affected by each one of the three mentioned stages. Finally, the last section presents discussion and conclusions of this work.

2 Data compression

According to the Shannon theorem, a message of n symbols (a_1, a_2, \dots, a_n) can be compressed down to nH bits, on average, but no further [17], where H is called the *entropy*, a quantity that determines the average number of bits needed to represent a data set. The entropy is calculated by Equation 1, where P_i is the probability of the occurrence of a_i .

¹Available at: <http://www.cwp.mines.edu/cwpcodes/data/oz.original/>

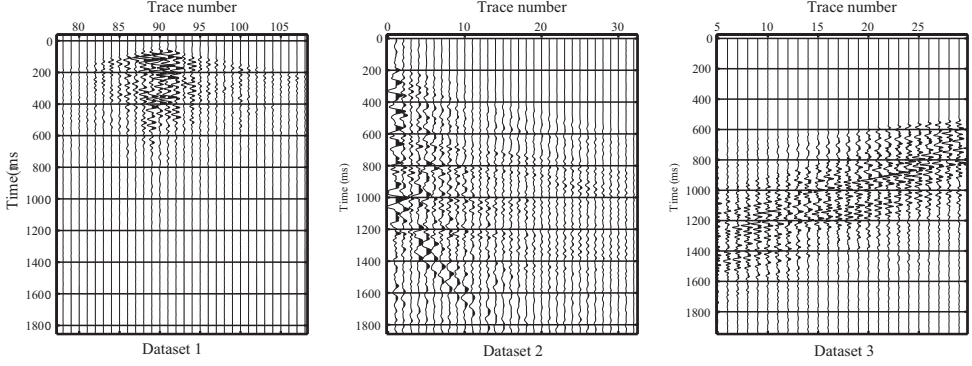


Figure 2: The three datasets used. The dataset 1 is a shot gather with 120 traces, having 1075 samples each. The dataset 2 is a shot gather with 120 traces, having 1375 samples each. The dataset 3 is a shot gather with 48 traces, having 2600 samples each.

$$H = - \sum_{i=1}^n P_i \log_2 P_i \quad (1)$$

The entropy is larger when all n probabilities are similar, and it is lower as they become more and more different. This fact is used to define the *redundancy* (R) in the data. The *redundancy* is defined as the difference between the current number of bits per symbol used (H_c) and the minimum number of bits per symbol required to represent the data set (Equation 2).

$$R = H_c - \left[- \sum_{i=1}^n P_i \log_2 P_i \right] = H_c + \sum_{i=1}^n P_i \log_2 P_i \quad (2)$$

In simple words, the redundancy is the amount of *wasted bits* –unnecessary bits– in the data representation. There are many strategies for data compression, but they are all based on the same principle: compressing data requires reducing redundancy.

Two important quantitative performance measures commonly used in data compression are the traditional *signal to noise ratio* (*SNR*) and the *Compression Ratio* (*CR*). The *SNR* is expressed in dB and defined by:

$$SNR_{dB} = 20 \cdot \log_{10} \left(\sum_{i=1}^n S_n^2 / \sum_{i=1}^n S_n'^2 \right) \quad (3)$$

Where S_n is the original data and S_n' is the decompressed data. The *CR* is defined as:

$$CR = \frac{\text{Number of bits without compression}}{\text{Number of bits with compression}} \quad (4)$$

2.1 Seismic data compression

The seismic data can be considered as a combination of three types of components: geophysical information, redundancy, and uncorrelated and broadband noise [18],[2]. In this way, different strategies to compress seismic data aim to decrease the redundancy.

$$\text{Seismic Data} = \text{Information} + \text{Redundancy} + \text{Noise} \quad (5)$$

3 The compression ratio according to the lifting-wavelet used

The DWT has traditionally been developed by convolutions, and its computational implementation demands a large number of computation and storage resources. A new approach has been proposed by Swelden [15] for wavelet transformation, which is called the *lifting scheme*. This mathematical formulation requires less computation and storage resources than the convolutional implementation.

Basically, the *lifting scheme* changes the convolution operations into matrix multiplications of the image with complementary filters and it allows for *in-place* computation, thus reducing the amount of both computation and storage resources [19]. At each step of the lifting method, the image

is filtered by a set of complementary filters (*i.e.*, a low-pass filter and its complementary high-pass filter) that allows perfect reconstruction of the image. In the next step of lifting the low-pass filtered image is again filtered by set of complementary filters, and so on. Each step of the lifting scheme can be inverted, so that the image can be recovered perfectly from its wavelet coefficients. The rigorous mathematical explanation of the wavelet transform using the lifting scheme can be found in [20],[15],[21].

We now show the use of the wavelet transform for compressing seismic data.

Figure 3 shows a histogram obtained from a seismic data set before and after a wavelet transform (using 6.8 biorthogonal filters). Clearly, from Figure 3, the wavelet transform data has a narrower distribution. Its entropy is 6.1 bits per symbol (See Equation 1), while the entropy for the original data is 7.4 bits per symbol, meaning that the wavelet transform data has a better chance to reach an improved compression ratio. In order to generate the histogram, the samples were converted from single precision floating point to integers and the frequencies were normalized.

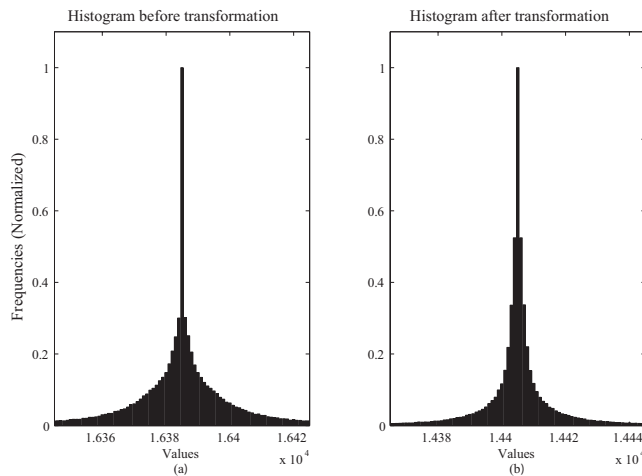


Figure 3: Histogram for a seismic data set. (a): histogram of the data values of the seismic data. (b): histogram of the coefficients of the wavelet transformation of the seismic data.

Thus, the transformation stage allows de-correlating the seismic data, *i.e.*, the representation in terms of wavelet coefficients is more compact than the original one.

3.1 The type of filter

To classify the compression ratio according to the selected type of filter, we used three different types of filters and we varied their lengths, and their number of vanishing moments. The types of filters used were: Biorthogonals (Bior), Cohen-Daubechies-Feauveau (CDF) and Daubechies (Db). The experiments were performed in the following order:

1. 2D lifting-wavelet decomposition (1-level) using different filters.
2. Uniform quantization from 6 to 14 quantization bits. Each mark in the figures corresponds to a number of quantization bits.
3. Huffman entropy coding.

Figures 4 to 6 show the performance of the algorithms based on Biorthogonals (Bior), Cohen-Daubechies-Feauveau (CDF) and Daubechies (Db). For simplicity we only show three filters for each dataset (low, medium and high performance). However, we observed that for each type of filter there is a range of vanishing moments that achieves a better performance.

Daubechies filters with a number of vanishing moments either 4 or 5, Biorthogonal filters with a number of vanishing moments from 5 to 8, and CDF filters with a number of vanishing moments from 3 to 5 achieved a better performance. These number of vanishing moments were required for both the decomposition filter and the reconstruction filter. In all cases, when either fewer or more of these vanishing moments were used, a lower CR was achieved.

Figure 7 compares the best results among the three types of filters and there were no significant differences between them.

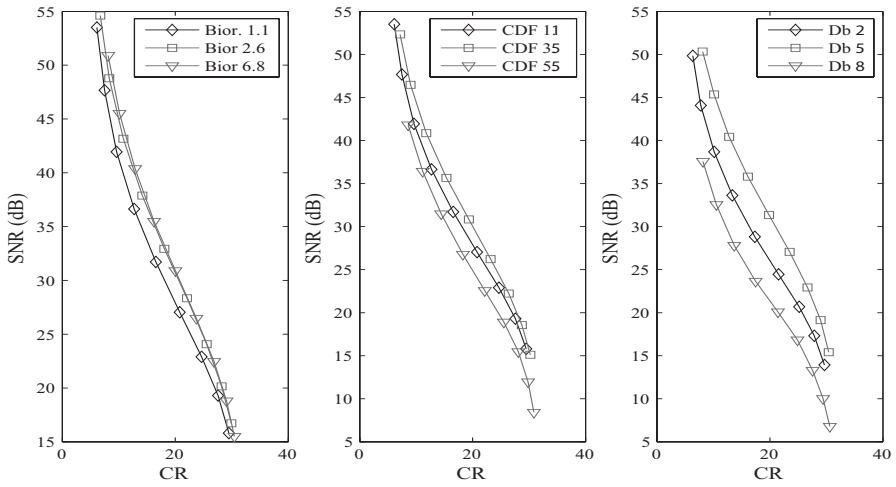


Figure 4: CR vs. SNR for the dataset Nr. 1.

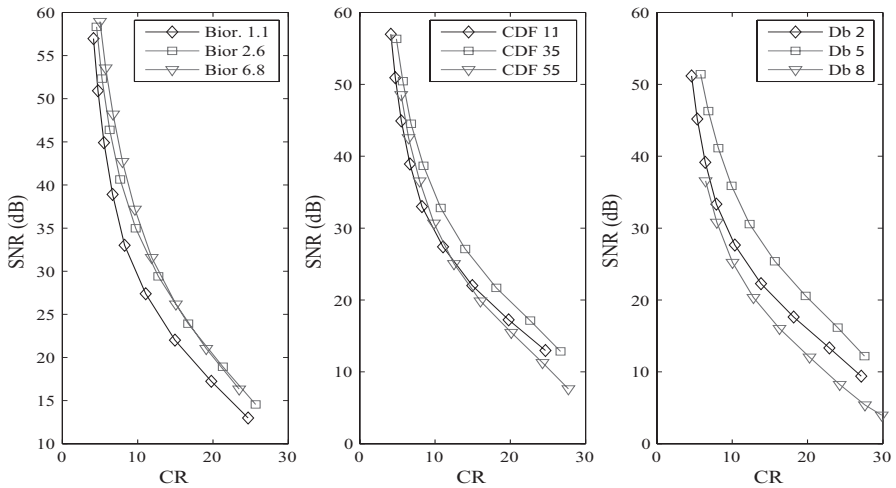


Figure 5: CR vs. SNR for the dataset Nr. 2

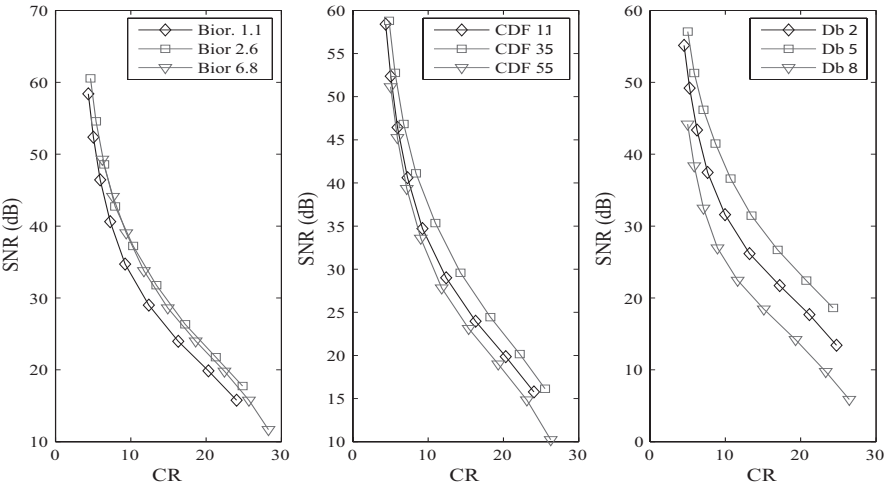


Figure 6: CR vs. SNR for the dataset Nr. 3

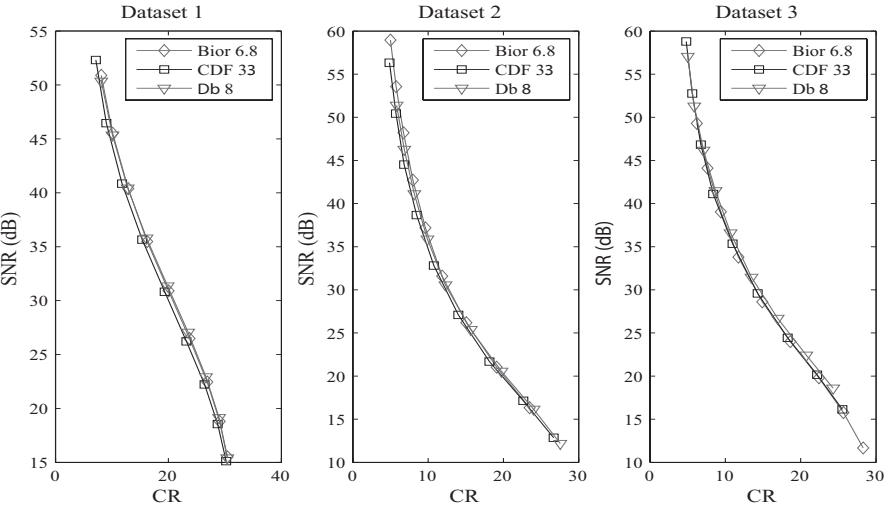


Figure 7: CR vs. SNR for all datasets. Best results for each type of filter at each dataset.

3.2 The number of the decomposition levels

The discrete wavelet transform (DWT) can be applied in different levels of decomposition [22]. We are interested to determine the influence of the decomposition levels in the improvement of the compression ratio. Therefore, we compress the seismic data using different levels of the wavelet decompositions. The experiment was performed in the following order:

1. 2D lifting-wavelet decomposition, using different levels of decomposition (From 1 to 7)
2. Uniform quantization using 12 quantization bits.
3. Huffman entropy coding.

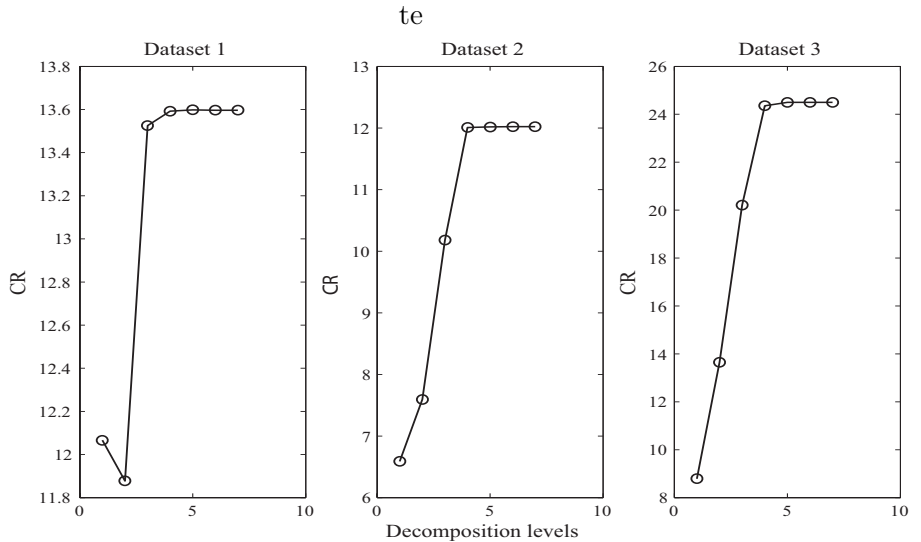


Figure 8: CR vs number of decomposition levels for all datasets.

Note in Figure 8 that as the number of decomposition levels increases, the CR increases. This is true for all datasets, until a particular number of decomposition levels is reached. After that level of decomposition,

the compression ratio holds almost constant. However, it is important to remark that as the number of decomposition levels increases, the SNR is reduced due to the loss of quality in the quantization process (Section 4). Therefore, it is necessary to choose the best compression ratio above 40 dB (in terms of SNR) among the different levels of decomposition. Table 1 summarizes our best results for each dataset.

Table 1: Better results above of 40 dB

Dataset	Level	SNR	CR
Data 1	4	42.45	11.01
Data 2	3	41.55	8.46
Data 3	2	42.08	7.45

4 The quantization stage

The wavelet transform stage reduces the entropy of the seismic data, but no compression has occurred so far, due to the fact that the number of coefficients is the same as the number of samples in the original seismic data. Achieving compression requires an approximation of the floating-point transform coefficients by a set of integers. This stage is called *scalar quantization*².

The quantization stage, denoted by $y_i = Q(x)$, is the process of mapping floating-point numbers (x) within a range (a, b) into a finite set of output levels (y_1, y_2, \dots, y_N) . Depending on how the y_i 's are distributed, the scalar quantizer can be uniform (Figure 9a) or non-uniform (Figure 9b).

A uniform quantizer is traditionally used in seismic compressing [2],[6],[7], [3], because the larger errors in the non-uniform quantization scheme are concentrated in the larger amplitudes (see Figure 9b), and usually the larger amplitudes for the seismic data contain the relevant geophysical information. On the other hand, the small amplitudes in the seismic data have a good chance to be noise. Thus, a uniform quantizer achieves the minimum entropy in seismic applications [5],[23]. An additional gain of using a uniform quantizer is its low computational complexity.

²The *scalar* term refers to each coefficient is independently approximated

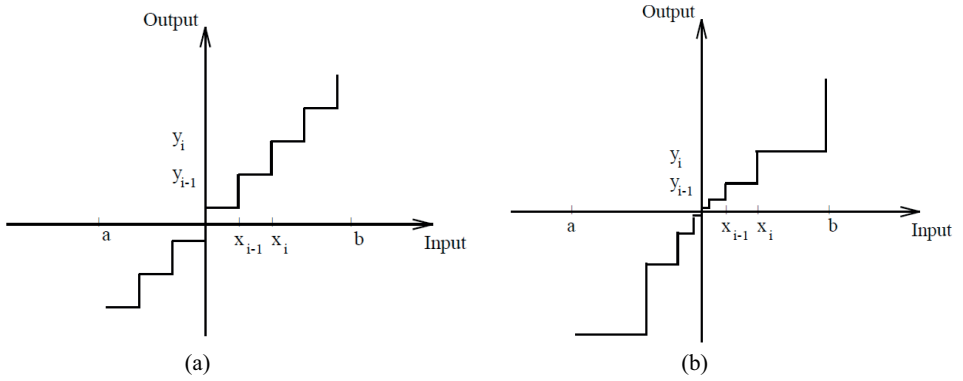


Figure 9: Uniform and non-uniform quantization [23]

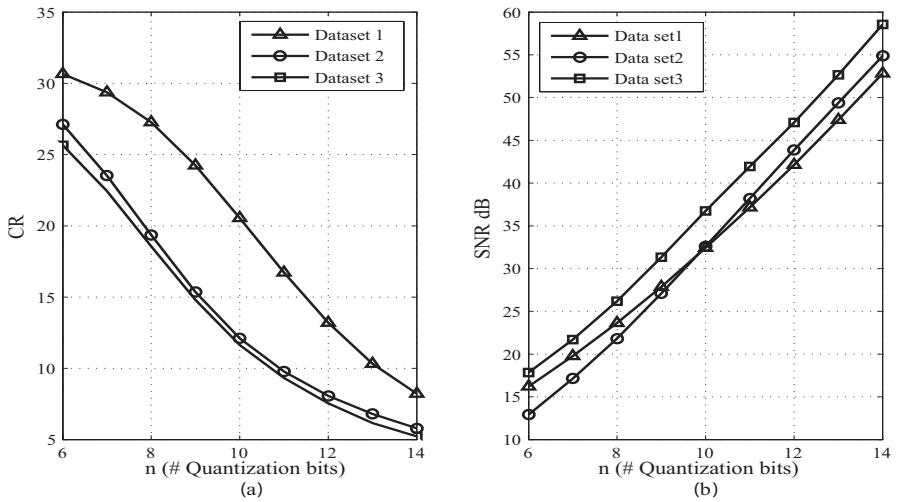


Figure 10: (a) CR vs number of quantization bits for the three datasets. (b) SNR vs number of quantization bits for the three datasets.

Mapping a *large* data set into a *small* one results in lossy compression. As the number of output levels is reduced, the data entropy is also reduced *i.e.*, we increase the possibility to compress the data (Section 2). However, after the quantization stage, a reduction in the SNR occurs due to the approximation process. Here the number of quantization bits determines the number of output levels 2^n . Figure 10-left shows how the compression ratio increases as the number of quantization bits is reduced, and Figure 10-right shows that the SNR is decreases as the number of quantization bits is reduced.

5 The compression ratio according to the coding scheme

Once the uniform quantizer is used, the data encoder needs to be selected. In this work, an entropy encoder is used in order to achieve good compression. The entropy coding stage is a lossless compression strategy. It seeks to represent the data with the lowest number of bits per symbol [24]. To classify the compression ratio according to the coding scheme, we tested two different coding schemes on the three data sets. The experiments were performed in the following order:

1. 2D Lifting-Wavelet decomposition (1 level) using a 6.8-Biorthogonal filter.
2. Uniform quantization from 6 to 14 bits.
3. Huffman and Arithmetic coding.

Figure 11 shows the performance of the algorithms based on *Huffman* and *arithmetic* coding scheme (CR vs SNR). Additionally, Figure 11 shows the maximum CR achieved when the entropy of the quantized wavelet coefficients is used.

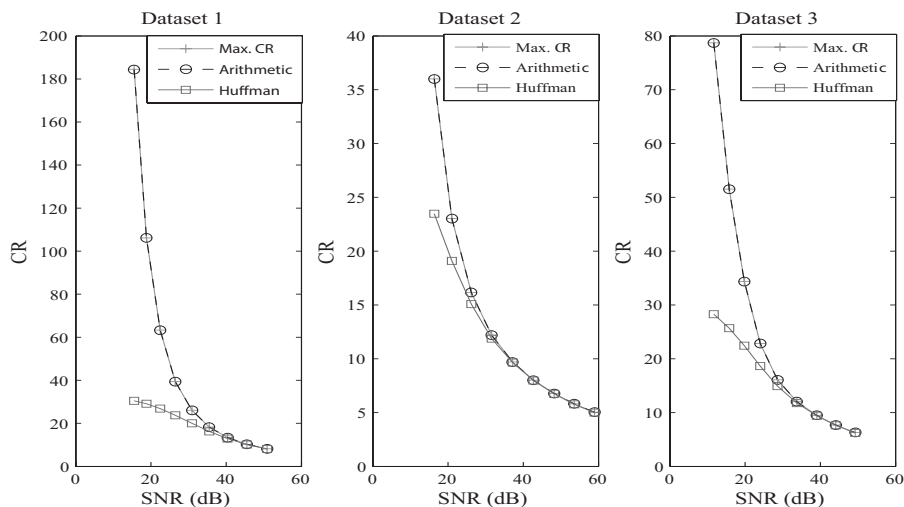


Figure 11: SNR vs CR for Huffman and arithmetic coding used to compress the three seismic datasets. Maximum CR achievable.

As is shown in Figure 11, the Arithmetic coding is very close to the maximum compression ratio, however, above 40 dB both Huffman and Arithmetic achieve a high performance.

6 Conclusions

One of the main goals of this paper is to attempt to know how both the transform stage and the coding stage affect the compression ratio.

Regarding the wavelet filter used, it seems that the performance, in terms of the SNR obtained for a given CR, is not associated with the type of filter, because it is possible to obtain a good compression performance using different types of wavelet filters (*e.g.*, Bior, CDF or Db). However, our results suggest that the performance is related to the the number of vanishing moments of the wavelet filter. Furthermore, the *more appropriate* number of levels of decomposition can not be established, since the compression ratio did not improve for a particular number of decomposition

levels. Previous results suggest that a *moderate* number of decomposition levels can be used and still we can get enough compression ratio.

The Arithmetic coding showed a superior performance for low levels of SNR. This codification scheme was very close to the maximum CR. However, for values of SNR above 40 dB, which is the level generally required, the performance of both Huffman and arithmetic coding showed similar performance and both were very close to the maximum CR. However, we consider that further research on selecting the best coding method based on the data and the previously transformation and quantization selected stages requires further analysis. This remains as an open problem for the seismic data compression. Further, it is important to remark that the arithmetic coding has a higher computational complexity than the Huffman coding. From the computational complexity perspective, the Huffman coding could be a better option, when the aim is to achieve a SNR above 40 dB.

We implemented several compression algorithms in order to study the influence of both the transform and the coding stage on the compression ratio. We underlined the importance of the number of vanishing moments in the wavelet filter and a *moderate* number of decomposition levels. In the quantization stage, we selected the uniform quantization, which is appropriate for seismic data since it helps to minimize errors in the geophysical information. Finally, we selected a Huffman coding which gives a high compression ratio with an SNR above 40 dB, and reduces the computational complexity in comparison to the arithmetic coding.

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